

# GEANT4 Simulation of the Jlab MeV Mott Polarimeter

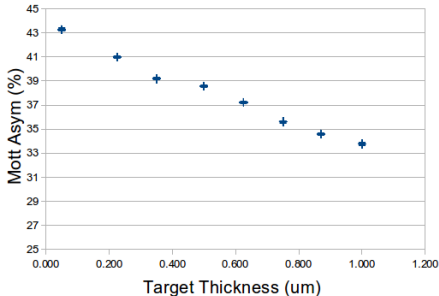
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# The Problem

We don't know the form of the effective Sherman function for targets of finite thickness,  $S(d)$ .

Asymmetry vs. Target Thickness  
Data From Dan's June Presentation



# How Can Simulation Help Us?

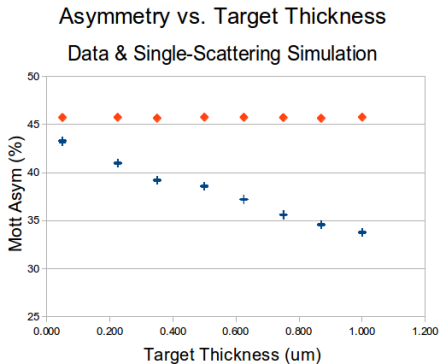
- Allows us to examine contributions to detector signal individually.
- Beam is treated as 100% polarized in  $y$  direction.
- Gaussian, circular beam profile with width of 1 mm.

## Why Brute Force doesn't

**work:**  $1 \mu\text{A}$  is  $6.24 \times 10^{12} e^- / \text{s}$   
and we need  $\approx 1000 \mu\text{As}$  of data  
for a decent measurement. Can  
only simulate 100 million events  
per day...

# How to Generate Single-Scattering Events

- 1 Pick point  $\vec{x}_1$  in the beam profile on the target.
- 2 Calculate energy loss to  $\vec{x}_1$ .  
Get new energy  $E_1$ .
- 3 Pick point  $\vec{x}_2$  in acceptance to throw at.
- 4 Calculate  $\sigma(\theta_1, \phi_1, E_1)$  based on  $\vec{x}_1, \vec{x}_2$ .
- 5 Throw random number,  $x$ .  
If  $x < \sigma$  throw electron.  
Else, repeat from 1.



# How to Generate Double-Scattering Events

- 1 Pick point  $\vec{x}_1$  in the beam profile on the target.
- 2 Calculate energy loss to  $\vec{x}_1$ . Get new energy  $E_1$ .
- 3 Pick point  $\vec{x}_2$  in target with  $|\vec{x}_2 - \vec{x}_1| < r_E$ .
- 4 Calculate  $\sigma_1(\theta_1, \phi_1, E_1)$  based on  $\vec{x}_1, \vec{x}_2$ .
- 5 Calculate energy loss to  $\vec{x}_2$ . Get new energy  $E_2$ .
- 6 Pick point,  $\vec{x}_3$ , in acceptance to throw at.
- 7 Calculate  $\sigma_2(\theta_2, \phi_1, E_2)$ .
- 8 Throw random number,  $x$ . If  $x < \sigma_1\sigma_2$  throw electron. Else, repeat from 1.

# Double Scattering Asymmetry

The Asymmetry is calculated to be:

$$A_{d.s.} = \frac{L - R}{L + R} = -01.05\% \pm 0.06\%$$

for all target thicknesses. The problem now becomes one of determining how much of a dilution this is at each target thickness.

# Calculating Rates

In order to compare both types of simulation and to compare simulation to data, we must be able to calculate rates. The rate is given as

$$\mathcal{R} = \mathcal{L} \int_x \sigma(x) \epsilon(x)$$

where  $\epsilon$  is the effective acceptance of the detectors and  $x$  are the degrees of freedom over which the integral is performed.

# Calculating Rates (Single Scattering)

In the case of single scattering the integral can be simplified to:

$$\mathcal{R} \approx \mathcal{L} \langle \sigma \rangle \frac{N_{hit}}{N_{thrown}} \Delta \cos \theta \Delta \phi$$

$$\mathcal{R}(0.05 \mu m) = 33 [\text{Hz}/\mu\text{A}]$$

$$\mathcal{R}(1.0 \mu m) = 690 [\text{Hz}/\mu\text{A}]$$

This is a good sanity check because it scales with thickness (since  $\mathcal{L} \propto d$ ) and roughly matches with data (2014-01-08 Meeting).



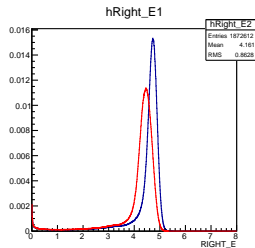
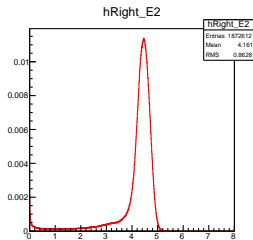
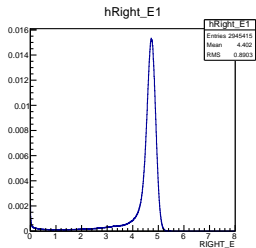
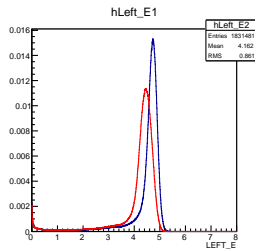
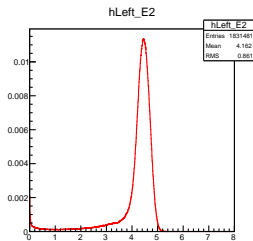
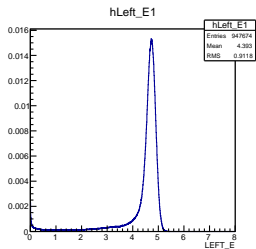
# Calculating Rates (Double Scattering)

- Attempting the same simplification doesn't work in the double scattering case. Rates are  $\approx 10^{-12}$  smaller than the single scattering case.
- More thought needs to go into performing this integral in order to make the simulation work.
- Once this works, we should be able to calculate

$$A(d) = \frac{[\mathcal{R}_{L_1}(d) - \mathcal{R}_{R_1}(d)] + [\mathcal{R}_{L_2}(d) - \mathcal{R}_{R_2}(d)]}{[\mathcal{R}_{L_1}(d) + \mathcal{R}_{R_1}(d)] + [\mathcal{R}_{L_2}(d) + \mathcal{R}_{R_2}(d)]}$$

directly from simulation.

# Spectra



# Summary

- Single scattering simulation gives good results but no  $d$ -dependence in Asymmetry.
- Can't calculate rate yet for Double-scattering. Asymmetry is small. Need to determine proper dilution.
- Spectra look decent, can't tell how much but it looks like the double scattering will influence the low energy shoulder to some degree.

# Energy Loss in the Gold Foils

Using the table at right, we determine the linear fit

$$\frac{dE}{dx}(E) = \frac{0.272}{\text{mm}} \times E + 1.888 \frac{\text{MeV}}{\text{mm}}.$$

Numerical integration of the above gives us energy loss within the target. Note: A particle with initial energy of 5 MeV will only lose 3 keV/ $\mu\text{m}$  and will lose 500 keV in  $\approx 200\mu\text{m}$ .

Energy [MeV]	dE/dx [MeV/mm]
1.0	2.179
2.0	2.422
3.0	2.702
4.0	2.980
5.0	3.254
6.0	3.526
7.0	3.796
8.0	4.065

Data from NIST estar database.

# What Steigerwald Did

His method of calculating multiple scattering's influence was direct integration of some form:

$$N = \int_{\theta=0}^{\pi} \int_{\phi=0}^{2\pi} \int_{x_1=0}^D \int_{\psi=\theta_2}^{\theta_2+\Omega_\theta} \sigma_1(x_1, \theta, \phi) \sigma_2(x_2, \theta_2) E(x_1, x_2) d\psi dl d\phi d\theta.$$

The problem is that his source for this integral is in German and his code is poorly documented and also in partial German.