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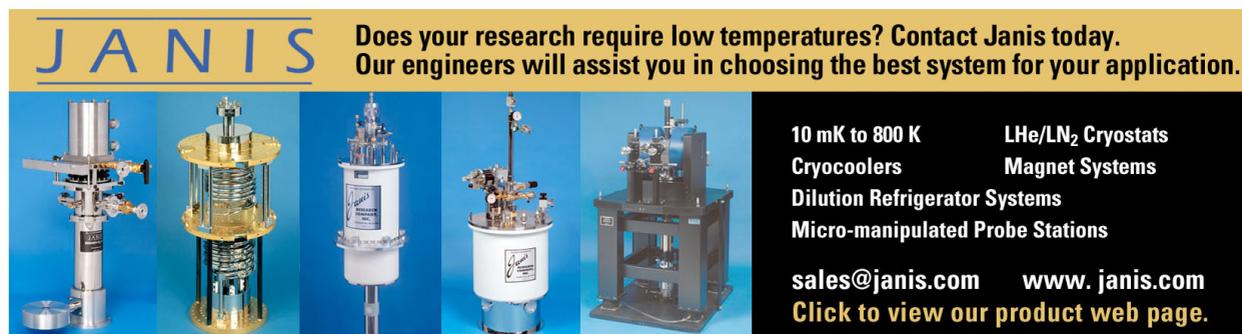
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Calibration of a Mott electron polarimeter: Comparison of different methods

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The accuracy of the calibration of a Mott polarimeter with a recently suggested method that uses an auxiliary target is compared with the accuracy obtained with the classical double-scattering experiment in its improved form. It turns out that the former method is affected by depolarization of the polarized incident beam in the auxiliary target. This systematic error source can, however, be eliminated by performing an additional asymmetry measurement.

I. INTRODUCTION

The interest in the accuracy of electron polarimetry has revived in the past few years. The issue came up because major advances in polarized-electron sources had the consequence that the accuracy of many experiments with polarized electrons is no longer limited by statistics but rather by the uncertainty in the measurement of electron polarization.

The most common method for electron-polarization analysis is the measurement of the left-right scattering asymmetry A of an electron beam with polarization normal to the scattering plane. (For a recent review on this "Mott electron polarimetry," see Ref. 1.) When L and R are the intensities scattered through the same angle Θ to the left and right, respectively, one has

$$A = (L - R) / (L + R). \quad (1)$$

From this asymmetry one obtains the electron polarization

$$P = A / S_{\text{eff}} \quad (2)$$

if the analyzing power S_{eff} (effective Sherman function) of the target is known.

By "calibration" of a Mott detector we mean in the following the determination of its effective analyzing power S_{eff} which differs from the value that is usually calculated for free atoms. Its exact value is affected by multiple scattering and depends in a complicated way on the design parameters of the polarimeter. Careful experimental analyses^{1,2} of recent years have shown that the calibration of a Mott analyzer with an accuracy of 1% or below is a difficult problem which has frequently been underestimated in the past.

A standard method of calibration is based on the double scattering of an initially unpolarized electron beam. If the parameters of the first and second scattering process (e.g., thickness of the target, electron energy, angles) are the same, S_{eff} follows from the measured asymmetry A according to

$$A = S_{\text{eff}}^2. \quad (3)$$

In a recent paper³ we have described how this method has been improved to yield an accuracy better than 1%.

There are other calibration methods which are anticipated to yield comparable accuracy. One can observe the

scattering asymmetry A of a polarized electron beam whose polarization P is measured simultaneously by using the circularly polarized impact radiation which the polarized electrons produce when they excite helium atoms.^{4,5} In another method suggested by Hopster and Abraham⁶ one also employs a polarized beam, performing additional measurements with an auxiliary target in order to eliminate the electron polarization from the equations used to evaluate S_{eff} . This will be substantiated in the following chapter.

The calibration is relatively easy if one assumes that one has an electron source of well-known polarization P , because then S_{eff} is simply obtained by a measurement of the asymmetry A and evaluation of Eq. (2). Needless to say, in this case the value of P cannot be determined with the polarimeter to be calibrated but has to be derived from physical principles or independent measurements.⁷

In one of our projects we apply various methods of polarimeter calibration trying to compare their reliability and practical applicability. If one aims at accuracies better than 1% for the calibration one has to pay great attention to the systematic errors of the measurement. In order to verify the accuracy claimed one can compare various independent calibration methods, checking whether they yield—within the error limits—the same result for one and the same Mott detector. Only if this is the case can one be sure to have successfully coped with the systematic errors.

In this paper we report on the calibration of a Mott analyzer using the idea suggested by Hopster and Abraham⁶ which will be called "auxiliary-target method" in the following. Comparison of this method with the calibration by double scattering shows that its accuracy is limited by a systematic depolarization effect resulting from multiple scattering in the auxiliary target.

II. CALIBRATION OF A MOTT DETECTOR USING THE AUXILIARY-TARGET METHOD

In order to determine the analyzing power S_{eff} of the Mott detector one can perform the following measurements:

(i) The primary beam of polarization P_0 hits the target of the Mott detector directly [cf. Fig. 1(i)]. One finds the left-right asymmetry

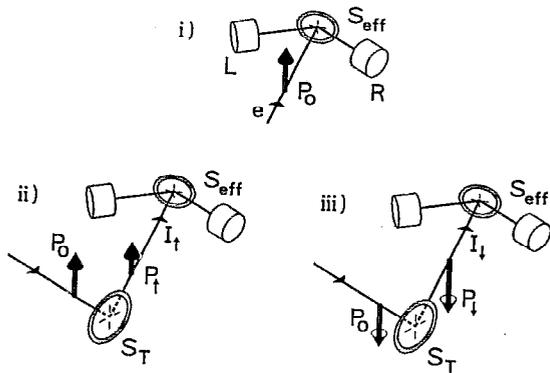


FIG. 1. Asymmetry measurements for determination of the analyzing power S_{eff} of a Mott detector.

$$A_0 = \frac{L-R}{L+R} = P_0 S_{\text{eff}}. \quad (4)$$

(ii) The primary beam is scattered from the auxiliary target [cf. Fig. 1(ii)]. The incident polarization P_0 is normal to the scattering plane in all the cases considered. Reflection symmetry requires that the polarization of the scattered beam $P_1 = (S_T + P_0)/(1 + P_0 S_T)$ is normal to the scattering plane as well (cf. Ref. 8, Chap. 3). S_T is the analyzing power of the auxiliary target. When the scattered beam hits the target of the Mott detector one finds the asymmetry

$$A_1 = P_1 S_{\text{eff}} = \frac{S_T + P_0}{1 + P_0 S_T} S_{\text{eff}}. \quad (5)$$

(iii) As shown in Fig. 1(iii), the previous step is repeated with the reversed polarization $-P_0$ yielding

$$A_1 = P_1 S_{\text{eff}} = \frac{S_T - P_0}{1 - P_0 S_T} S_{\text{eff}}. \quad (6)$$

For an unpolarized incident beam one has simply

$$A = S_T S_{\text{eff}}. \quad (7)$$

If, in cases (ii) and (iii), the intensities I_1 and I_1 of the beam scattered from the auxiliary target are monitored one can also evaluate the up-down asymmetry

$$A_T = \frac{I_1 - I_1}{I_1 + I_1} = P_0 S_T. \quad (8)$$

Measurement of the asymmetries (4)–(8) yields a redundant set of data for the determination of S_{eff} . In the present experiment the following relationships have been used to evaluate the effective analyzing power S_{eff} . (The subscript “eff” will be dropped from now on while $S_{(a)}$ to $S_{(d)}$ denote the effective analyzing powers calculated from the various relationships.)

Evaluation (a) using Eqs. (4), (5), and (8)

$$S_{(a)}^2 = \frac{A_0}{A_T} [A_1(1 + A_T) - A_0]; \quad (9)$$

evaluation (b) using Eqs. (4), (6), and (8)

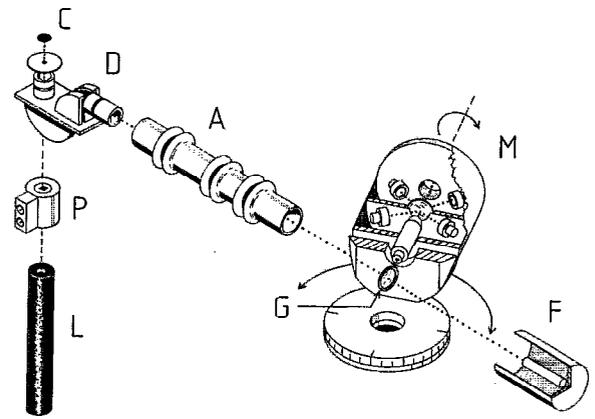


FIG. 2. Schematic view of the apparatus. (L) He-Ne laser, (P) Pockels cell, (C) GaAsP crystal, (D) monochromator/deflector, (A) accelerator, (G) gold foil, (M) Mott analyzer, (F) Faraday cup.

$$S_{(b)}^2 = \frac{A_0}{A_T} [A_1(1 - A_T) + A_0]; \quad (10)$$

evaluation (c) using Eqs. (5), (6), and (8)

$$S_{(c)}^2 = \frac{1}{4A_T} \{ [A_1(1 + A_T)]^2 - [A_1(1 - A_T)]^2 \}; \quad (11)$$

evaluation (d) using Eqs. (4), (7), and (8)

$$S_{(d)}^2 = \frac{A_0 A}{A_T}. \quad (12)$$

There are, of course, further possibilities of combining the measured asymmetries (4)–(8) in order to evaluate the analyzing power. Under the conditions of the present experiment, Eqs. (9)–(12) were the most suitable combinations from the viewpoint of minimizing the error propagation from the measured asymmetries to the final result.

III. APPARATUS

The experimental arrangement for the comparison of the double-scattering method with the auxiliary-target method is a modified version of an electron scattering apparatus which has been built for the precise measurement of the Sherman function of gold. A detailed description of this apparatus is given elsewhere,³ so that we report only on the most important features and recent changes.

The present arrangement is shown in Fig. 2. A beam of transversely polarized electrons is extracted from a standard-type photoemission source, using a GaAsP crystal as cathode which is irradiated with circularly polarized light from a 10 mW He-Ne laser. Typical values for the present source are an electron current of ~ 200 nA at the target and a polarization P_0 of $30\% \pm 4\%$, depending on the surface conditions of the cathode. Electron sources of this type were frequently described in the literature, see e.g., Refs. 9 and 10. A Pockels cell is used to switch the sign of the circular light polarization in order to reverse the electron polarization. For the double-scattering method a beam of unpolarized electrons is produced by irradiating

the cathode with linearly polarized light. This is achieved by adjusting the voltage of the Pockels cell to the appropriate value.

The beam emerging from the source passes through some transport optics and is then injected into the scattering chamber via a 120 keV accelerator tube. For ease of operation the source is on ground potential, whereas the scattering chamber and the electron detection circuits are kept at +120 keV. A gold foil serves as the auxiliary target. For the double scattering according to Eq. (3) this gold foil must be a duplicate of the analyzer foil and the scattering angle must be the same as in the Mott analyzer. The polarization analyzer to be calibrated is a Mott detector, containing a gold foil of $(210 \pm 3) \mu\text{g}/\text{cm}^2$ thickness as the target and monitor counters for the elimination of spurious asymmetries. The correction for instrumental asymmetries with the help of the monitor counters is carried out following the strategy described in Ref. 11. The scattering angle at the auxiliary target can be varied in the full range between 125° on the left side and 125° on the right side by rotating the Mott analyzer with the help of a stepper motor. A Faraday cup serves as a monitor for the primary beam current.

The apparatus is controlled by a VME-bus computer which also accumulates and processes the experimental data. The computer is connected to the high-voltage part of the apparatus by fiber optic cables.

IV. CALIBRATION PROCEDURE AND RESULTS

For a reliable comparison of different calibration methods one has to apply them to one and the same analyzer. Furthermore, care must be taken that the experimental conditions remain the same during all necessary measurements. Excessive time delay, caused, e.g., by the change of targets or even worse by breaking the vacuum, should be avoided between the measurements because otherwise the results may be affected by drift effects.

The experimental comparison between the double-scattering and the auxiliary-target method, on which we report in this paper, was performed by switching as quickly as possible between the asymmetry measurements required for the two methods until the desired statistical accuracy was reached. The polarizer for the double-scattering method served also as the auxiliary target for calibration according to Eqs. (9)–(12), and the scattering angle at this target remained fixed at 120° during the measurements of the asymmetries A , A_T , A_r , and A_l . Switching between the different asymmetry measurements was achieved by simply changing the voltage of the Pockels cell every two seconds so that spin-up electrons, spin-down electrons and—for the measurement of the asymmetry A —unpolarized electrons were alternately extracted from the source.

The production of unpolarized electrons with the source was more difficult than anticipated, because birefringence of the vacuum window, through which the laser beam entered the source, affected the light polarization. This led to a clearly recognizable offset in electron polarization, even when the circular polarization of the laser

light was adjusted to zero outside the vacuum. The correct setting was found by monitoring the electron polarization with the Mott detector while adjusting the Pockels cell.

Another problem was connected with the measurement of the asymmetry A_0 [see Fig. 1(i)]. For this measurement the intensity of the primary beam had to be reduced because otherwise the counters in the Mott detector would have been saturated. It turned out that the beam was intolerably depolarized down to 95% of its initial polarization when the intensity was reduced by defocusing in front of an aperture. We therefore chose a different way of reducing the intensity, taking advantage of the fact that, for a scattering angle of 45° , the polarization of the scattered beam $(S_T + P_0)/(1 + P_0 S_T)$ is practically identical with the polarization P_0 of the primary beam, since the Sherman function S_T of the gold target is practically zero at 45° (see Ref. 3). The asymmetry A_0 was therefore determined with the reduced intensity of the beam scattered through 45° at the auxiliary target, so that the count rates in the Mott detector did not exceed 3 kHz. The disappearance of the Sherman function at this angle was verified by scattering an unpolarized beam emerging from a thermal emission source and measuring the polarization of the electrons scattered through 45° with the Mott detector. No scattering asymmetry was observed within the statistical uncertainty of 10^{-3} . In order to eliminate errors introduced by a shift in the scattering angle the scattering was alternately performed in the left and the right 45° position of the Mott analyzer.

The whole calibration procedure was divided into 76 runs, each lasting ~ 1 h. Every run started with a measurement of A_0 before the Mott analyzer was turned into the 120° position for the measurement of the other asymmetries. The intensities I_r and I_l were obtained by summing up the counts of the two monitor counters in the Mott detector while measuring the asymmetries A_r and A_l . Before calculating the asymmetry A_T according to Eq. (8), the intensities were normalized to the primary beam current which was monitored with the help of the Faraday cup. This correction was necessary because of instrumental switching asymmetries, which sometimes reached values up to a few percent. Such asymmetries may, e.g., have been caused by a shift of the laser beam due to improper adjustment of the Pockels cell or birefringence of the vacuum window as discussed in Ref. 12. At the end of each run the A_0 measurement was repeated which always showed that there was no significant drift in polarization during a run. The mean value of the two A_0 values obtained at the beginning and at the end of such a run was therefore regarded as the relevant A_0 value for the whole run.

For each run the analyzing power of the Mott detector was evaluated from the five Eqs. (3) and (9)–(12). In order to check the reproducibility of the measurements the standard deviation of the results from the 76 runs was calculated separately for each of the five evaluations. It turned out that the standard deviation never exceeded the statistical uncertainty of the mean value. Nevertheless, the various methods of evaluating the analyzing power of the Mott detector turned out to not be equivalent, as can be

TABLE I. Results for the effective Sherman functions following from the different methods of calibration. The sign follows from theory. A gold foil of $(205 \pm 3) \mu\text{g}/\text{cm}^2$ thickness has been used as the auxiliary target or the polarizer, respectively. The subscript (dsc) denotes the value obtained by double scattering according to Eq. (3). The subscripts (a)–(d) are explained in Sec. II. The uncertainties due to counting statistics are given in parentheses.

$S_{(\text{dsc})}$	$S_{(a)}$	$S_{(b)}$	$S_{(c)}$	$S_{(d)}$
$-0.2681(7)$	$-0.2724(10)$	$-0.2625(8)$	$-0.2625(8)$	$-0.2668(9)$

seen from Table I. This is contrary to what had been anticipated.

As will be shown in the next section, the unexpected deviations can be explained by depolarization of the incident electron beam in the auxiliary target. Depolarization has the consequence that Eqs. (5) and (6) are not strictly valid. As a result, those calibrations where Eqs. (5) and (6) have been used yielding $S_{(a)}$, $S_{(b)}$, and $S_{(c)}$ are subject to a systematic error of a few percent. Since depolarization may be caused by multiple scattering, the amount of this error should depend on the thickness of the auxiliary target. In order to study this influence, the calibration procedure was repeated using gold foils of different thicknesses as auxiliary targets. The results of evaluations (a) and (b) from Eqs. (9) and (10) are shown in Fig. 3. It is obvious that the discrepancies increase with increasing foil thickness in accordance with what has been said about depolarization and multiple scattering. The evaluations (c) and (d) from Eqs. (11) and (12) yield no further information and will therefore not be further discussed.

V. THE INFLUENCE OF DEPOLARIZATION ON THE AUXILIARY-TARGET METHOD

Multiple scattering is usually taken into account by using effective values for the Sherman function rather than values calculated for scattering from a single atom. This does, however, not take into account that in the auxiliary-target method multiple scattering results in depolarization of the electron beam in the auxiliary target. This is clearly

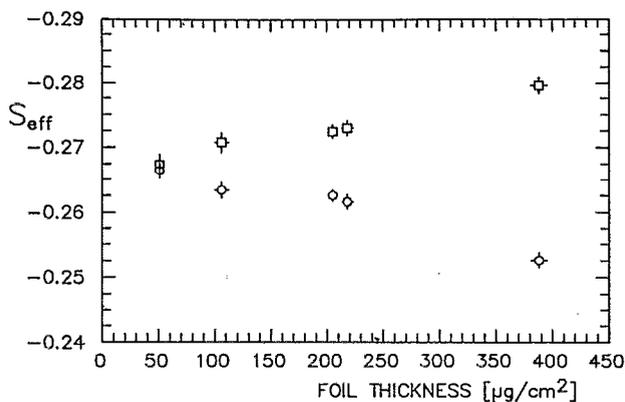


FIG. 3. Analyzing power of the Mott detector determined by different evaluations of the auxiliary-target method vs thickness of the gold foil used as the auxiliary target. Squares: $S_{(a)}$ evaluated according to Eq. (9); circles: $S_{(b)}$ evaluated according to Eq. (10).

seen by inserting $P_0=1$ into Eq. (5), which results in $P_1=1$, i.e., conservation of total polarization or absence of depolarization regardless of which value is inserted for the Sherman function S_T .

The depolarization can be visualized as follows. While in single scattering the electrons move in the plane defined by the incident beam and the axis from the target to the detector (we will call it the “macroscopic” scattering plane), this is no longer true when multiple scattering plays a role. The electrons may be scattered out of the macroscopic scattering plane and still reach the detector by subsequent scattering processes. The incident polarization vector, which in our experiment is normal to the macroscopic scattering plane, has components parallel to the “microscopic” scattering planes of the individual collisions leading to multiple scattering. This results in a change of the directions of the polarization vectors in the individual scattering events since only for polarization normal to the scattering plane the polarization vector retains its direction during scattering. Quantitatively the change of direction is described by the parameters S , T , and U .⁸ The polarization vector of the beam that leaves the auxiliary target is the average of the polarization vectors of all the partial beams that have undergone various multiple scattering processes. Since these individual polarization vectors have now slightly different directions in space the resulting polarization is smaller than the polarization one would obtain from single scattering. The resulting polarization vector is, however, still normal to the macroscopic scattering plane, because the individual in-plane components compensate each other owing to the reflection symmetry of the experiment with respect to the macroscopic scattering plane. For a more thorough treatment we refer to Rose and Bethe¹³ who showed that multiple elastic scattering may cause significant depolarization whereas the influence of inelastic and exchange scattering is negligible. A comprehensive theory of depolarization by multiple scattering is given by Mühschlegel and Koppe.¹⁴

These consequences of multiple scattering can be described by introducing the spin-flip cross sections σ_{-+} for incident spin-up electrons (polarization parallel to the normal \hat{n} of the scattering plane) and σ_{+-} for incoming spin-down electrons. For nonflip scattering of spin-up electrons we use σ_{++} and for spin-down electrons σ_{--} . The analyzing power S_T of the auxiliary target is then

$$S_T = \frac{\sigma_{++} + \sigma_{-+} - \sigma_{--} - \sigma_{+-}}{\sigma_{++} + \sigma_{-+} + \sigma_{--} + \sigma_{+-}} \quad (13)$$

because the scattering cross section for spin-up electrons is proportional to $\sigma_{++} + \sigma_{-+}$ while for spin-down electrons it is proportional to $\sigma_{--} + \sigma_{+-}$. For the polarizing power P one has

$$P = \frac{\sigma_{++} + \sigma_{-+} - \sigma_{--} - \sigma_{+-}}{\sigma_{++} + \sigma_{-+} + \sigma_{--} + \sigma_{+-}} \quad (14)$$

because the number of spin-up electrons in the scattered beam is proportional to $\sigma_{++} + \sigma_{-+}$ and the number of spin-down electrons is proportional to $\sigma_{--} + \sigma_{+-}$. The

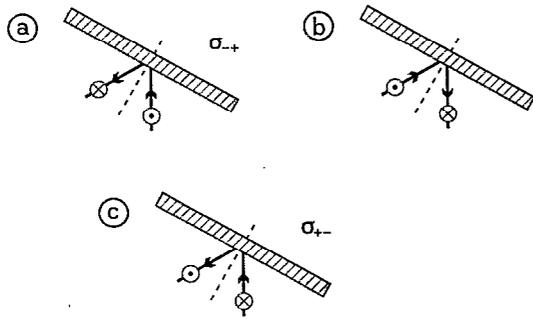


FIG. 4. Symmetry operations showing the equality of the spin-flip cross sections σ_{+-} and σ_{-+} for specular scattering from the auxiliary target. (a) is transformed into (b) by time reversal, (b) into (c) by 180° rotation around the dashed line.

equality of P and S_T which—according to Eqs. (3), (5), and (6)—is required for the calibration methods studied, is only fulfilled if the two spin-flip cross sections are equal. In the case of specular elastic scattering σ_{+-} can be transformed into σ_{-+} by time reversal and rotation by 180° around the surface normal of the target foil, as shown in Fig. 4. Since the scattering cross sections are invariant under these symmetry operations, σ_{+-} must equal σ_{-+} and the equality of S_T and P is fulfilled. In our experiment the geometry was not specular since the incoming beam was perpendicular to the foil. Nevertheless, our present experimental data are, within the error limits, in agreement with the assumption $S_T = P$ also in that case. This will be shown at the end of the next section. In the following we will no longer distinguish between P and S_T .

The depolarization effect becomes obvious when one calculates the polarization of the scattered beam in the case of non-zero initial polarization P_0 . Taking into account that the number of spin-up electrons in the incoming beam is proportional to $(1+P_0)/2$ whereas the number of spin-down projectiles is proportional to $(1-P_0)/2$, one obtains from Eq. (14) for primary polarization parallel to \hat{n}

$$P_1 = \frac{\frac{1+P_0}{2} \sigma_{++} + \frac{1-P_0}{2} \sigma_{+-} - \frac{1+P_0}{2} \sigma_{-+} - \frac{1-P_0}{2} \sigma_{--}}{\frac{1+P_0}{2} \sigma_{++} + \frac{1-P_0}{2} \sigma_{+-} + \frac{1+P_0}{2} \sigma_{-+} + \frac{1-P_0}{2} \sigma_{--}}. \quad (15)$$

Straightforward calculation using Eq. (13) yields

$$P_1 = \frac{A_1}{S_{\text{eff}}} = \frac{S_T + \alpha P_0}{1 + P_0 S_T}, \quad (16)$$

where

$$\alpha = 1 - 2 \frac{\sigma_{+-} + \sigma_{-+}}{\sigma_{++} + \sigma_{+-} + \sigma_{-+} + \sigma_{--}}. \quad (17)$$

For primary polarization reversed one obtains

$$P_1 = \frac{A_1}{S_{\text{eff}}} = \frac{S_T - \alpha P_0}{1 - P_0 S_T}. \quad (18)$$

These expressions differ from Eqs. (5) and (6) by the depolarization factor α which is mainly determined by the

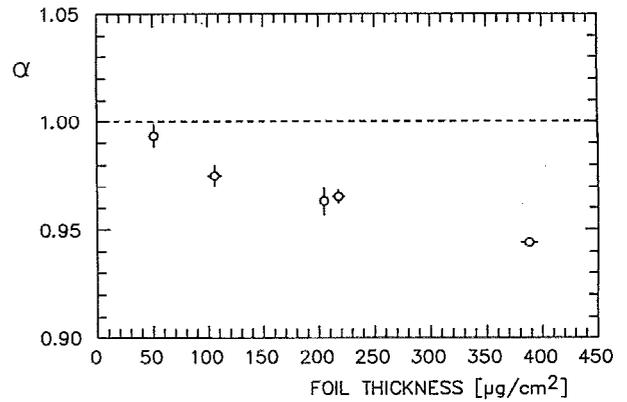


FIG. 5. Depolarization factor α vs thickness of the gold foil used as the auxiliary target.

spin-flip cross sections σ_{+-} and σ_{-+} . Since the depolarization is caused by multiple scattering in the auxiliary target, α should depend on the thickness of the target foil. This can be checked experimentally since one can find a simple relationship between α and the measured asymmetries Eqs. (4)–(8). By subtracting Eqs. (16) from (18) and using Eqs. (4) and (8) one finds

$$\alpha = \frac{1}{2A_0} [A_1(1+A_T) - A_1(1-A_T)]. \quad (19)$$

Figure 5 shows values of the depolarization factor α for target foils of different thicknesses. As expected, the influence of depolarization increases with increasing foil thickness. For the thickest gold foil considered α drops below 0.95. This leads to an error of at least $\pm 5\%$ in analyzer calibration when this foil is used as an auxiliary target for the calibration procedure according to Hopster and Abraham.

VI. CORRECT CALIBRATION OF THE MOTT ANALYZER

At this point it is obvious that the double-scattering method has the advantage, compared to the auxiliary-target method, that the use of an unpolarized primary beam does not give rise to the depolarization problem. On the other hand, the auxiliary-target method has some experimental advantages, such as the fact that the parameters of the first and second scattering process can be chosen differently. Fortunately, the depolarization problem inherent in this method can be easily solved, once the problem has been recognized. It is possible to modify the evaluation in such a way that the depolarization factor α is eliminated.

By adding Eqs. (16) and (18) and using again Eqs. (4) and (8) one obtains the correct formula for the auxiliary-target method

$$S_{\text{eff}}^2 = \frac{A_0}{A_T} [A_1(1+A_T) + A_1(1-A_T)]. \quad (20)$$

This is nothing but the mean value of expressions (9) and (10):

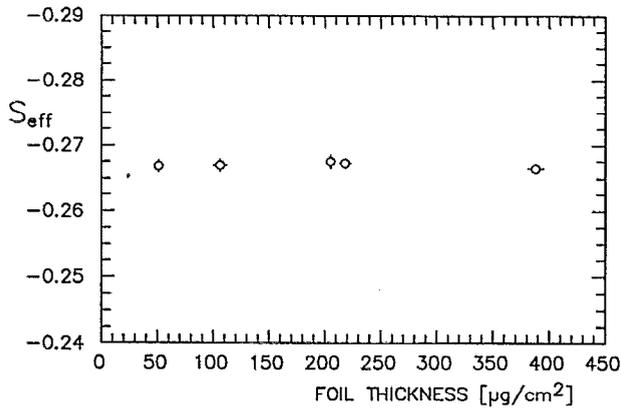


FIG. 6. S_{eff} vs thickness of the auxiliary-target foil. The values were calculated from those shown in Fig. 3 using Eq. (21).

$$S_{\text{eff}}^2 = \frac{S_{(a)}^2 + S_{(b)}^2}{2}. \quad (21)$$

The price one has to pay for the elimination of the depolarization factor is that one needs four instead of three different asymmetry measurements for a correct evaluation of the auxiliary-target method.

In Fig. 6 we have plotted S_{eff} versus the thickness of the auxiliary-target foil. The values were calculated from those shown in Fig. 3 using Eq. (21). It can be seen that these values do not depend on the auxiliary-target thickness. They agree within the statistical uncertainty of 0.4% with the value obtained from the double-scattering experiment and with $S_{(a)}$ obtained from Eq. (12) (cf. Table I).

Figure 6 may also be regarded as a proof for the equality of analyzing and polarizing power, which is required for the calibration methods applied. For the thinnest gold foil used in the present investigation the depolarization, which is proportional to $\sigma_{+-} + \sigma_{-+}$, is almost below the detection limit, as shown in Fig. 5. Consequently, the difference between S_T and P , which is proportional to $\sigma_{+-} - \sigma_{-+}$ and therefore clearly smaller, is not detectable for the thinnest foil. According to Fig. 6 the calibration does not depend on the thickness of the auxiliary gold foil even in the region of thicknesses where the depolarization is significant. One has therefore no reason to assume that the equality of P and S_T is violated to a measurable extent for any of the gold foils used in the present experiment, because otherwise the values for S_{eff} should be affected as the target

thickness increases. This possible error source can therefore be excluded.

VII. DISCUSSION

The auxiliary-target method suggested by Hopster and Abraham is an expedient way of calibrating a Mott polarimeter. It enables one to determine the analyzing power of the polarimeter and the polarization of the incident electron beam by performing three asymmetry measurements. Unfortunately, the accuracy of the method is limited by a systematic error caused by depolarization of the electron beam in the auxiliary target. In our experiment it results in an error of the calibration of a few percent depending on the thickness of the auxiliary-target foil. This systematic error can, however, be avoided by an appropriate evaluation procedure if an additional asymmetry measurement is made. This means that four asymmetry measurements are required for proper calibration of the polarimeter. When this is done, the accuracy of the auxiliary-target method is comparable to the accuracy of the classical double-scattering experiment in its improved version. From the experimental data one can also conclude that the equality of polarizing and analyzing power which is assumed to be valid in the calibration methods discussed is fulfilled within the error limits of our experiment.

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