

# Development of a Polarized Positron Source for CEBAF

## Beam dynamics: Design and optimization

Sami Habet

IJCLab & JLab

February 13, 2023



# Plan

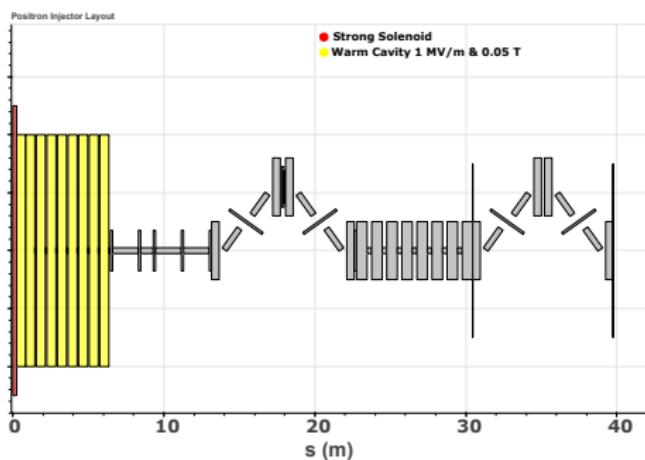
## ① Target optimization

## ② Collection system

## ③ Momentum collimation

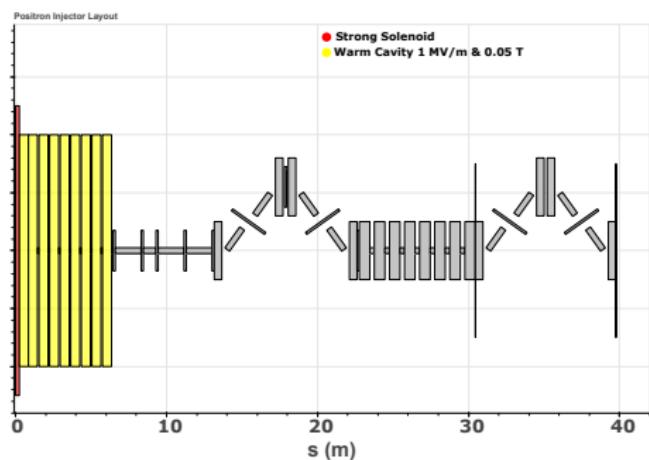
## ④ Longitudinal optimization

## ⑤ Conclusion



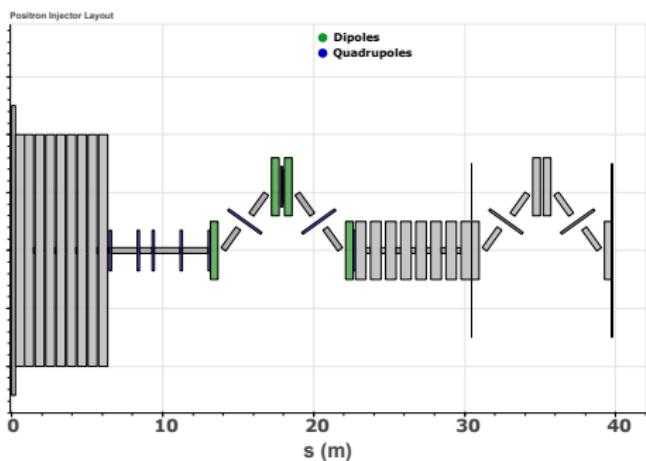
# Plan

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion



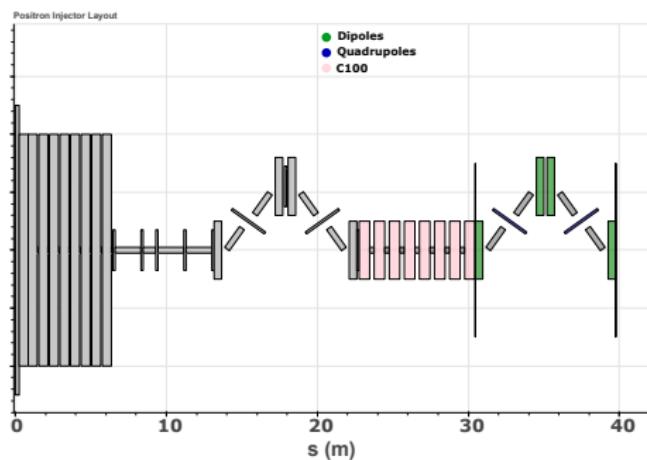
# Plan

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion



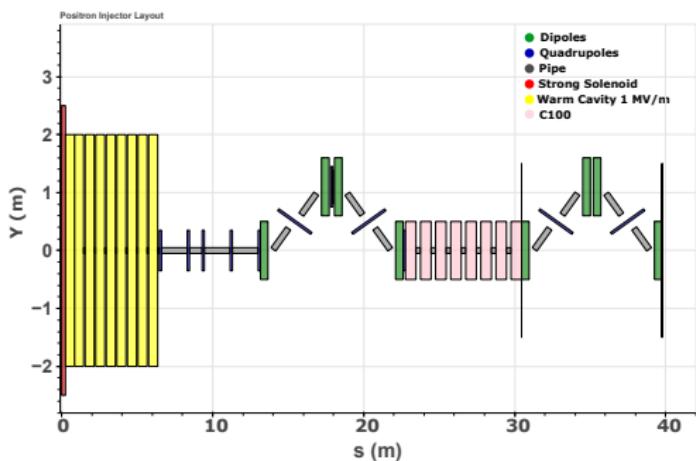
# Plan

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion



# Plan

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion



# Outline

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion  
Backup slides

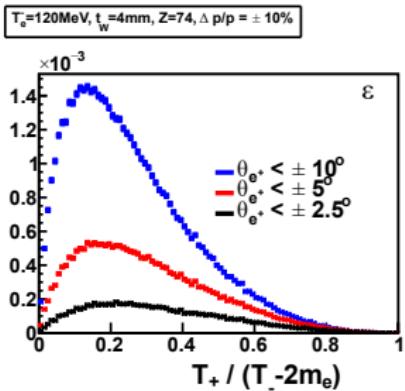
# Positron characterization

## Unpolarized mode

- Efficiency :  $\epsilon = \frac{N_{e^+}}{N_{e^-}}$

## Polarized mode

- Figure-of-Merit  $FoM = \epsilon P_{e^+}^2$



# Positron characterization

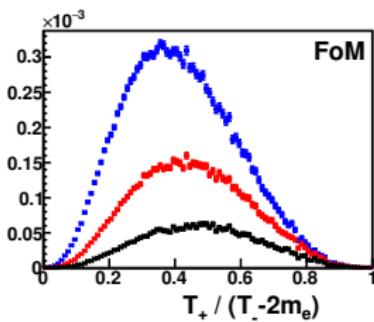
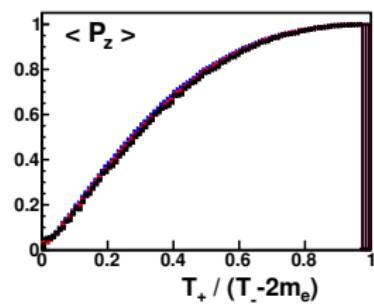
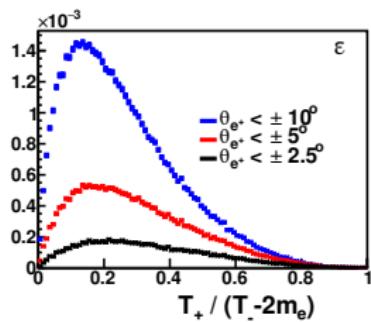
## Unpolarized mode

- Efficiency :  $\epsilon = \frac{N_{e^+}}{N_{e^-}}$

## Polarized mode

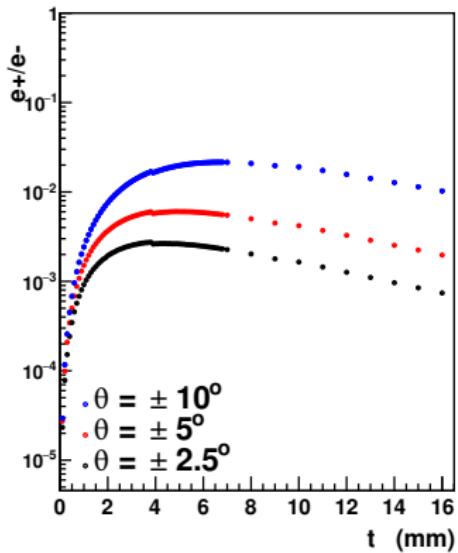
- Figure-of-Merit  $FoM = \epsilon P_{e^+}^2$

$T_e=120\text{MeV}$ ,  $t_W=4\text{mm}$ ,  $Z=74$ ,  $\Delta p/p = \pm 10\%$

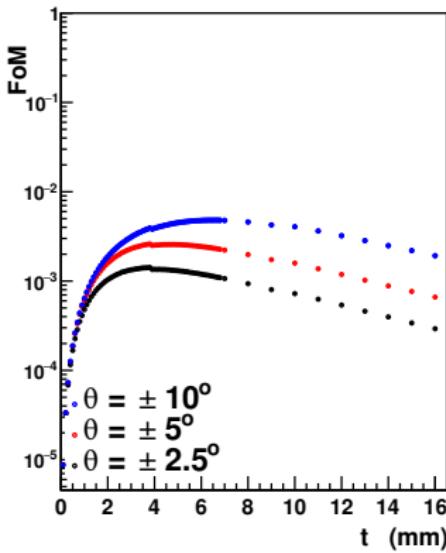


## Target thickness optimization

## Unpolarized mode

 $T_e = 120\text{ MeV}$ ,  $\Delta P / P = \pm 10\%$ ,  $Z = 74$ 

## Polarized mode



# Outline

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion  
Backup slides

# Quarter Waves Transformer

- Reduce the angular transverse spread  
 $x_p = \frac{p_x}{p_z}$  and  $y_p = \frac{p_y}{p_z}$ .
- Rotate the transverse phase space  $(x, x_p)$  and  $(y, y_p)$  at the exit of the QWT.
- Use a QWT as an energy filter.

# Quarter Waves Transformer

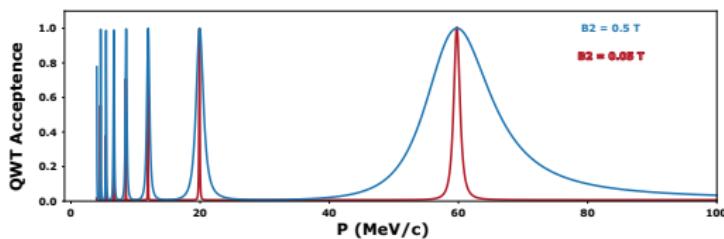
- Reduce the angular transverse spread  
 $x_p = \frac{p_x}{p_z}$  and  $y_p = \frac{p_y}{p_z}$ .
- Rotate the transverse phase space  $(x, x_p)$  and  $(y, y_p)$  at the exit of the QWT.
- Use a QWT as an energy filter.

# Quarter Waves Transformer

- Reduce the angular transverse spread
$$x_p = \frac{p_x}{p_z} \text{ and } y_p = \frac{p_y}{p_z}.$$
- Rotate the transverse phase space  $(x, x_p)$  and  $(y, y_p)$  at the exit of the QWT.
- Use a QWT as an energy filter.

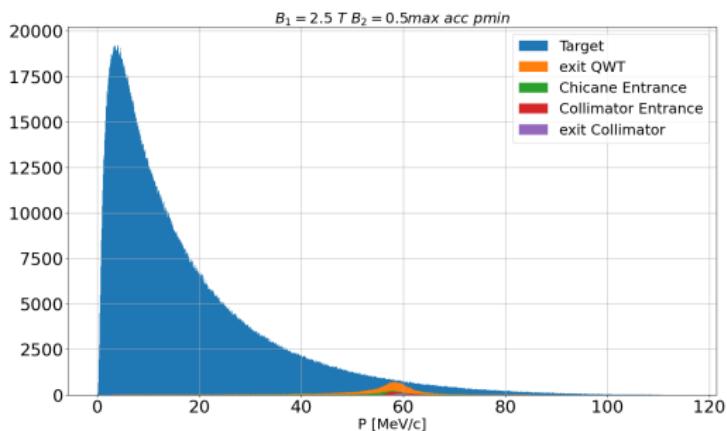
# Quarter Waves Transformer

- Reduce the angular transverse spread  
 $x_p = \frac{p_x}{p_z}$  and  $y_p = \frac{p_y}{p_z}$ .
- Rotate the transverse phase space ( $x, x_p$ ) and ( $y, y_p$ ) at the exit of the QWT.
- Use a QWT as an energy filter.



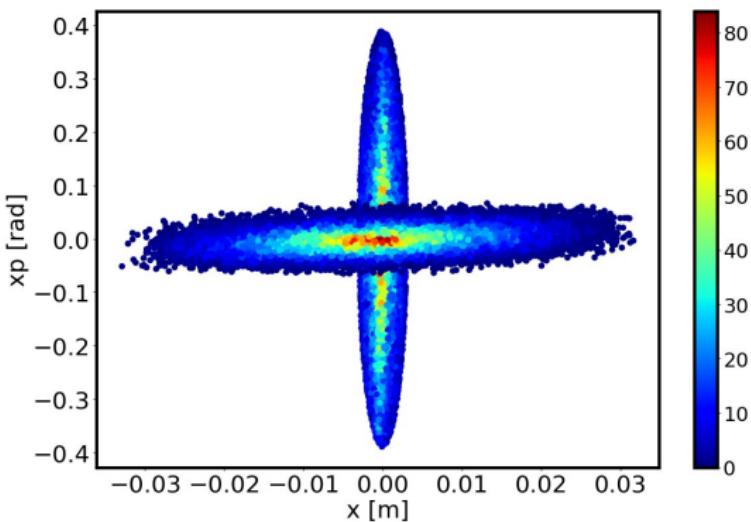
# Quarter Waves Transformer

- Reduce the angular transverse spread  $x_p = \frac{p_x}{p_z}$  and  $y_p = \frac{p_y}{p_z}$ .
- Rotate the transverse phase space  $(x, x_p)$  and  $(y, y_p)$  at the exit of the QWT.
- Use a QWT as an energy filter.



# Quarter Waves Transformer

- Reduce the angular transverse spread  
 $x_p = \frac{p_x}{p_z}$  and  $y_p = \frac{p_y}{p_z}$ .
- Rotate the transverse phase space ( $x, x_p$ ) and ( $y, y_p$ ) at the exit of the QWT.
- Use a QWT as an energy filter.



# Accelerating warm section

## Goal

- Reduce the energy spread of the accepted  $e^+ @ p = 60 \text{ MeV}/c$
- $f = 1497 \text{ Mhz}$
- $E = 1 \text{ MV}/m$
- $L_{cell} = 0.2 \text{ cm}$
- $r_{cell} = 3 \text{ cm}$

# Accelerating warm section

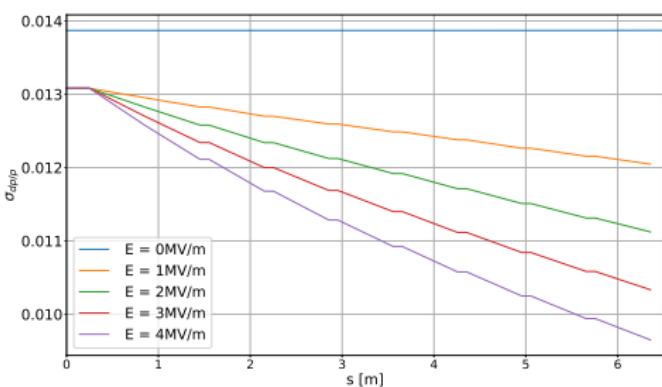
## Goal

- Reduce the energy spread of the accepted  $e^+ @ p = 60 \text{ MeV}/c$
- $f = 1497 \text{ MHz}$
- $E = 1 \text{ MV}/m$
- $L_{cell} = 0.2 \text{ cm}$
- $r_{cell} = 3 \text{ cm}$

# Accelerating warm section

## Goal

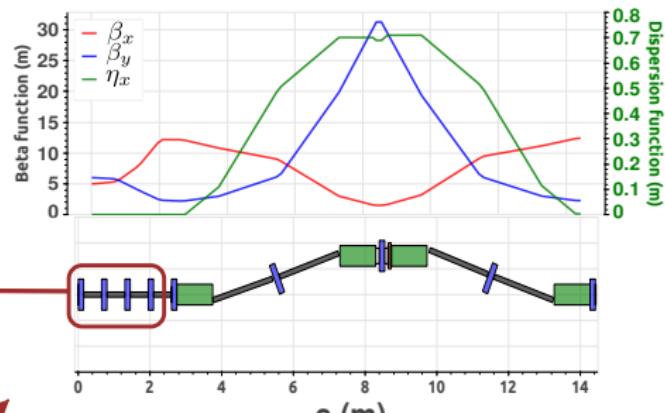
- Reduce the energy spread of the accepted  $e^+$  @  $p = 60 \text{ MeV}/c$
- $f = 1497 \text{ MHz}$
- $E = 1 \text{ MV/m}$
- $L_{cell} = 0.2 \text{ cm}$
- $r_{cell} = 3 \text{ cm}$



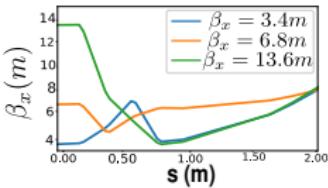
# Outline

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion  
Backup slides

# Beam size optimization



Matching section



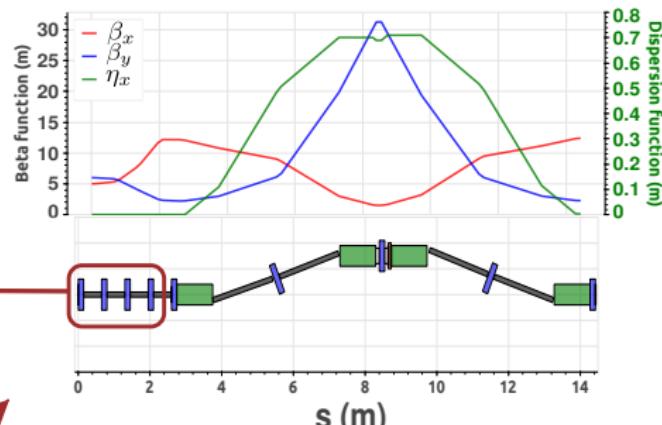
● Periodic Twiss in FODO:

$$\beta_{x,y_{in}} = \beta_{x,y_{out}}$$

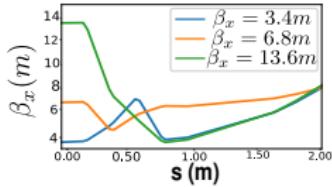
● Minimum beam size condition:

$$\beta_x = \beta_{x,MIN} \longrightarrow \alpha_x = 0$$

# Beam size optimization



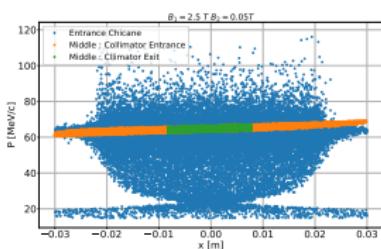
Matching section



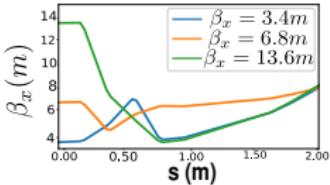
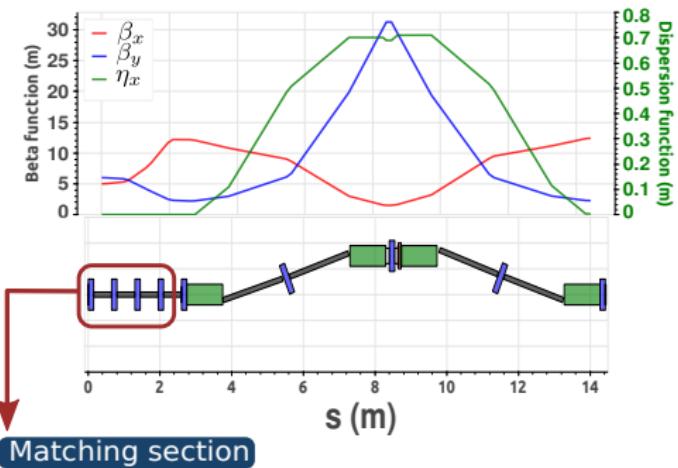
- **Periodic Twiss in FODO:**  

$$\beta_{x,y_{in}} = \beta_{x,y_{out}}$$
- **Minimum beam size condition:**  

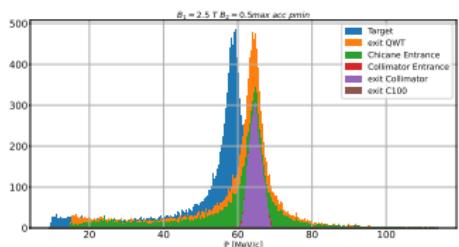
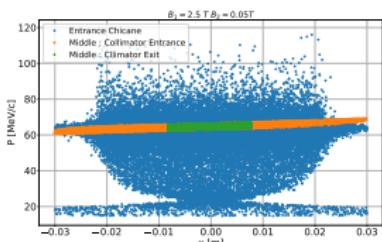
$$\beta_x = \beta_{x,MIN} \longrightarrow \alpha_x = 0$$



# Beam size optimization



- **Periodic Twiss in FODO:**  
 $\beta_{x,y_{in}} = \beta_{x,y_{out}}$
- **Minimum beam size condition:**  
 $\beta_x = \beta_{x,MIN} \longrightarrow \alpha_x = 0$



# Outline

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion  
Backup slides

# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$
- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$
- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.

# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$
- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$
- Where:
  - $R_{56}$  : Longitudinal chicane element.
  - $k = 2\pi \frac{f}{c} [m^{-1}]$
  - $f$  is the cavity frequency
  - $eV_0$  Cavity acceleration [MeV]
  - $E_0$  Central energy [MeV]
  - $\phi$  Cavity phase advance.

# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$

- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$

- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.

# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$
- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$
- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.

# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

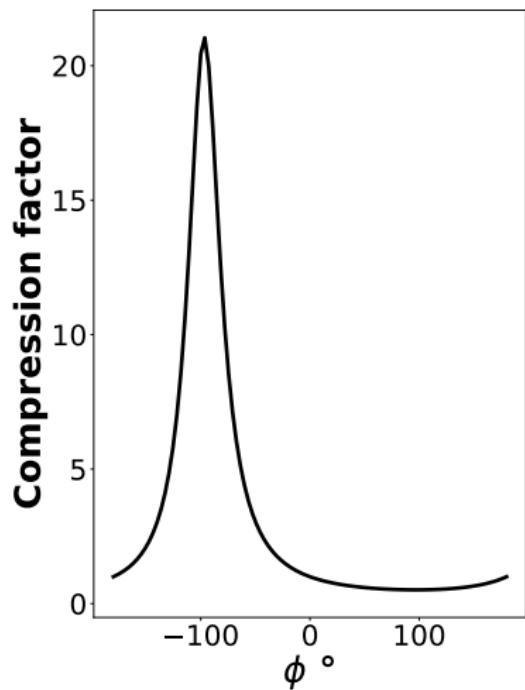
$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$

- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$

- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.



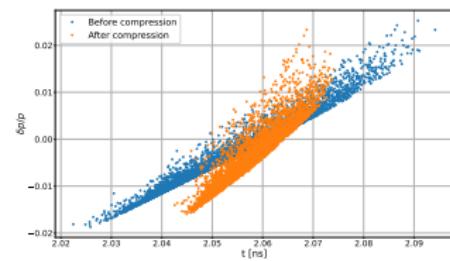
# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$
- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$
- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.



# Longitudinal optimization: Energy spread and bunch length

- **Compression factor =**

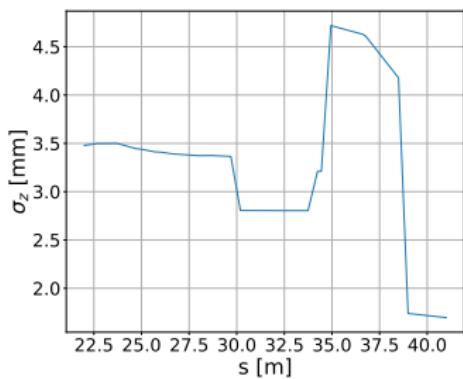
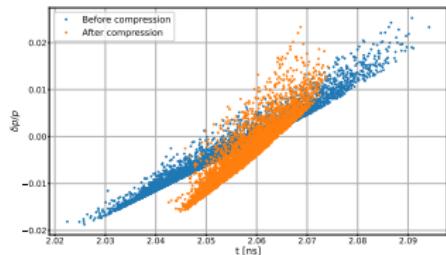
$$\frac{\text{Bunch length}_{\text{Entrance}}}{\text{Bunch length}_{\text{Exit}}}$$

- $C = \frac{1}{1 + [R_{56} \times \kappa]}$

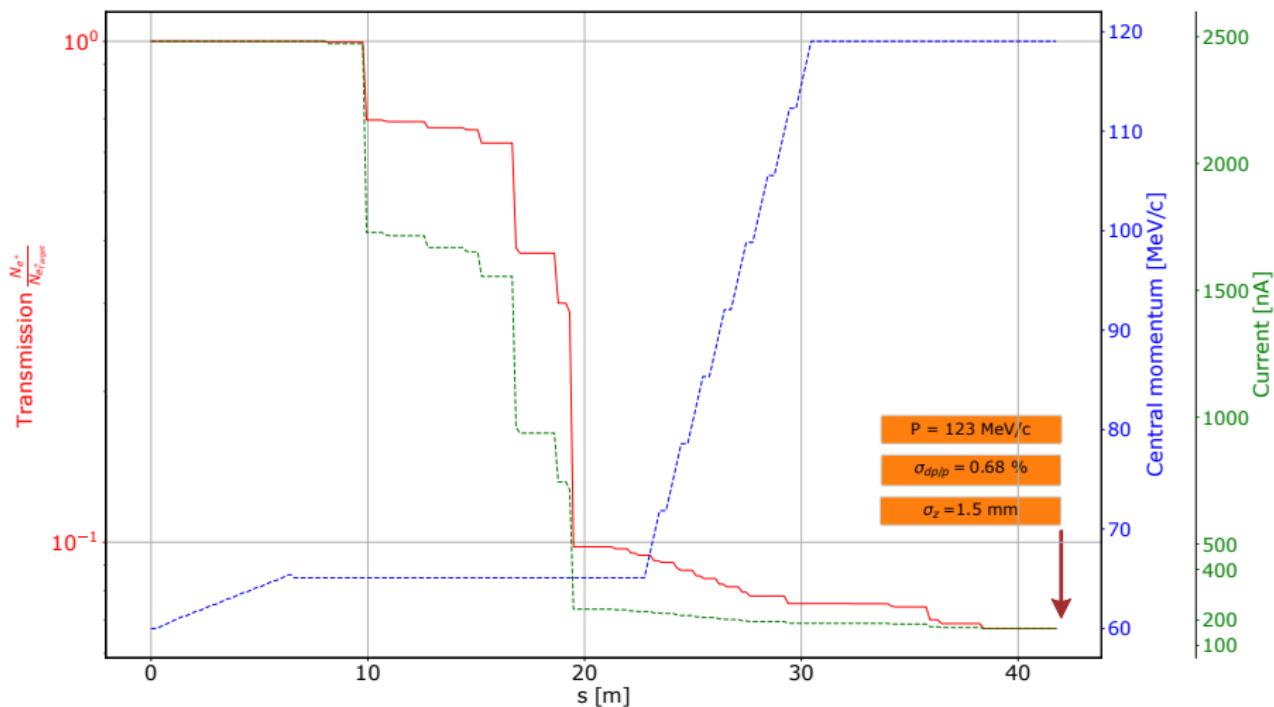
- $\kappa = \frac{d\delta_p}{dz} = \frac{-keV_0}{E_0 + eV_0 \cos \phi} \sin \phi$

- Where:

- $R_{56}$  : Longitudinal chicane element.
- $k = 2\pi \frac{f}{c} [m^{-1}]$
- $f$  is the cavity frequency
- $eV_0$  Cavity acceleration [MeV]
- $E_0$  Central energy [MeV]
- $\phi$  Cavity phase advance.



# Transmission and Current



# Summary

Params	e <sup>-</sup> beam	Target	Exit one period	Exit
$\sigma_{dp/p}$ [%]			1.3870	0.68
$\sigma_z$ [m]			0.0002	0.0016
$\sigma_x$ [m]	0.0005		0.0028	0.0081
$\sigma_{xp}$ [rad]	pencil beam		0.0021	0.0007
N $\epsilon_x$ [mrad]			0.019	0.0014
N $\epsilon_y$ [m rad]			0.02	0.0014
p Central [MeV/c]	120		60	123
e <sup>+</sup>	1 mA		2482 nA	170 nA

# Outline

- ① Target optimization
- ② Collection system
- ③ Momentum collimation
- ④ Longitudinal optimization
- ⑤ Conclusion  
Backup slides

# Conclusion

- The performance of the positron system is heavily influenced by the central momentum. For a high yield of positrons, the central momentum should be set to 15 MeV/c, while a high polarization requires a central momentum of 60 MeV/c.
- The QWT helps the selection of the desired momentum and reduces the spread of transverse angles.
- The accelerating section exerts significant influence on the longitudinal plane, thereby reducing the energy spread to meet the CEBAF requirement of  $\sigma_{dp/p} = \pm 1\%$ .
- For improved compression, the energy spread at the exit of the C100 must be at least five times smaller.
- Expecting higher current for the unpolarized mode P=15 MeV/c.

## Conclusion

- The performance of the positron system is heavily influenced by the central momentum. For a high yield of positrons, the central momentum should be set to 15 MeV/c, while a high polarization requires a central momentum of 60 MeV/c.
- The QWT helps the selection of the desired momentum and reduces the spread of transverse angles.
- The accelerating section exerts significant influence on the longitudinal plane, thereby reducing the energy spread to meet the CEBAF requirement of  $\sigma_{dp/p} = \pm 1\%$ .
- For improved compression, the energy spread at the exit of the C100 must be at least five times smaller.
- Expecting higher current for the unpolarized mode P=15 MeV/c.

## Conclusion

- The performance of the positron system is heavily influenced by the central momentum. For a high yield of positrons, the central momentum should be set to 15 MeV/c, while a high polarization requires a central momentum of 60 MeV/c.
- The QWT helps the selection of the desired momentum and reduces the spread of transverse angles.
- The accelerating section exerts significant influence on the longitudinal plane, thereby reducing the energy spread to meet the CEBAF requirement of  $\sigma_{dp/p} = \pm 1\%$ .
- For improved compression, the energy spread at the exit of the C100 must be at least five times smaller.
- Expecting higher current for the unpolarized mode P=15 MeV/c.

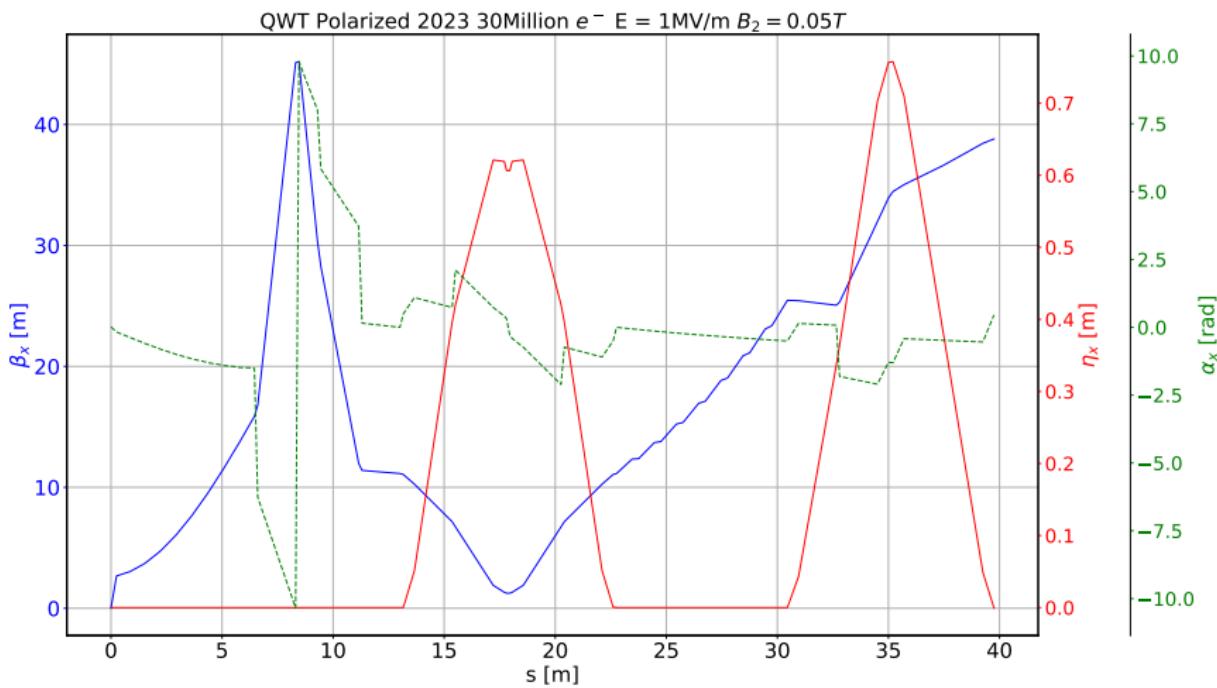
## Conclusion

- The performance of the positron system is heavily influenced by the central momentum. For a high yield of positrons, the central momentum should be set to 15 MeV/c, while a high polarization requires a central momentum of 60 MeV/c.
- The QWT helps the selection of the desired momentum and reduces the spread of transverse angles.
- The accelerating section exerts significant influence on the longitudinal plane, thereby reducing the energy spread to meet the CEBAF requirement of  $\sigma_{dp/p} = \pm 1\%$ .
- For improved compression, the energy spread at the exit of the C100 must be at least five times smaller.
- Expecting higher current for the unpolarized mode P=15 MeV/c.

## Conclusion

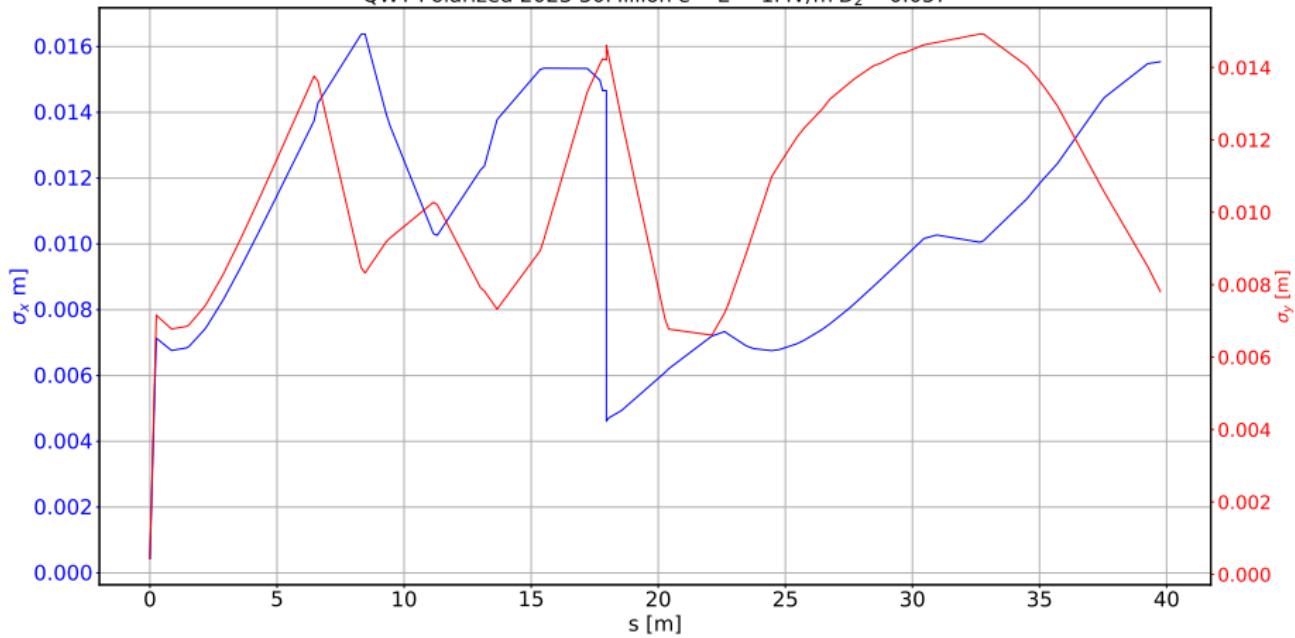
- The performance of the positron system is heavily influenced by the central momentum. For a high yield of positrons, the central momentum should be set to 15 MeV/c, while a high polarization requires a central momentum of 60 MeV/c.
- The QWT helps the selection of the desired momentum and reduces the spread of transverse angles.
- The accelerating section exerts significant influence on the longitudinal plane, thereby reducing the energy spread to meet the CEBAF requirement of  $\sigma_{dp/p} = \pm 1\%$ .
- For improved compression, the energy spread at the exit of the C100 must be at least five times smaller.
- Expecting higher current for the unpolarized mode P=15 MeV/c.

## Twiss functions

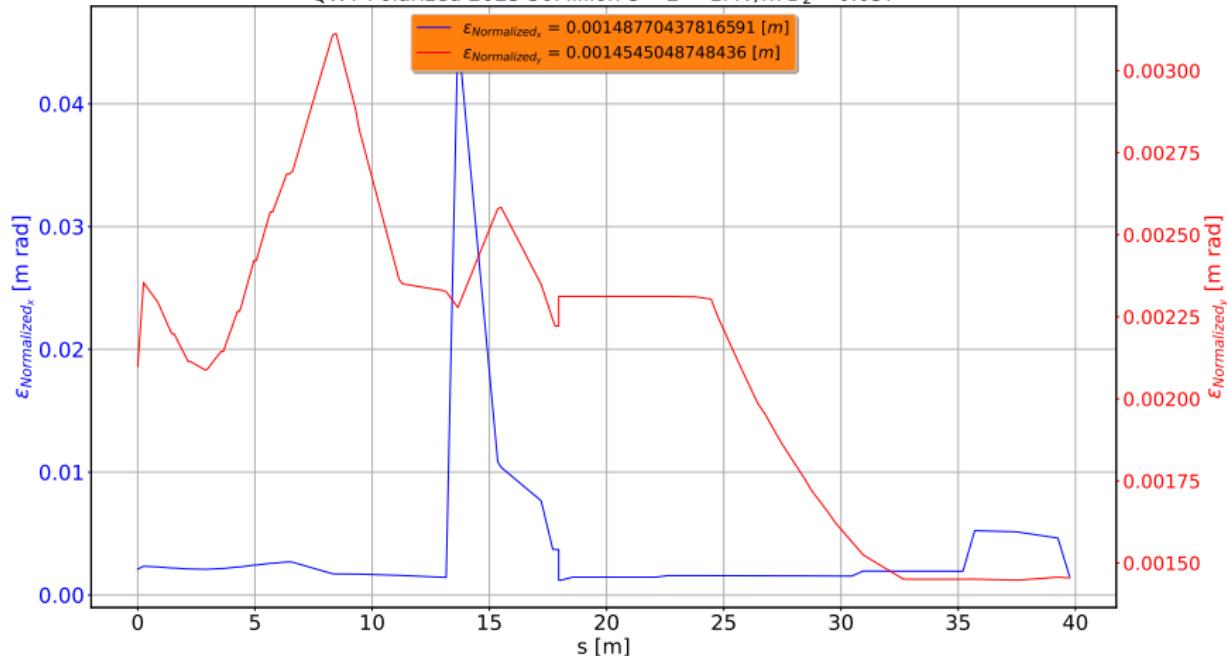


# Beam size

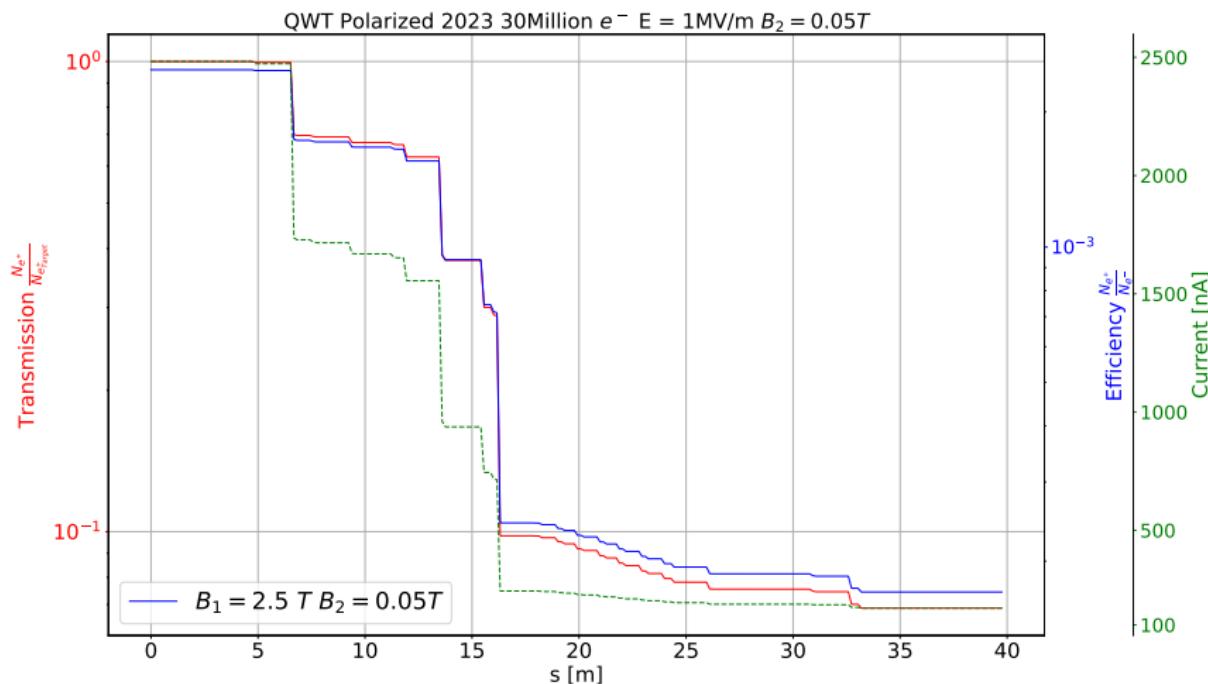
QWT Polarized 2023 30Million  $e^-$   $E = 1\text{MV/m}$   $B_2 = 0.05T$



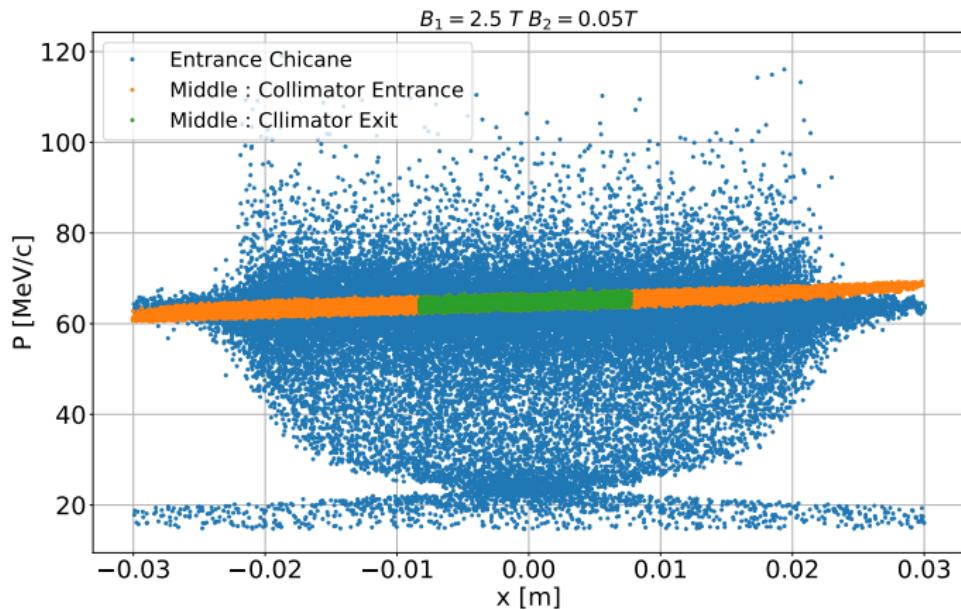
## Normalized emittance

QWT Polarized 2023 30Million e<sup>-</sup> E = 1MV/m B<sub>2</sub> = 0.05T

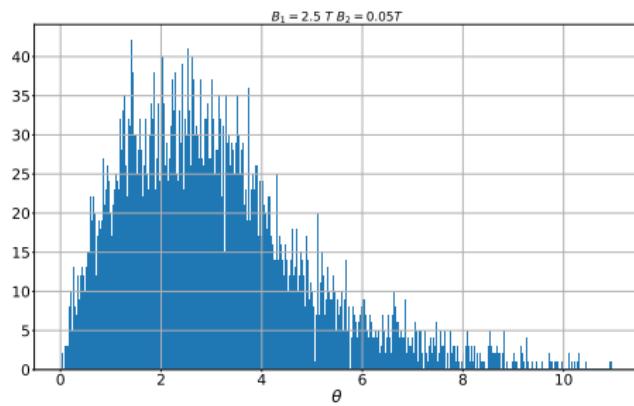
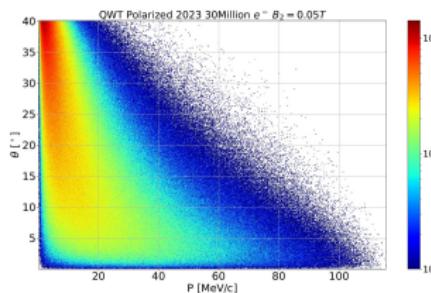
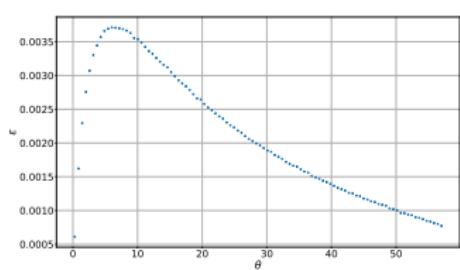
## Transmission and current



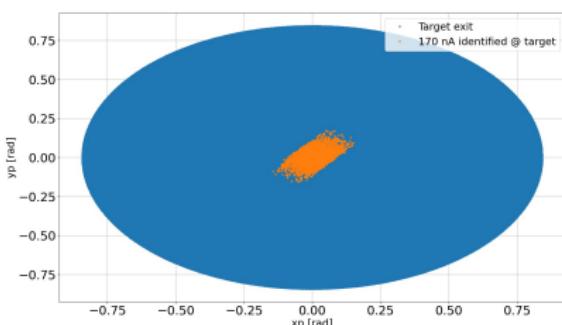
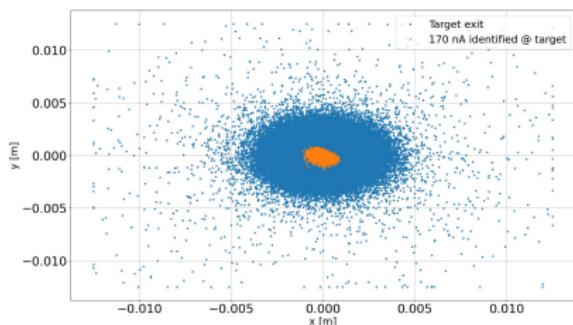
# Momentum collimation



# Angular distribution



# Transverse space



- The transmitted positrons are within the acceptance of the QWT
- $p_t^{QWT} = \frac{eB_1R}{2} . = 10.31^\circ$
- $r_0^{QWT} = \frac{B_2}{B_1} R = 0.6 \text{ mm}$