

Measurement of  $^{16}\text{O}(\gamma, \alpha)^{12}\text{C}$  with a Bubble Chamber  
and a Bremsstrahlung Beam at Jefferson Lab Injector

Riad Suleiman  
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B. DiGiovine  
D. Henderson  
R. J. Holt  
K. E. Rehm



A. Robinson  
C. Ugalde



A. Sonnenschein

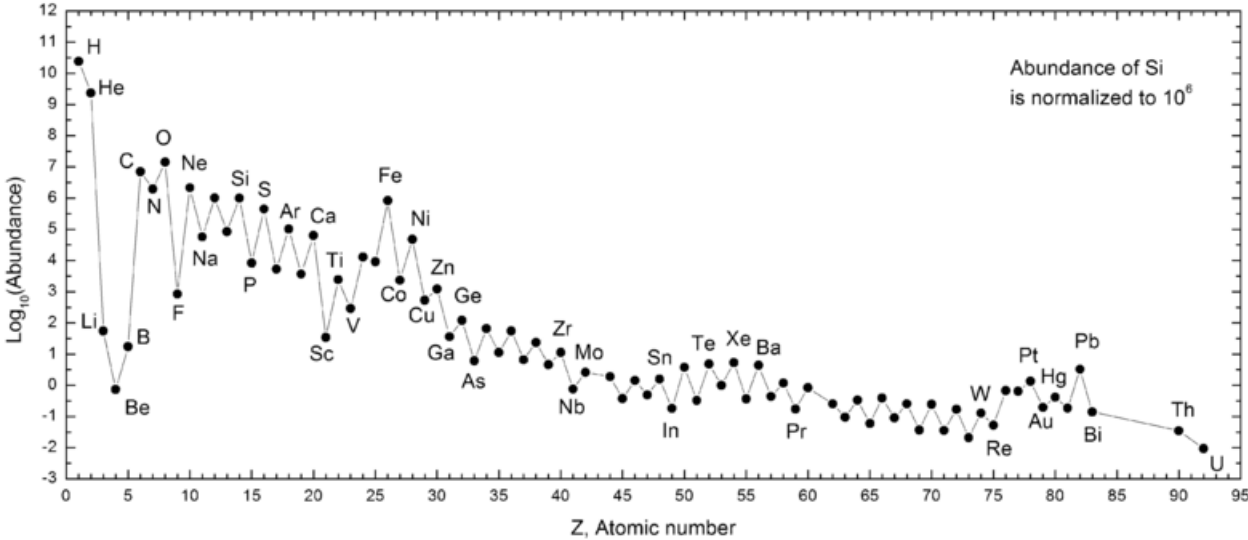
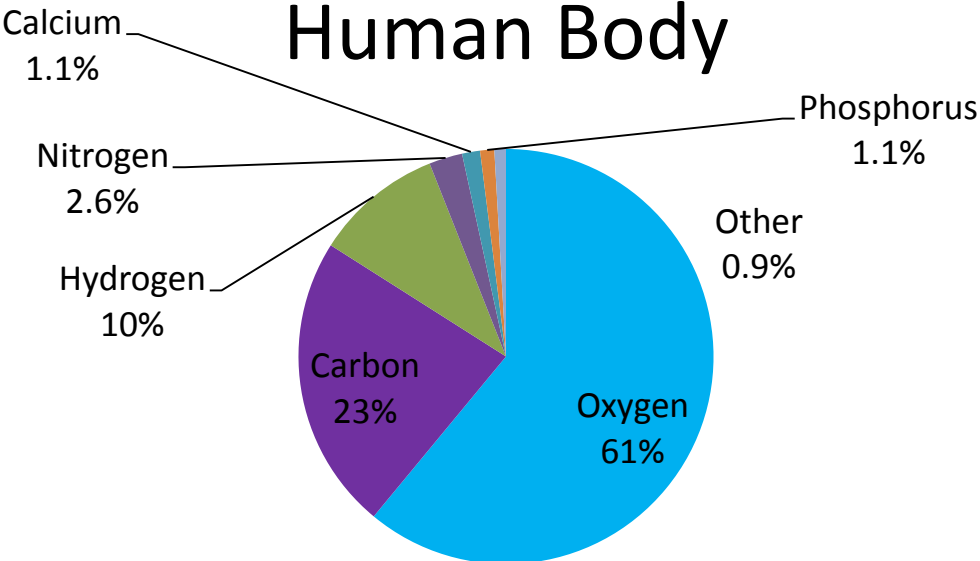
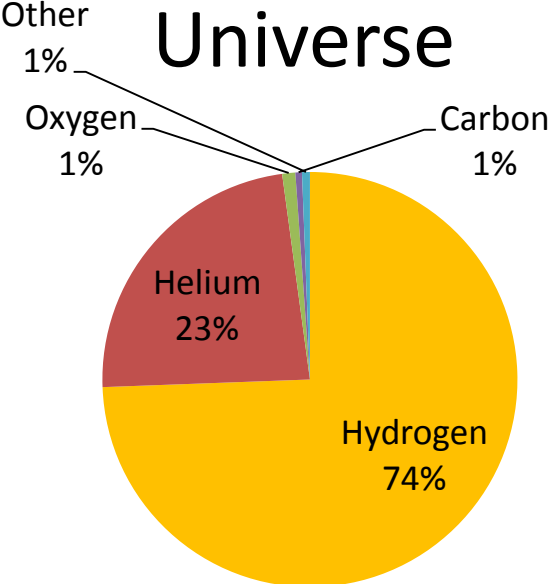


J. Benesch  
P. Degtiarenko  
A. Freyberger  
J. Grames  
C. Tennant  
G. Kharashvili  
D. Meekins  
M. Poelker  
Y. Roblin  
R. Suleiman  
V. Vylet

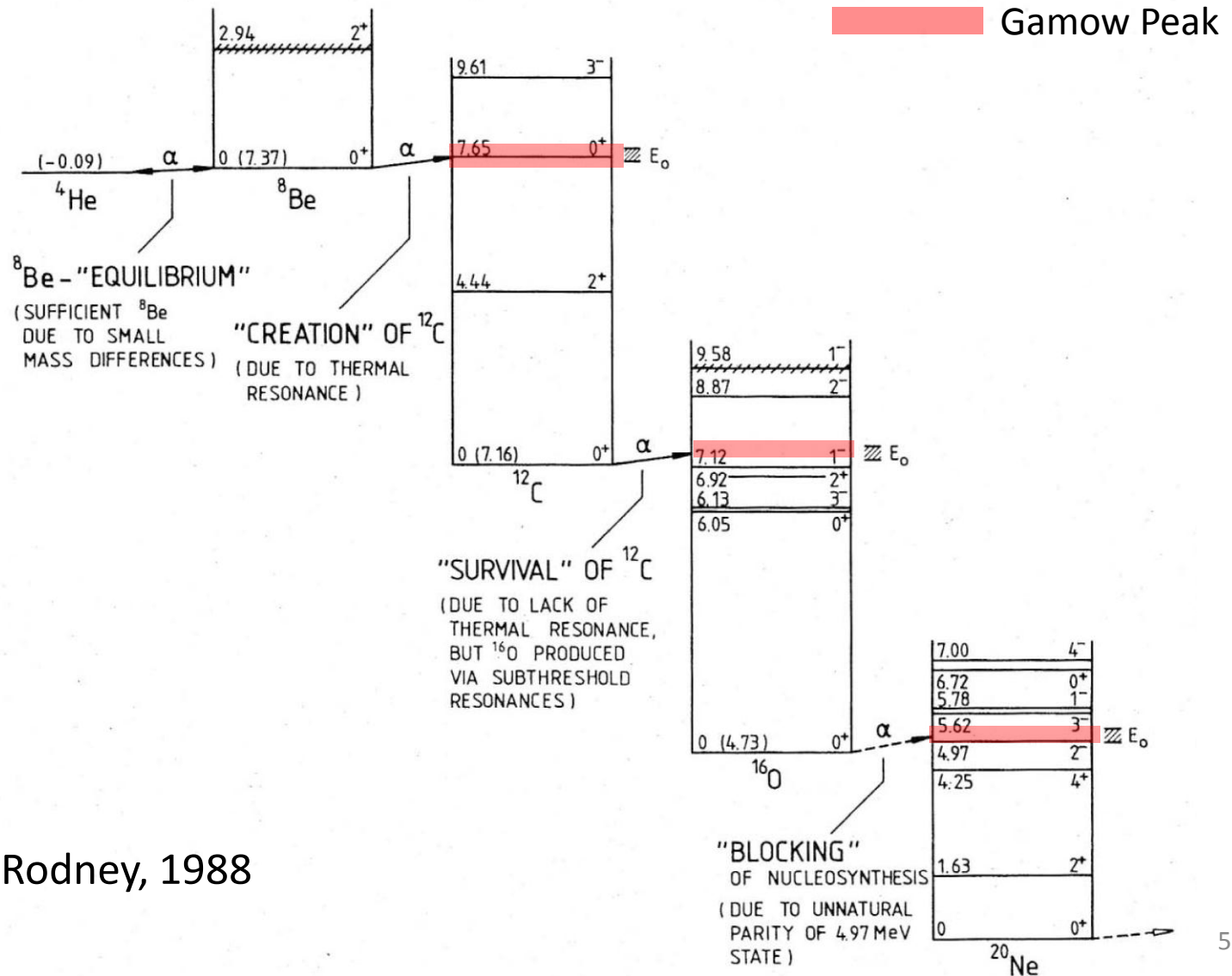
# OUTLINE

- Nucleosynthesis and the  $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$  Reaction
- Time-reversal Reaction:  $^{16}\text{O}(\gamma,\alpha)^{12}\text{C}$
- Bubble Chamber Theory and Design
- Work at HIGS
- Experimental Setup at Jefferson Lab Injector
- Bremsstrahlung Beam and Penfold-Leiss Unfolding
- Statistical and Systematic Errors
- Backgrounds and Ion Energy Distributions
- Safety
- Summary and Outlook

# RELATIVE ABUNDANCE OF ELEMENTS BY WEIGHT



# STELLAR HELIUM BURNING



Rolfs and Rodney, 1988

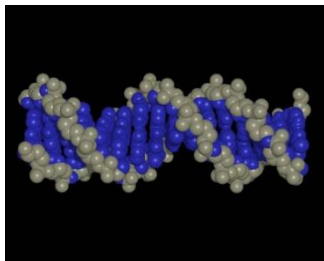
# THE $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$ Reaction

- The “holy grail” of nuclear astrophysics

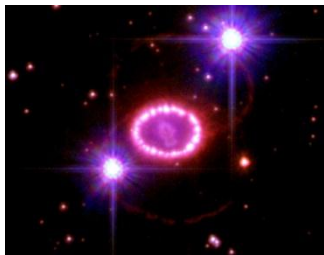
Periodic Table of the Elements

The image shows a standard periodic table of elements, with the title 'Periodic Table of the Elements' at the top. The elements are arranged in rows and columns, with their chemical symbols and atomic numbers. The table is color-coded by groups.

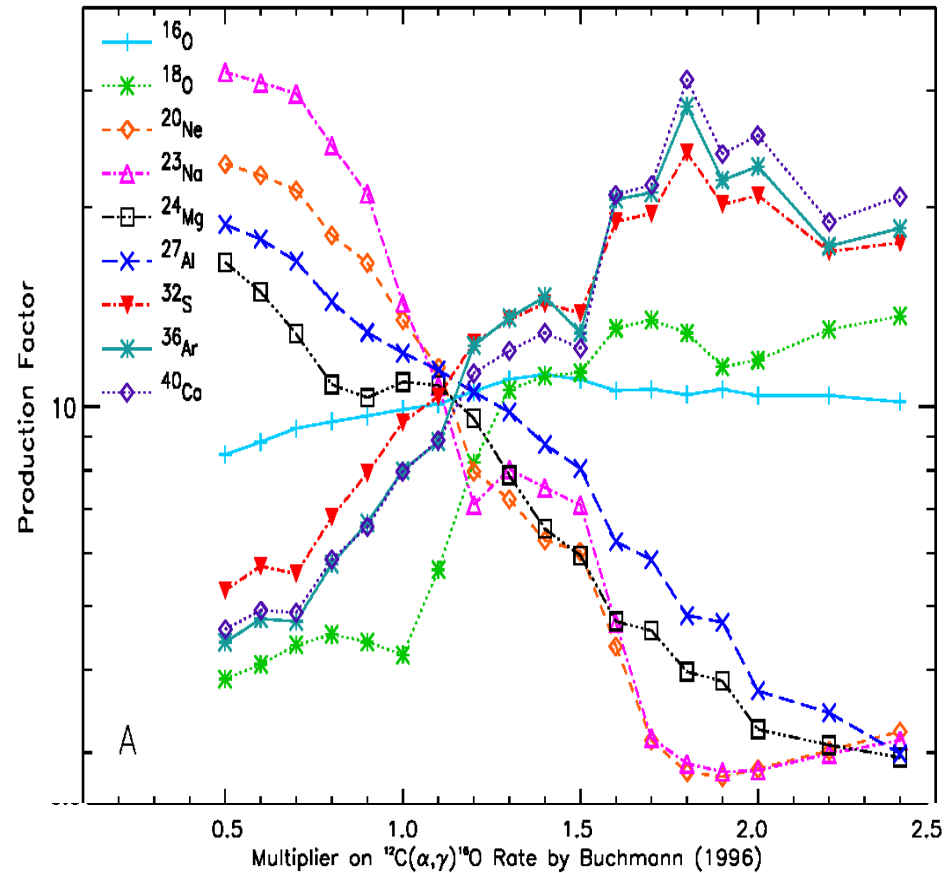
Affects the synthesis of most of the elements of the periodic table



Sets the C to O ratio in the universe



Determines the minimum mass a star requires to become a supernova



# STELLAR CARBON BURNING

- Helium burning stage of stellar evolution occurs at  $T=0.2 \cdot 10^9$  K
- Most effective stellar energy,  $E_{\text{CM}} = 300$  keV
- He burning at cross section  $\sigma \sim 10^{-17}$  barn
- Thermonuclear reaction rate involving two nuclei is:

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi m (kT)^3}} \int_0^{\infty} E \sigma(E) e^{-\frac{E}{kT}} dE$$

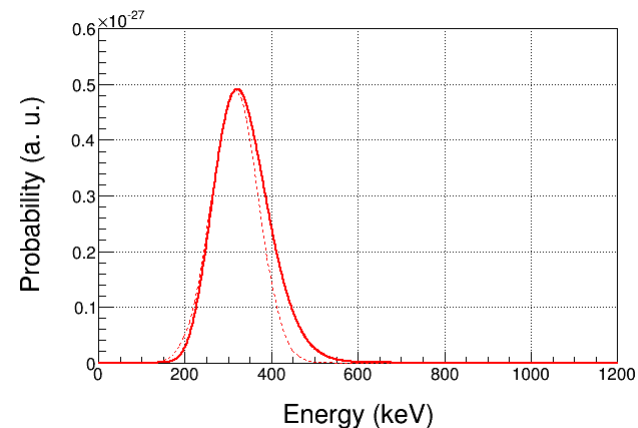
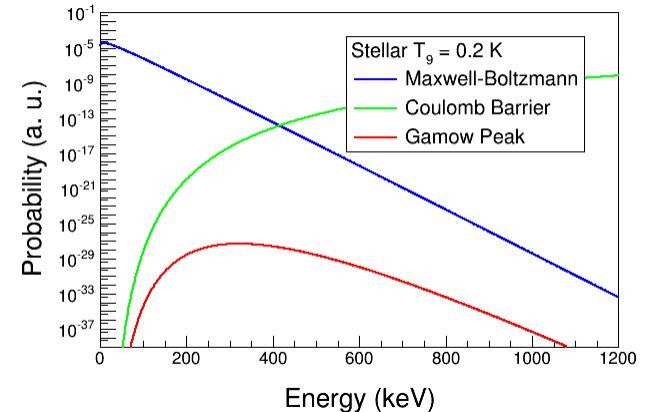
# THE GAMOW PEAK

- Narrow energy range where thermonuclear reactions is most likely to occur in stellar plasma is a product of two distributions:
  - Maxwell-Boltzmann energy distribution with  $e^{-E/kT}$
  - Penetration through Coulomb barrier with  $e^{-b/E^{1/2}}$

$$E_0 = 1.220 \left( Z_1^2 Z_2^2 A T_6^2 \right)^{1/3} \text{ keV}$$

$$W = 0.2368 \left( Z_1^2 Z_2^2 A T_6^5 \right)^{1/6} \text{ keV}$$

- For  $\alpha + {}^{12}\text{C}$  ( $Z_1=2, Z_2=6, A=3$ ), and stellar  $T=0.2 \cdot 10^9$  K:
  - Gamow Peak,  $E_0 = 315$  keV,  $W = 54$  keV
  - Maximum of Maxwell-Boltzmann energy distribution,  $kT = 17$  keV





# Heroic efforts in search of the holy grail of astrophysics: $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$

## ➤ Previous Experiments:

### A. Direct Techniques:

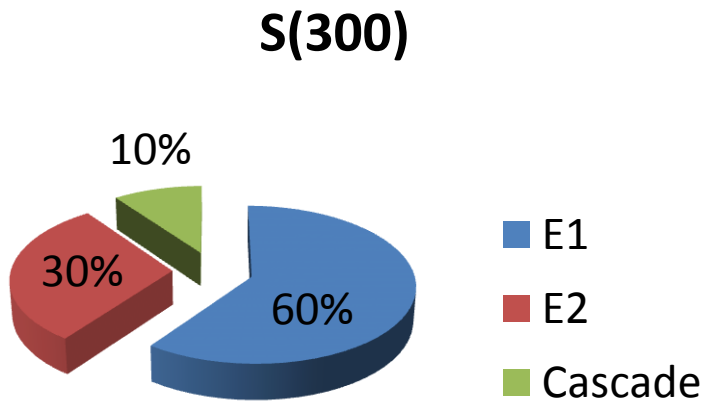
- I. Helium ions on carbon target:  $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$
- II. Carbon ions on helium gas:  $^4\text{He}(^{12}\text{C},^{16}\text{O})\gamma$

Experiment	Beam Current (mA)	Detector Efficiency	Target (nuclei/cm <sup>2</sup> )	Time (h)
Redder	0.7	Ge, 35%	$^{12}\text{C}$ , $3 \cdot 10^{18}$	900
Ouellet	0.03	Ge, 30%	$^{12}\text{C}$ , $5 \cdot 10^{18}$	1950
Roters	0.02	BGO, 270%	$^4\text{He}$ , $1 \cdot 10^{19}$	5000
Kunz	0.45	Ge, 100%	$^{12}\text{C}$ , $3 \cdot 10^{18}$	700
EUROGAM	0.34	Ge, 70%	$1\text{E}19$	2100

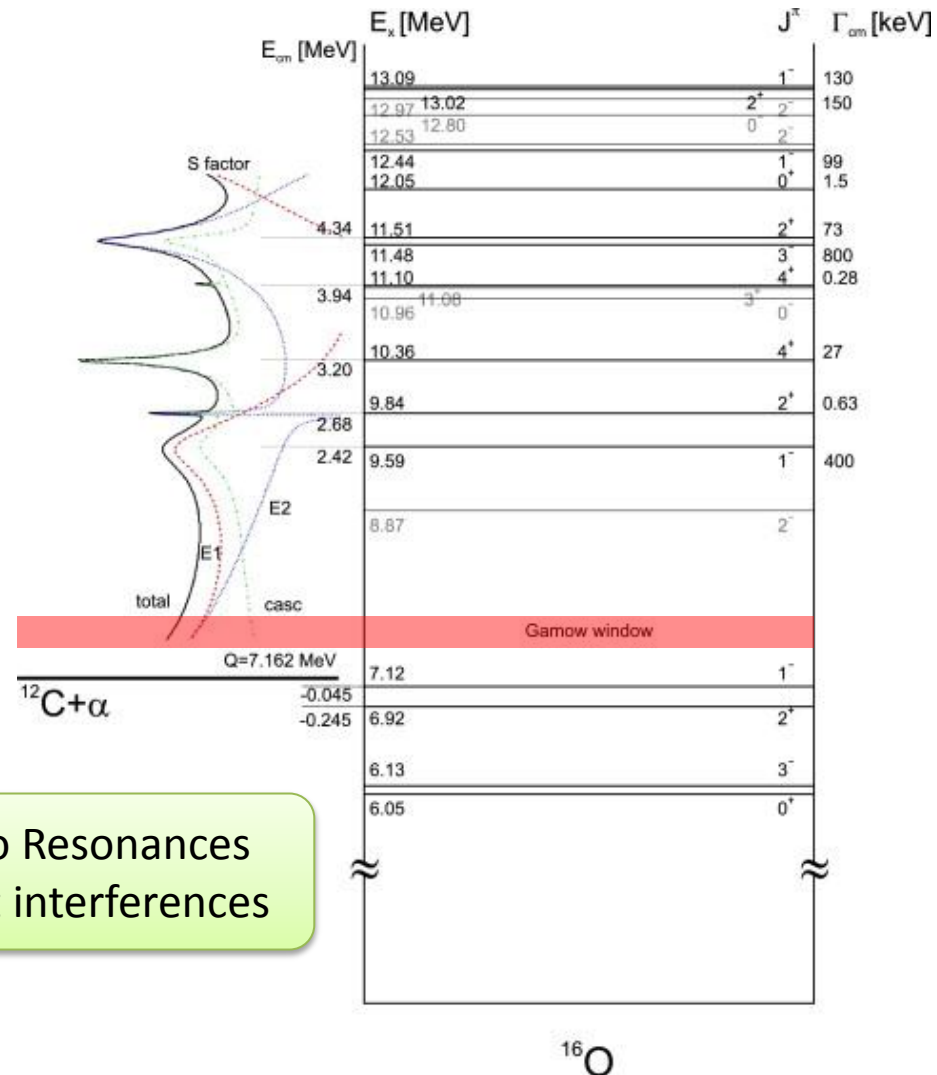
### B. Indirect Methods:

- I.  $\beta$ -delayed  $\alpha$  decay of  $^{16}\text{N}$  ( $J^\pi=2^-$ ,  $T_{1/2}=7.13$  sec, BR=0.12%).  $\text{N} \rightarrow \beta^- + \alpha + ^{12}\text{C}$
- II. Elastic  $\alpha - ^{12}\text{C}$  Scattering

# ENERGY LEVEL-DIAGRAM OF $^{16}\text{O}$



$S_{E1}(300)$	$70 \pm 20$
$S_{E2}(300)$	$70 \pm 20$
$S_{casc}(300)$	$70 \pm 20$

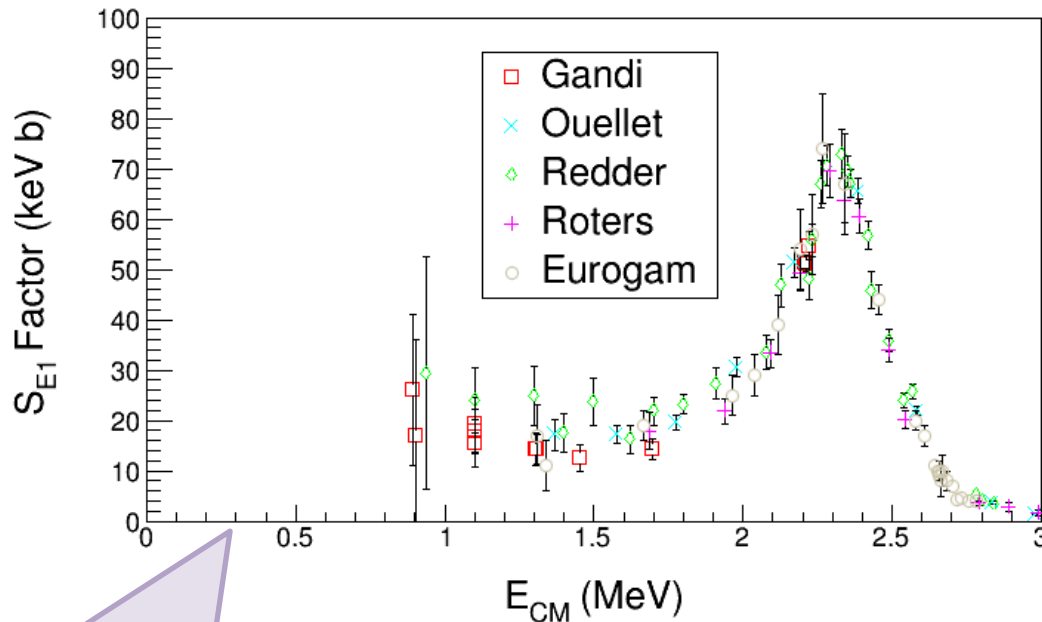


# ASTROPHYSICAL S-FACTOR $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$

- Define S-Factor to remove both  $1/E$  dependence of nuclear cross sections and Coulomb barrier transmission probability:

$$S \equiv E_{CM} \sigma(\alpha, \gamma) e^{2\pi\eta}$$

$$\eta = \frac{1}{137} Z_{\alpha} Z_{^{12}\text{C}} \sqrt{\frac{m_{^{12}\text{C}\alpha}}{2E_{CM}}}$$



Extrapolate to Stellar helium burning at  $E = 300$  keV

Author	$S(300 \text{ keV})$ (keV b)
Buchmann (2005)	102–198
Caughlan and Fowler (1988)	120–220
Hammer (2005)	$162 \pm 39$

# $(\gamma, \alpha)$ and $(\alpha, \gamma)$ – Reciprocity Relation

- $A(\alpha, \gamma)B$ :

$$\sigma_{B\gamma}^{j \rightarrow i}(E_\gamma) = \frac{(2J_i + 1)(2J_\alpha + 1)}{2J_j + 1} \frac{m_{A\alpha} c^2 E_{A\alpha}}{E_\gamma^2} \sigma_{A\alpha}^{i \rightarrow j}(E_{A\alpha})$$

$$m_{A\alpha} c^2 = \frac{M(^{12}\text{C}) \cdot M(\alpha)}{M(^{12}\text{C}) + M(\alpha)} = 2796 \text{ MeV}$$

$$J_i = 0, J_j = 0, J_\alpha = 0 \quad E_{A\alpha} = E_{CM} = \frac{M(^{12}\text{C})}{M(^{12}\text{C}) + M(\alpha)} E_\alpha$$

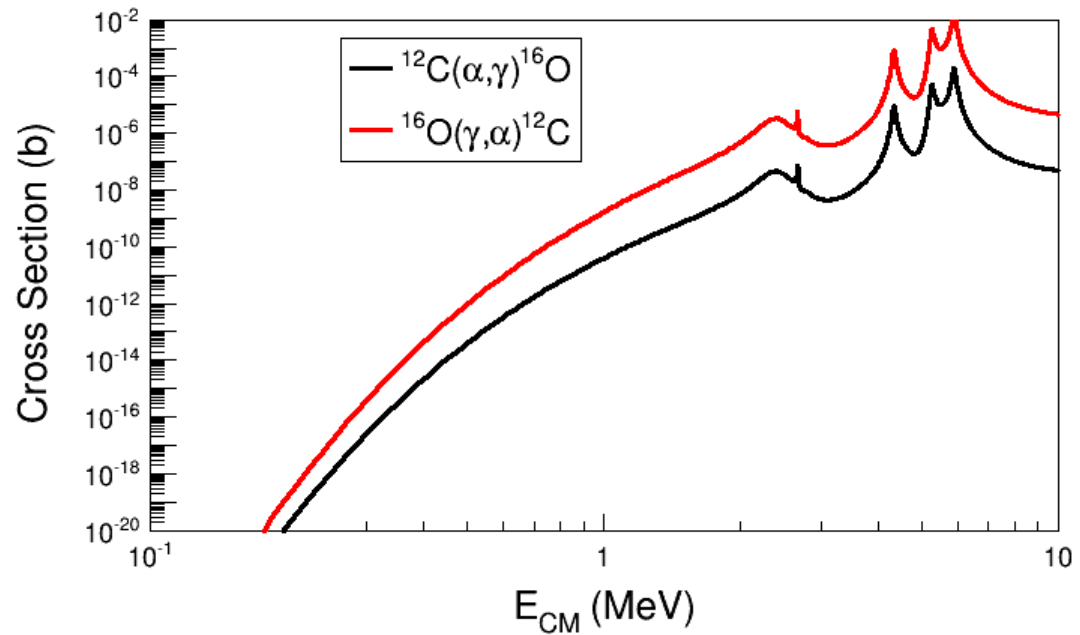
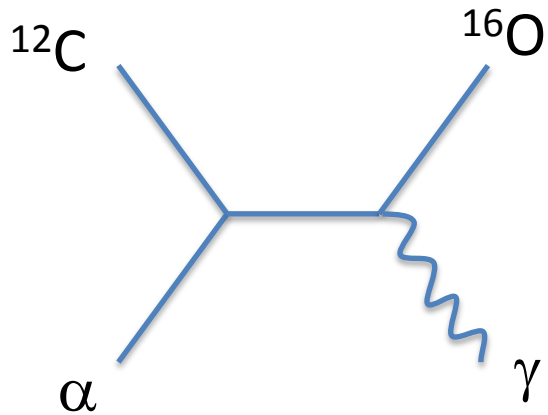
$$E_{CM} = \sqrt{m_B^2 + 2E_\gamma m_B} - m_B - Q$$

$$Q = m_A + m_\alpha - m_B = 7.162 \text{ MeV}$$

$$\sigma_{(\gamma, \alpha)}(E_\gamma) = \frac{m_{A\alpha} c^2 E_{CM}}{E_\gamma^2} \sigma_{(\alpha, \gamma)}(E_{CM})$$

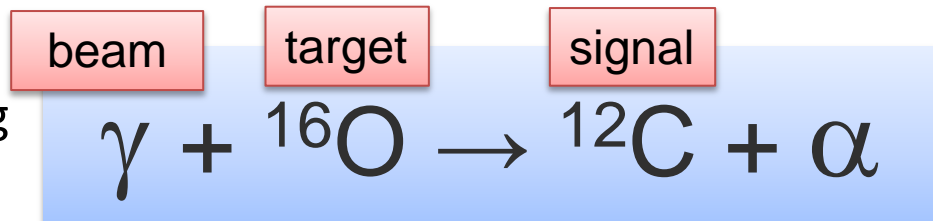
- $\sigma(\gamma, \alpha)$  is over two orders of magnitude larger than  $\sigma(\alpha, \gamma)$

# TIME REVERSAL REACTION



# NEW APPROACH: REVERSAL REACTION + BUBBLE CHAMBER

- Extra gain (factor of 100) by measuring time reversal reaction
- Target density up to  $10^4$  higher than conventional targets. Number of  $^{16}\text{O}$  nuclei =  $3.5 \cdot 10^{22} / \text{cm}^2$
- Solid Angle and Detector Efficiency = 100%
- Superheated liquid will nucleate from  $\alpha$  and  $^{12}\text{C}$  recoils
- Electromagnetic debris (electrons and gammas, or positrons) do NOT trigger nucleation (detector is insensitive to  $\gamma$ -rays by at least 1 part in  $10^{11}$ ).

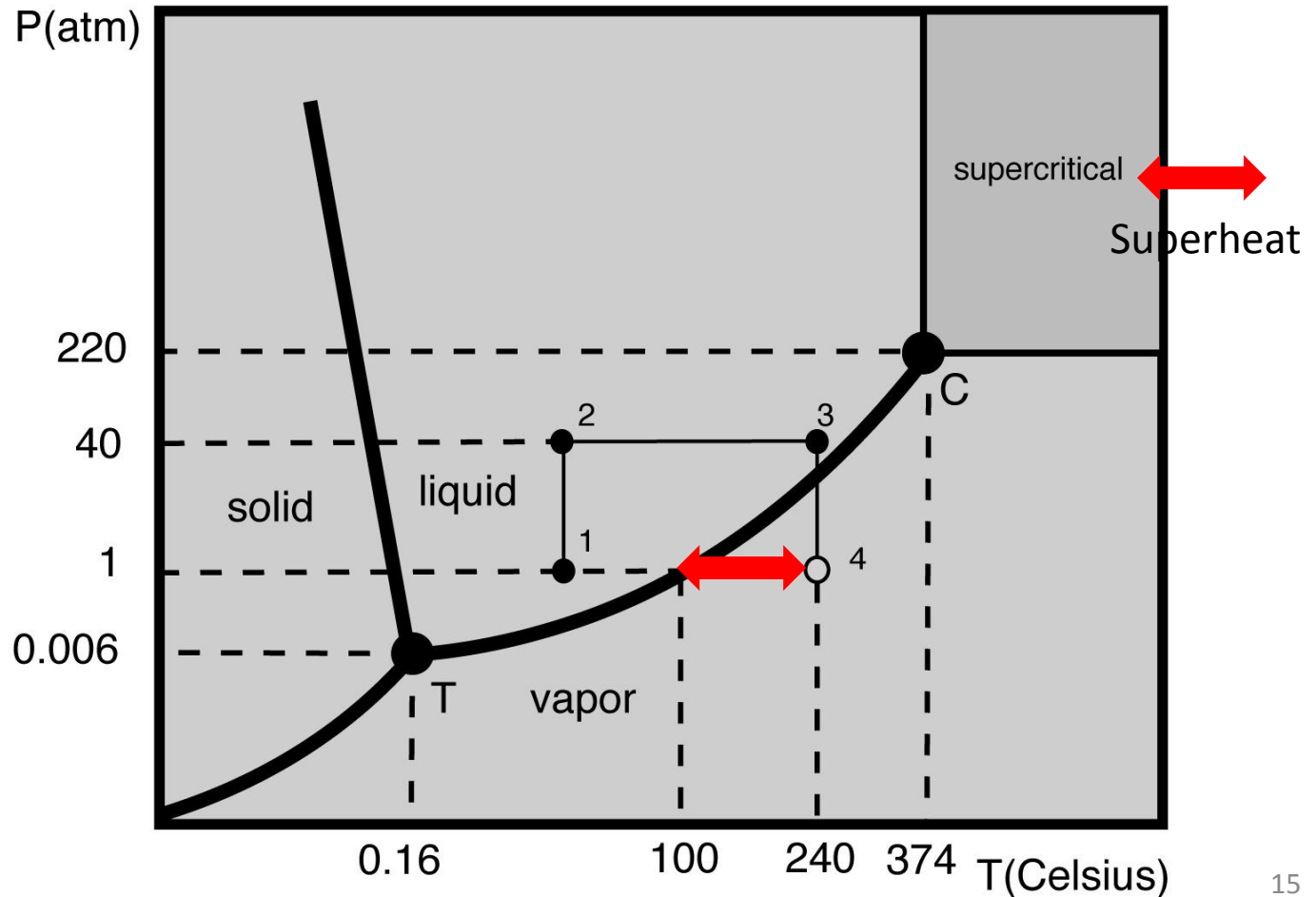


- Monochromatic  $\gamma$  beam at HIGS  $\sim 10^{7-8} \gamma/\text{s}$
- Bremsstrahlung at JLab  $\sim 10^9 \gamma/\text{s}$  (top 250 keV)

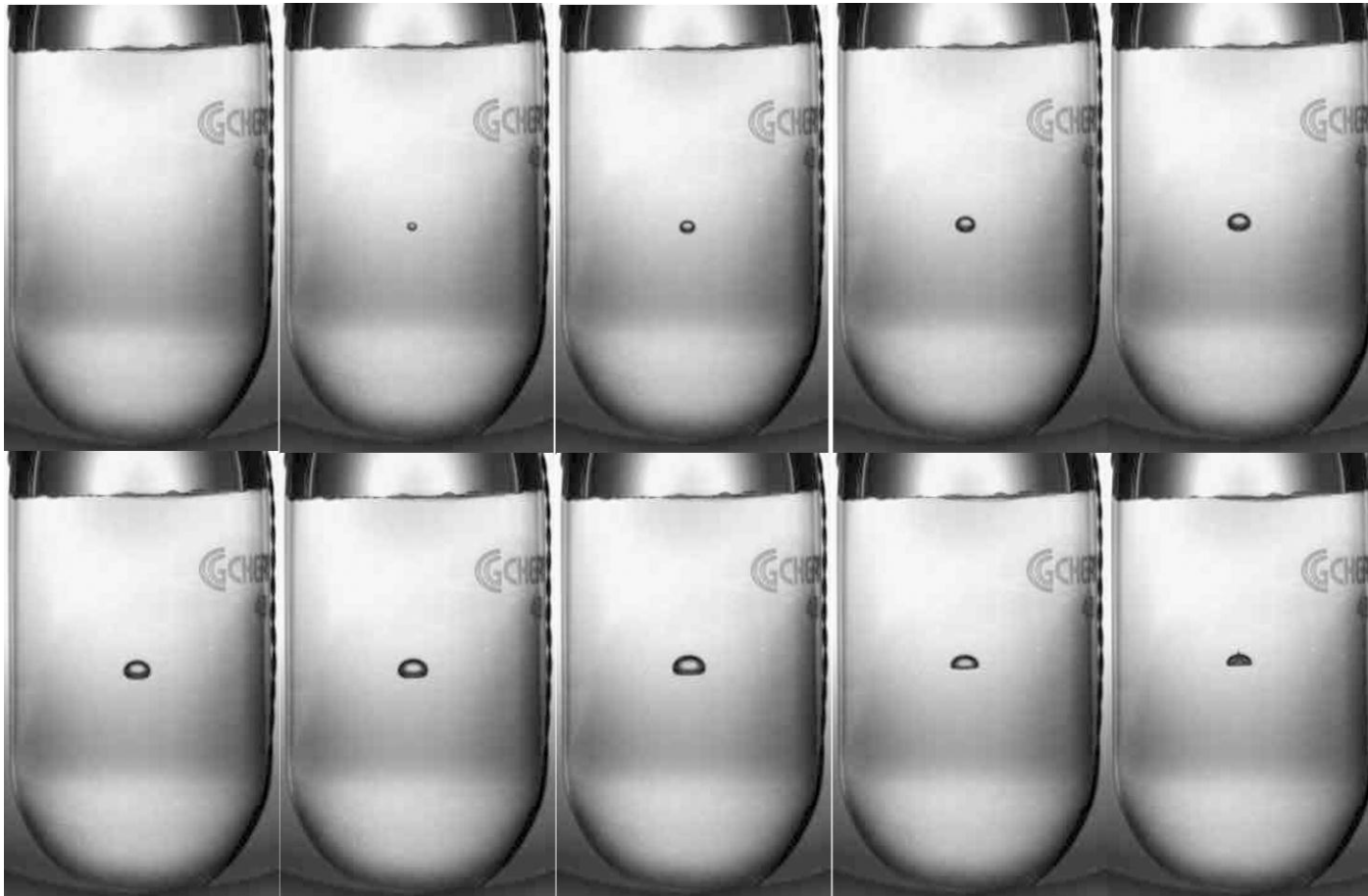
# BUBBLE CHAMBER THEORY AND DESIGN

- Donald Glaser, 86, won Nobel for inventing chamber to detect subatomic particles (1960)

- Dark Matter
- COUPP F
- PICASSO
- SIMPLE P



# BUBBLE GROWTH AND QUENCHING



$^{19}\text{F}(\gamma, \alpha)^{15}\text{N}$  in R134a

$\Delta t = 10 \text{ ms}$

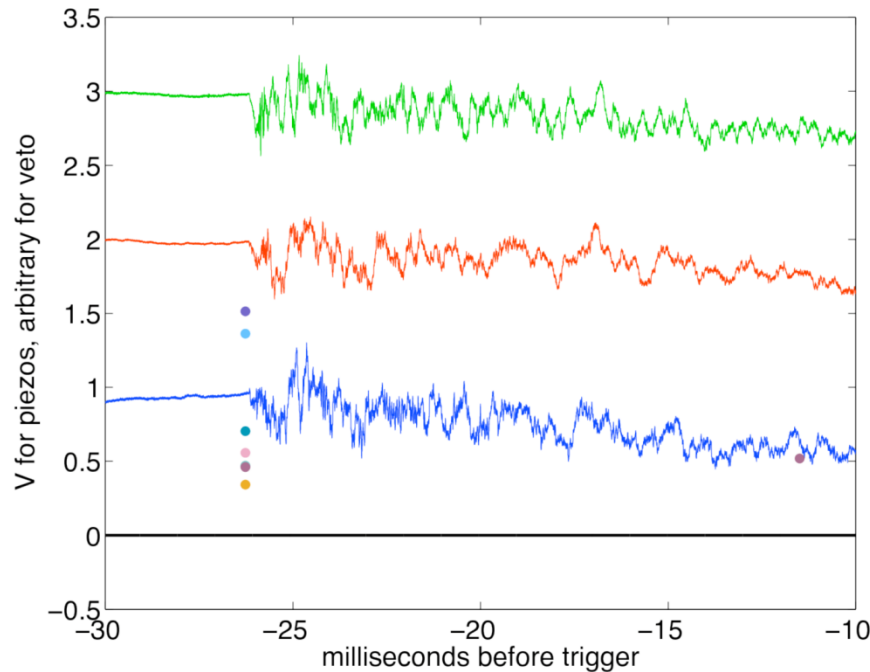


# ACOUSTIC SIGNAL: PARTICLE ID

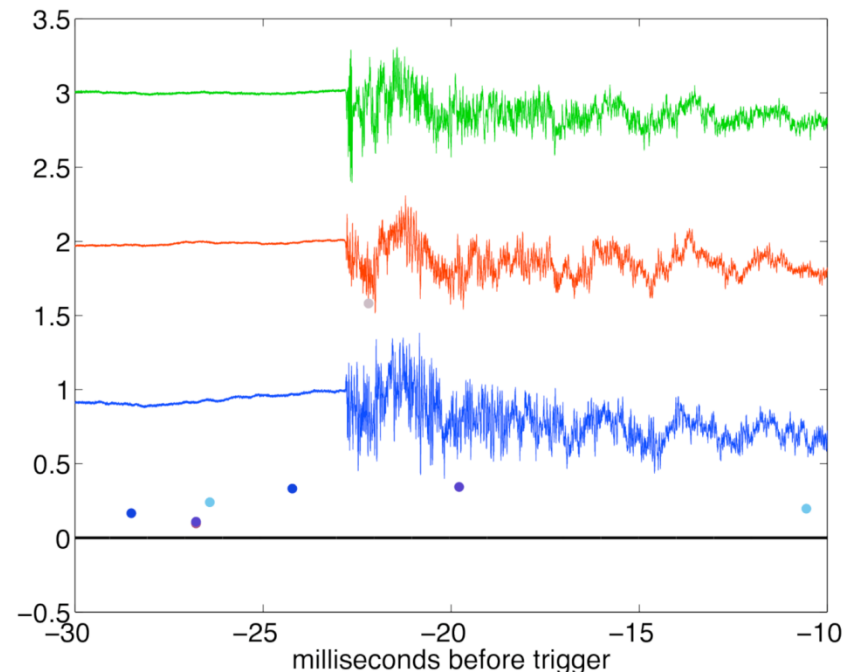
## Acoustic Signatures, time domain

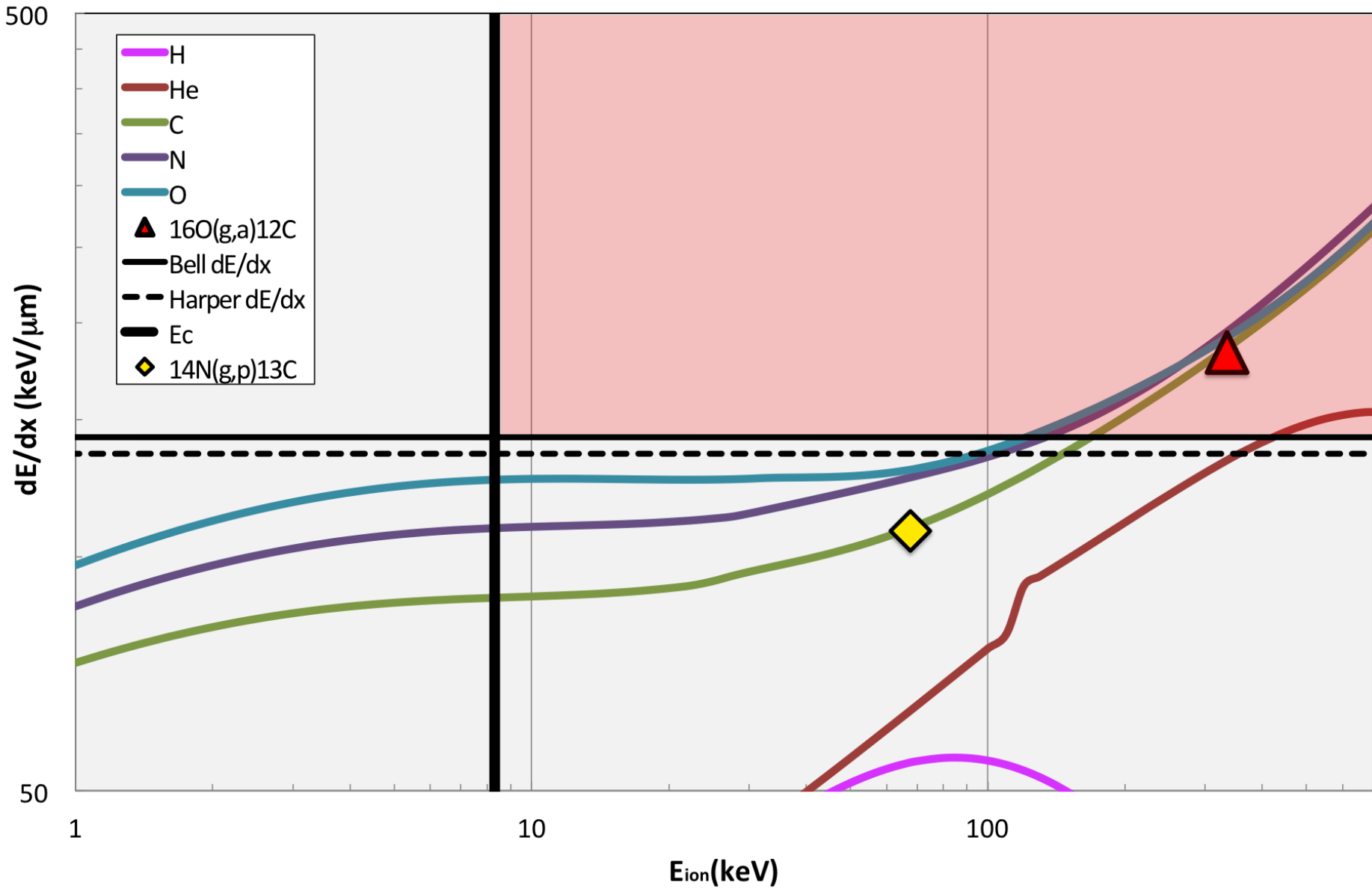
Suppress neutron events by x500 from acoustic signal – FNAL dark matter bubble chambers

### Neutron

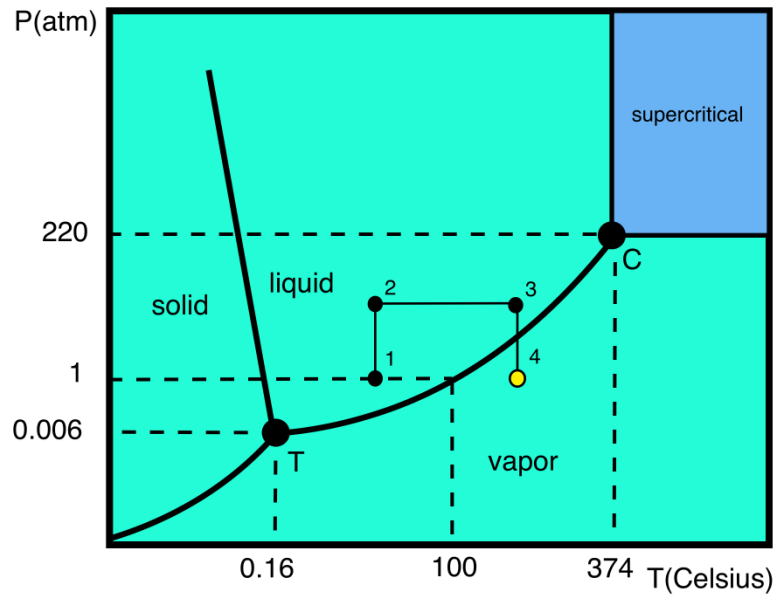


### Alpha

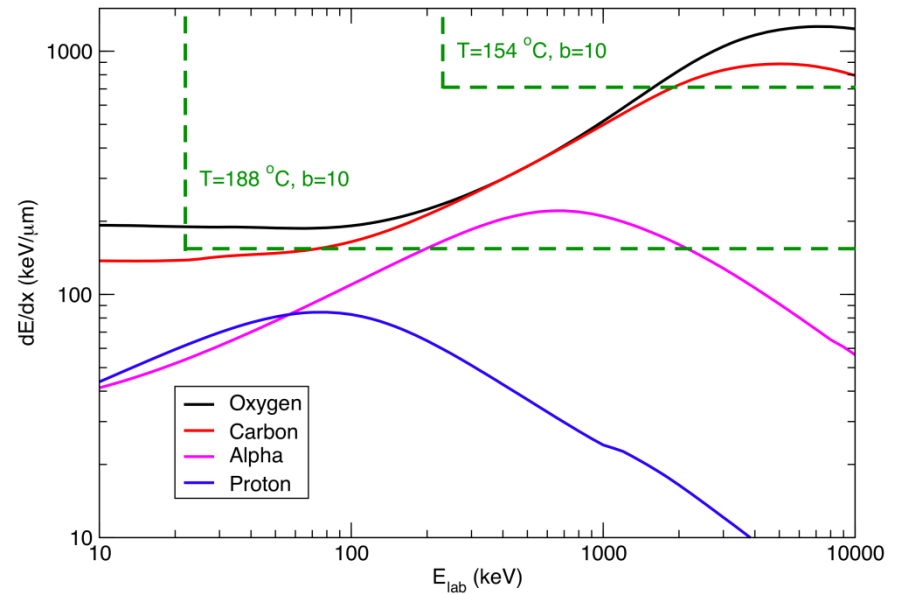




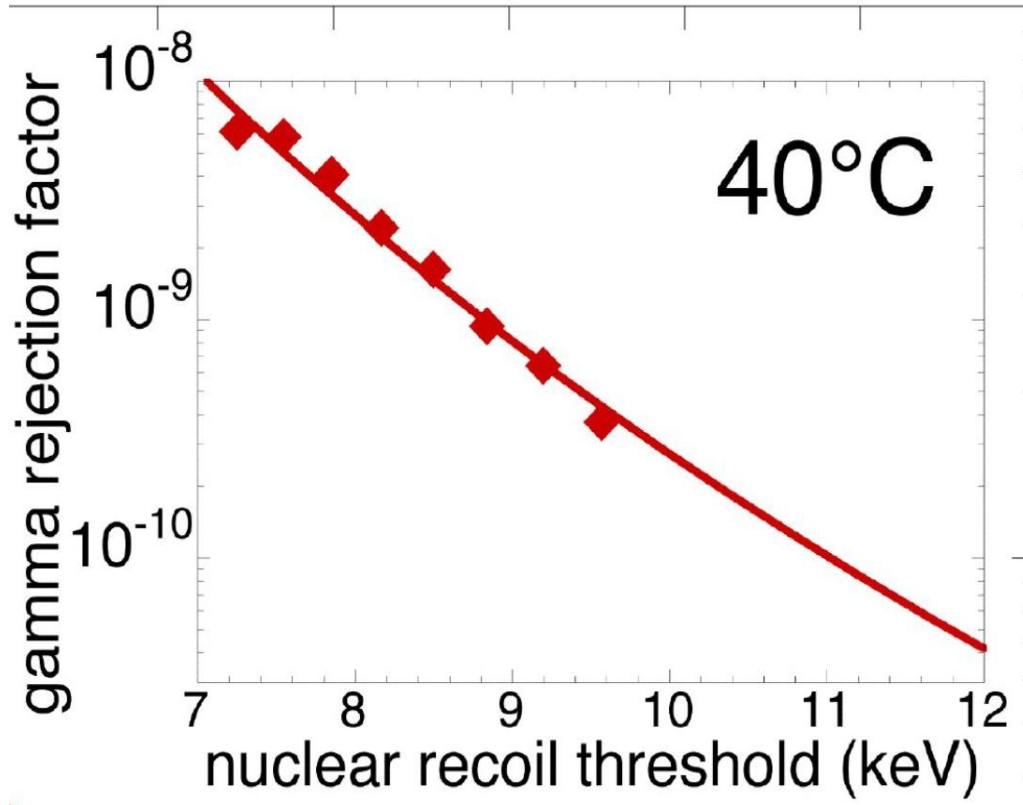
# Bubble chamber basics



Nucleation thresholds (Water)

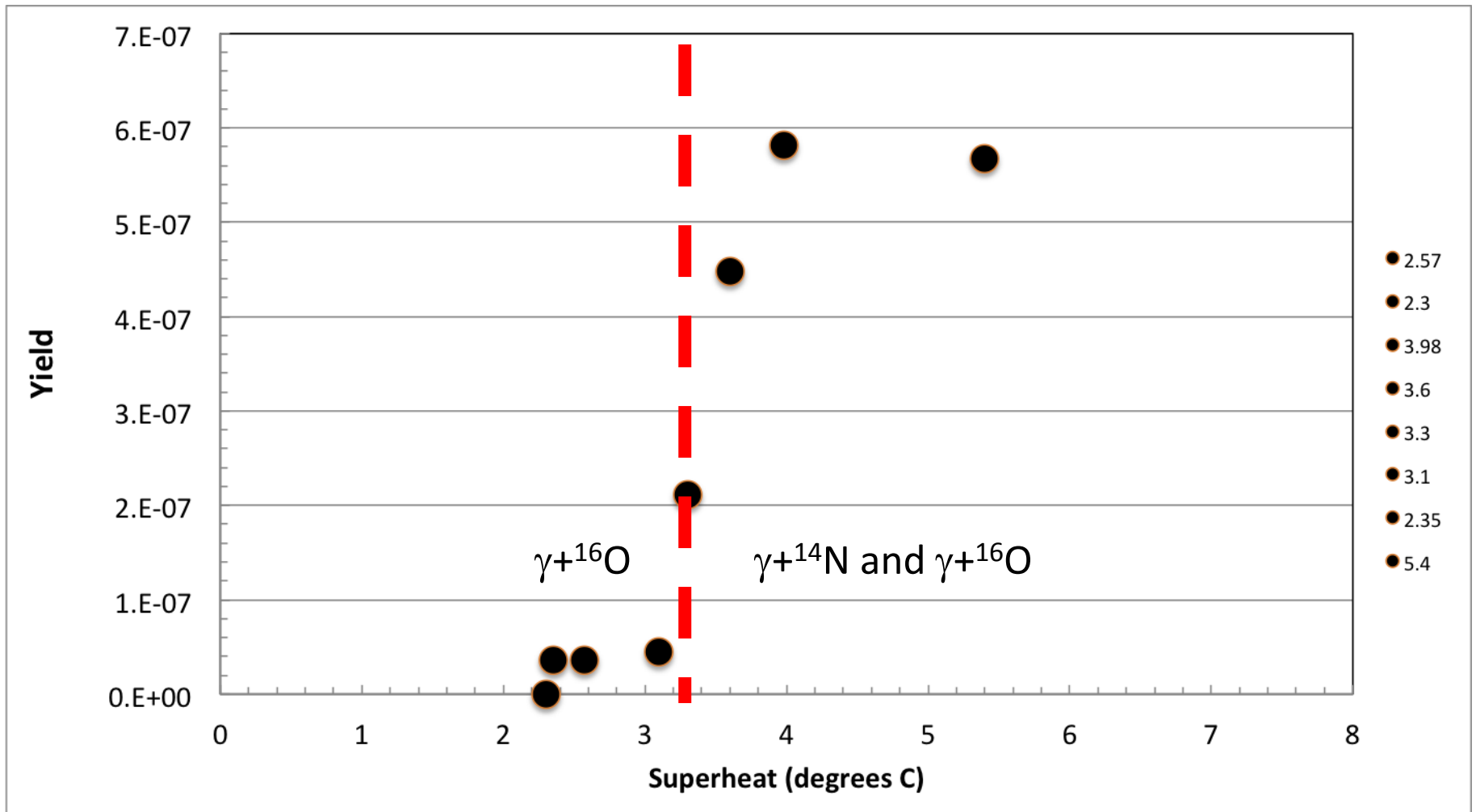


# Gamma suppression



**COUPP exp. FNAL**

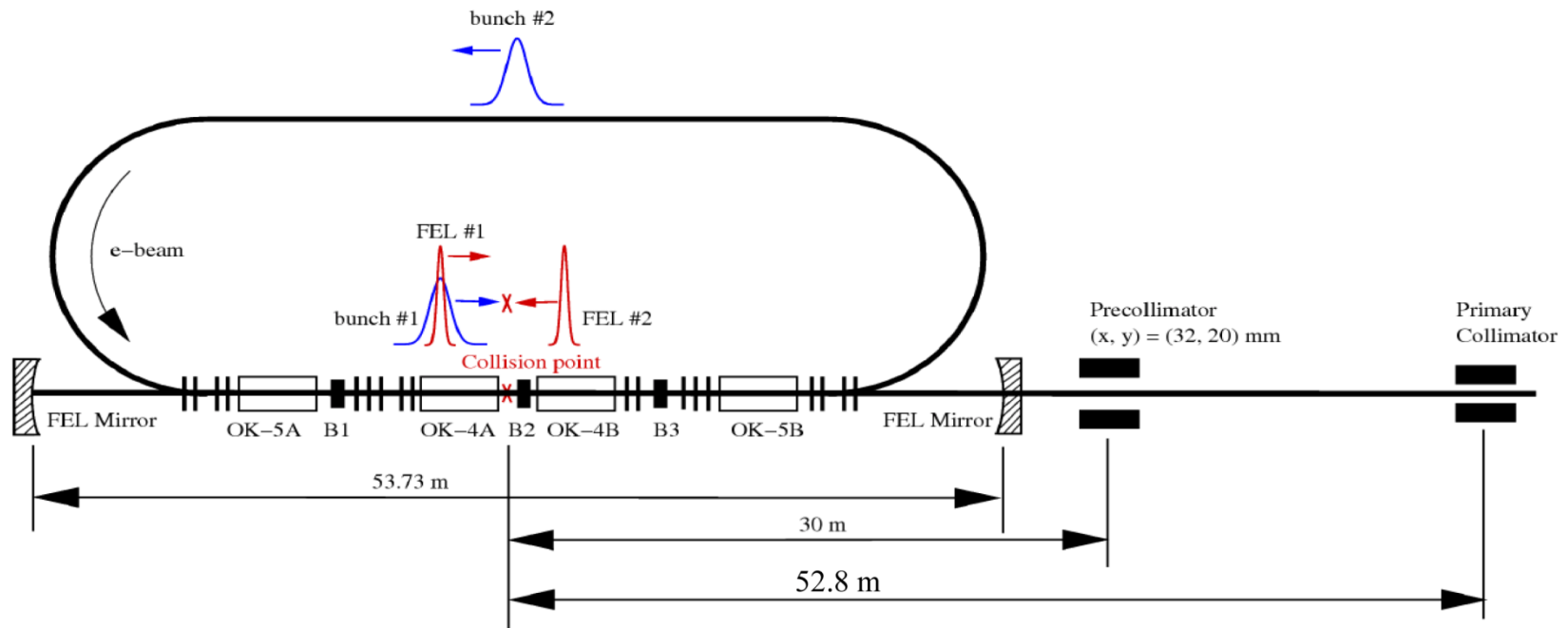
# EFFICIENCY CURVE



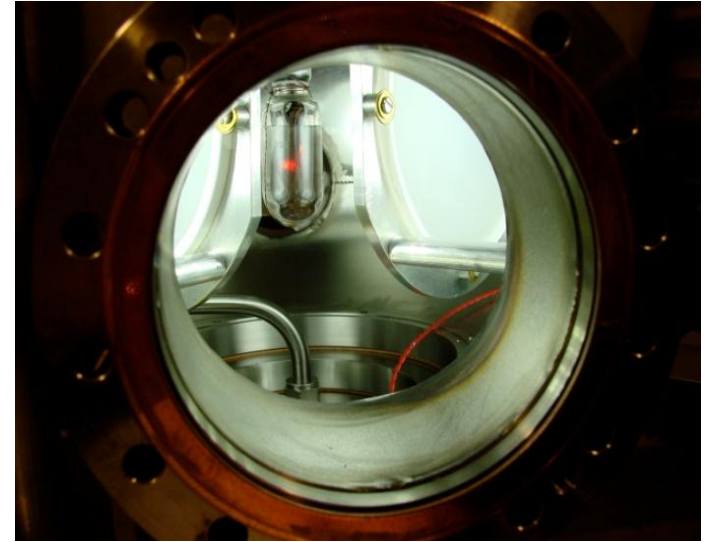
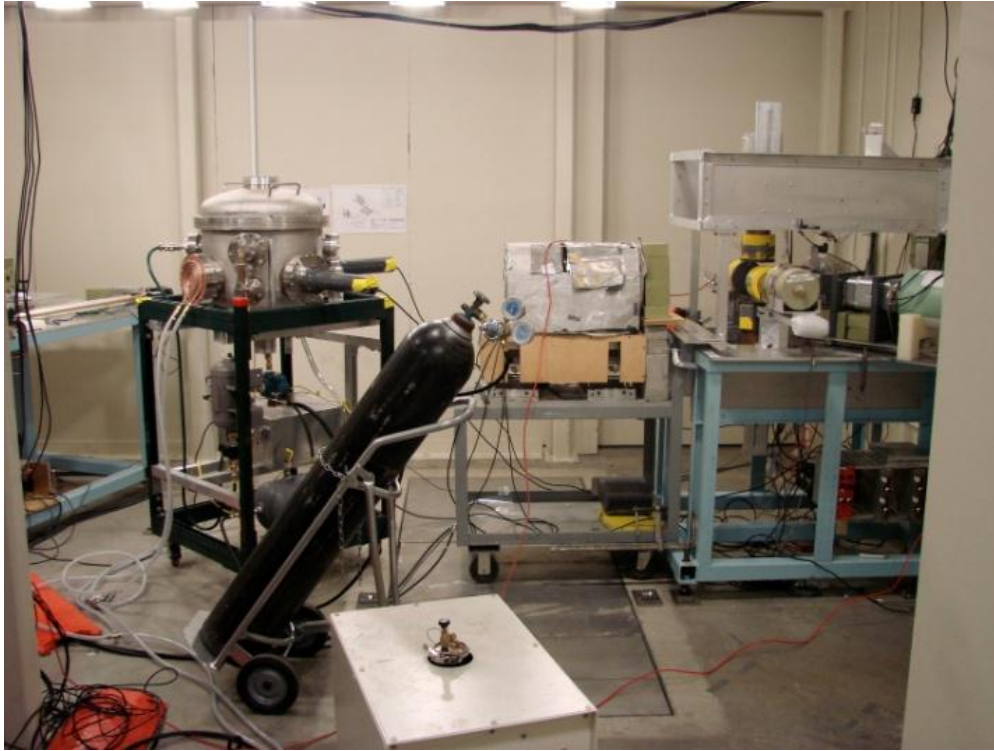
$\text{N}_2\text{O}$  efficiency curve, HIGS April 2013.  $E_\gamma = 9.7$  MeV

# BUBBLE CHAMBER AT HIGS

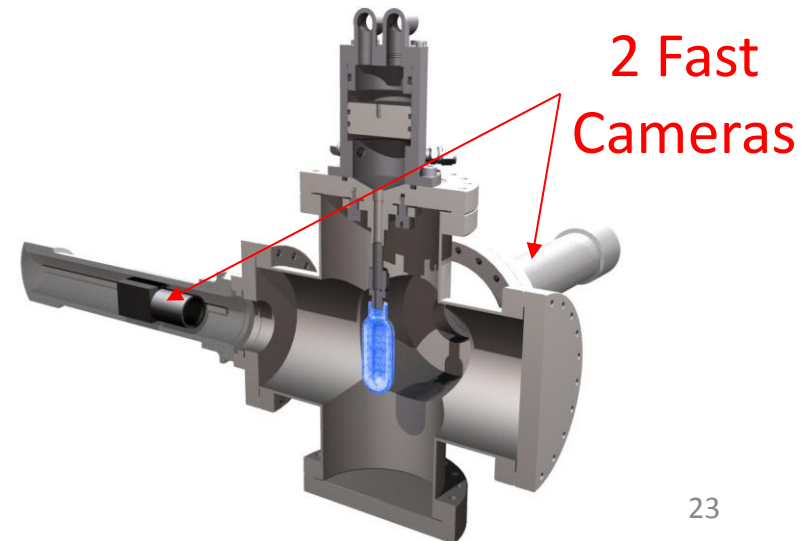
- I. High Intensity Gamma Source (HIGS) at Duke University
- II.  $\gamma$ -rays generated by Compton backscattering of free-electron-laser (FEL) light from high-energy electron beam bunches



# MEASURING $^{19}\text{F}(\gamma, \alpha)^{15}\text{N}$ AT HIGS



$\text{C}_4\text{F}_{10}$  Bubble Chamber  
T = 310 K  
P = 160 kPa – 900 kPa





Contents lists available at [SciVerse ScienceDirect](http://SciVerse ScienceDirect)

# Physics Letters B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



## First determination of an astrophysical cross section with a bubble chamber: The $^{15}\text{N}(\alpha, \gamma)^{19}\text{F}$ reaction

C. Ugalde <sup>a,\*</sup>, B. DiGiovine <sup>b</sup>, D. Henderson <sup>b</sup>, R.J. Holt <sup>b</sup>, K.E. Rehm <sup>b</sup>, A. Sonnenschein <sup>c</sup>, A. Robinson <sup>d</sup>,  
R. Raut <sup>e,f,1</sup>, G. Rusev <sup>e,f,2</sup>, A.P. Tonchev <sup>e,f,3</sup>

<sup>a</sup> Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA

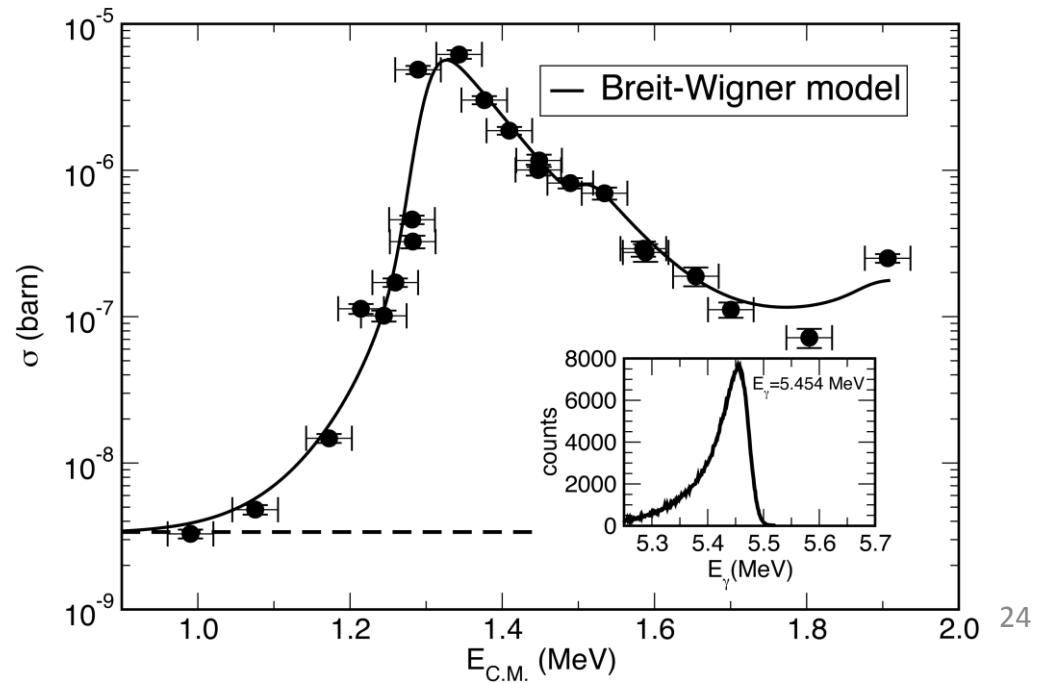
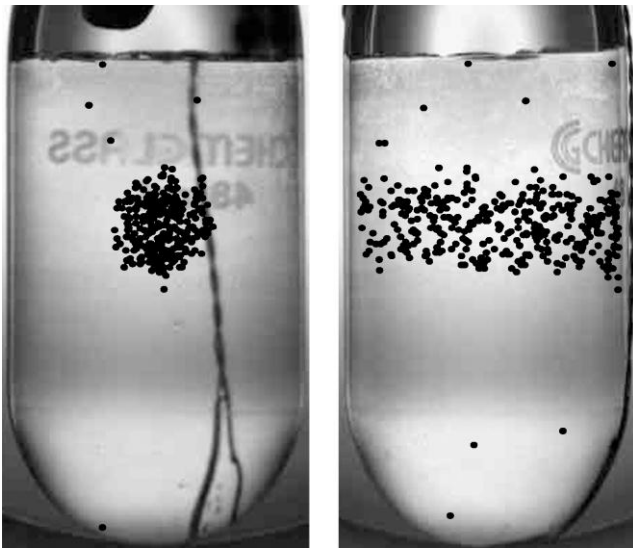
<sup>b</sup> Physics Division, Argonne National Laboratory, Argonne, IL 60439, USA

<sup>c</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA

<sup>d</sup> Department of Physics, University of Chicago, Chicago, IL 60637, USA

<sup>e</sup> Department of Physics, Duke University, Durham, NC 27708, USA

<sup>f</sup> Triangle Universities Nuclear Laboratory, Durham, NC 27708, USA





# BREMSSTRAHLUNG BACKGROUND AT HIGS

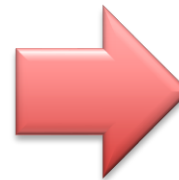
Vacuum:  $2 \times 10^{-10}$  Torr

Residual Gas:  $Z = 10$

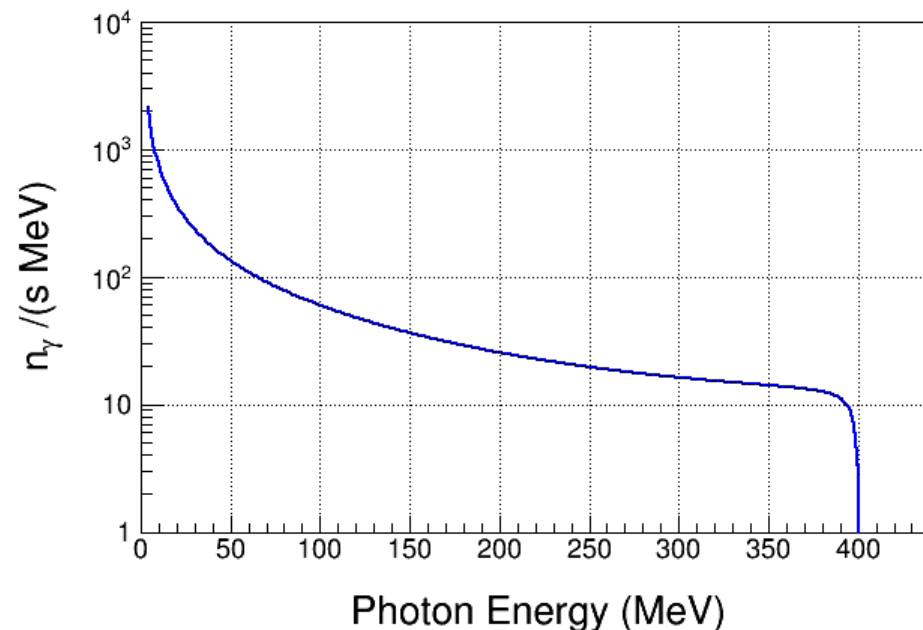
Electron Beam Energy: 400 MeV

Electron Beam Current: 41 mA

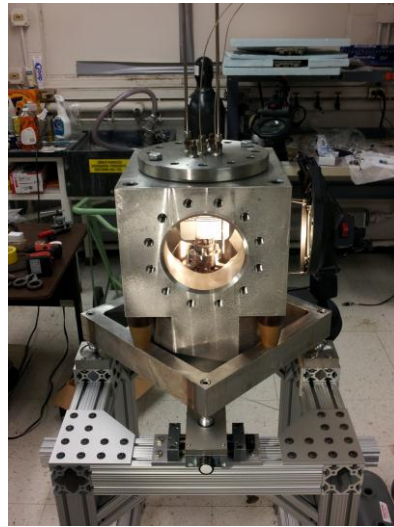
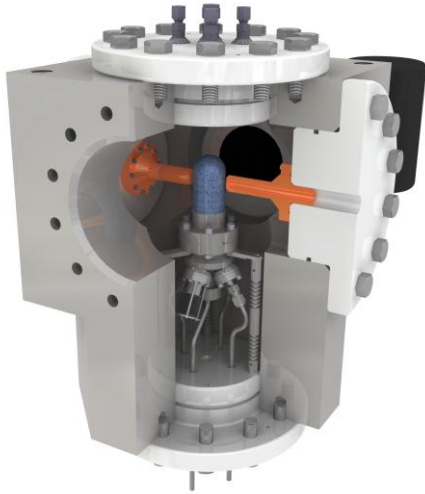
Interaction Length: 35 m



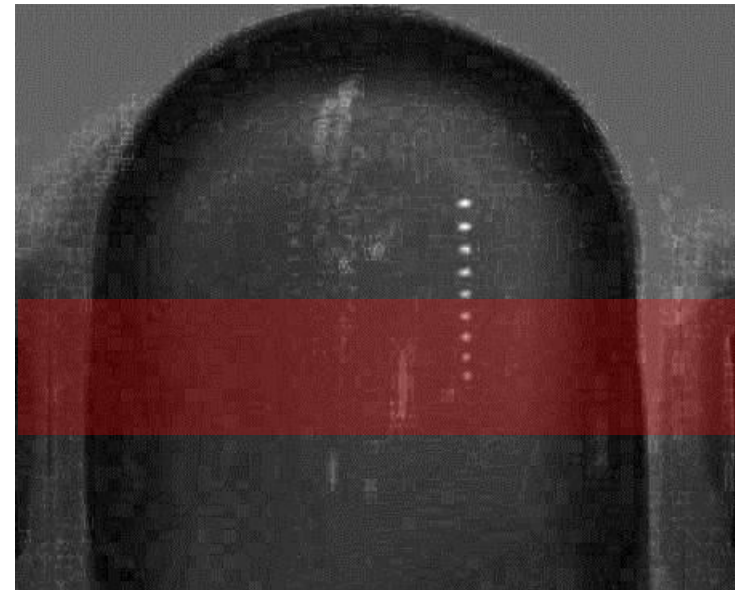
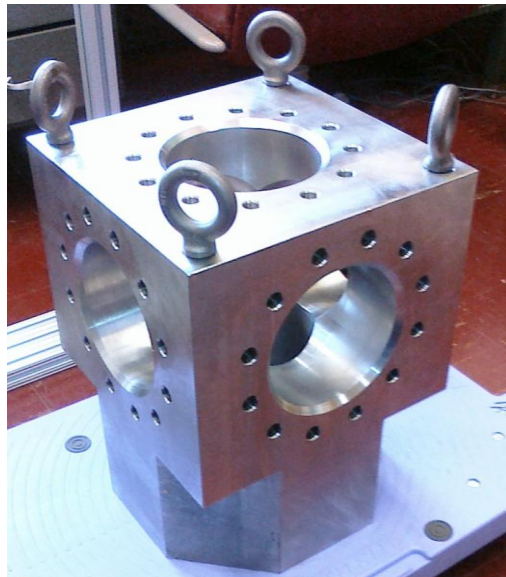
Strong Bremsstrahlung  
Background



# RECENT WORK



N<sub>2</sub>O Bubble Chamber  
First  $\gamma+O \rightarrow \alpha+C$  bubble  
April 2013



# SUPERHEATED TARGETS

I. List of superheated liquids to be used in the experiment:

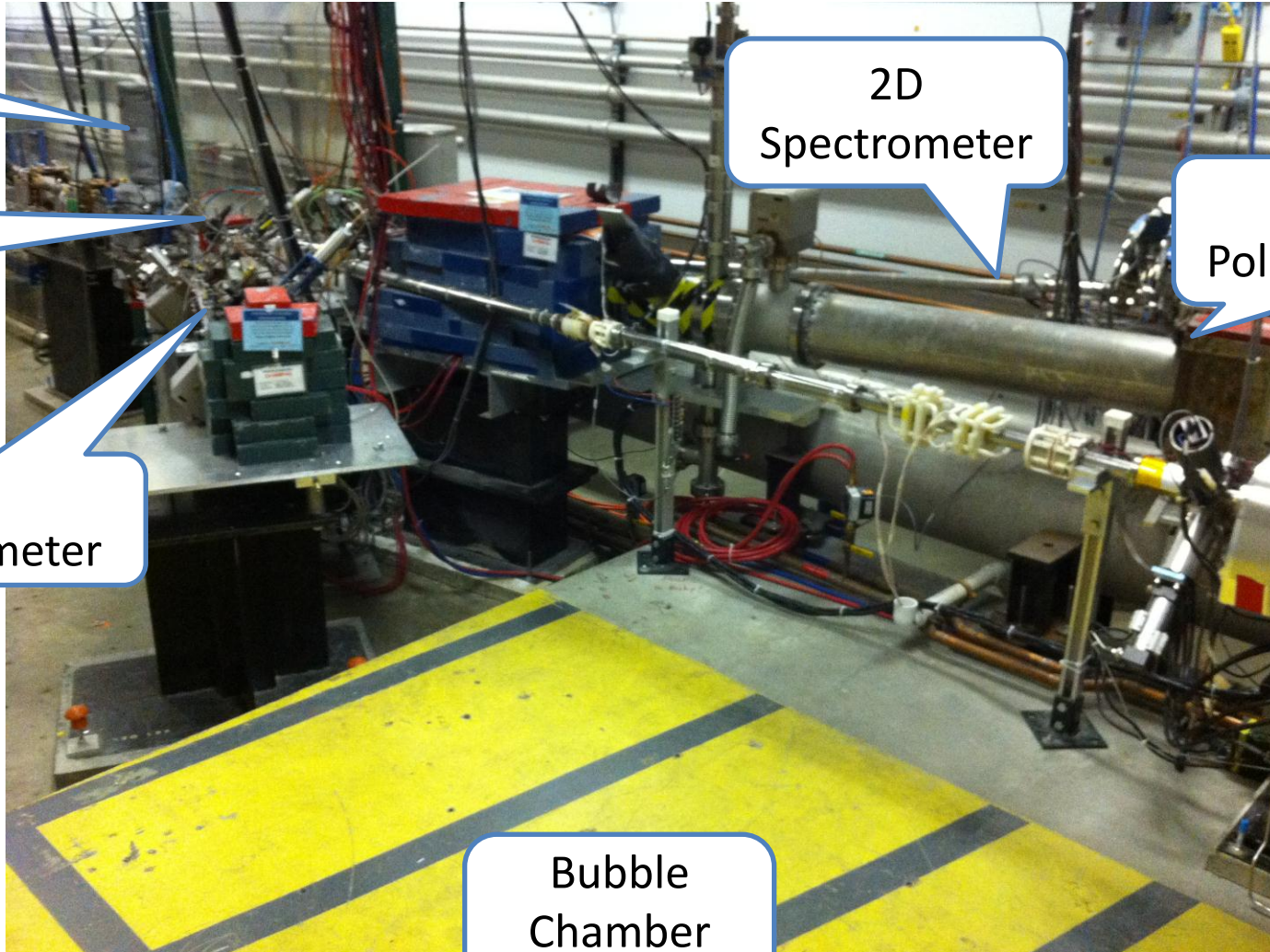
<b>N<sub>2</sub>O Targets</b>	<b><sup>16</sup>O</b>	<b><sup>17</sup>O</b>	<b><sup>18</sup>O</b>
Natural Target	99.757%	0.038%	0.205%
<sup>16</sup> O Target		Depleted > 5,000	Depleted > 5,000
<sup>17</sup> O Target		Enriched > 80%	<1.0%
<sup>18</sup> O Target		<1.0%	Enriched > 80%

II. Readout:

- I. Optical Camera
- II. Acoustic Signal to discriminate between ( $\gamma, \alpha$ ) and ( $\gamma, n$ ) events



# EXPERIMENTAL SETUP



BCM

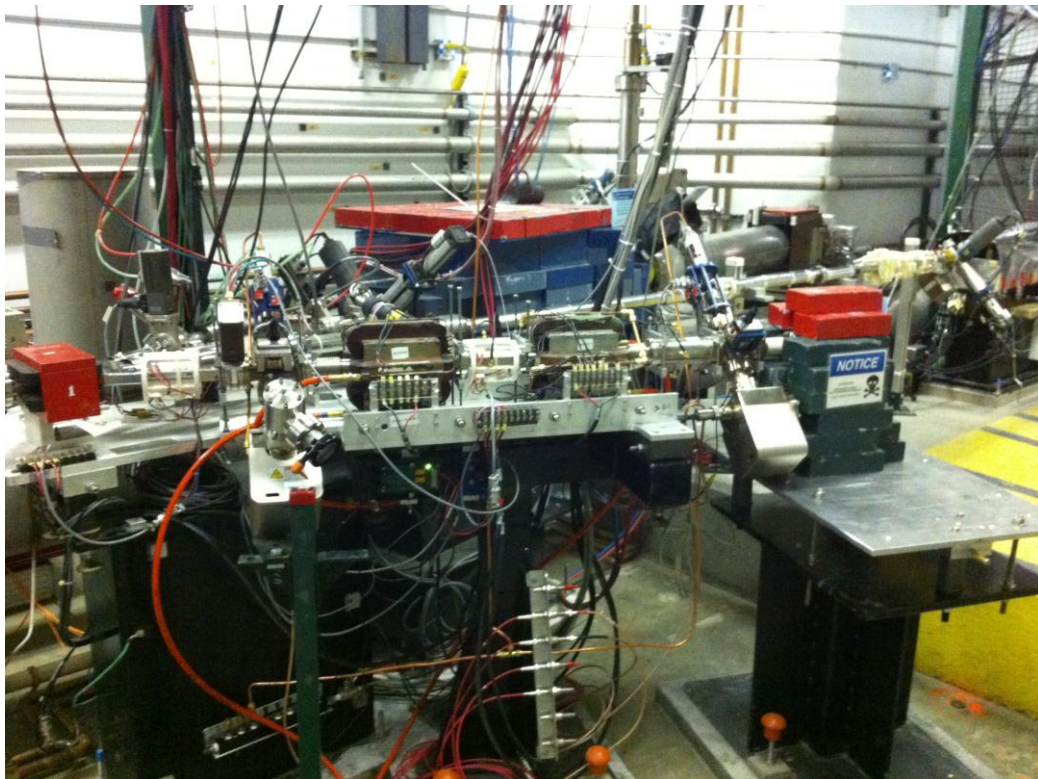
5 MeV  
Dipole

5D  
Spectrometer

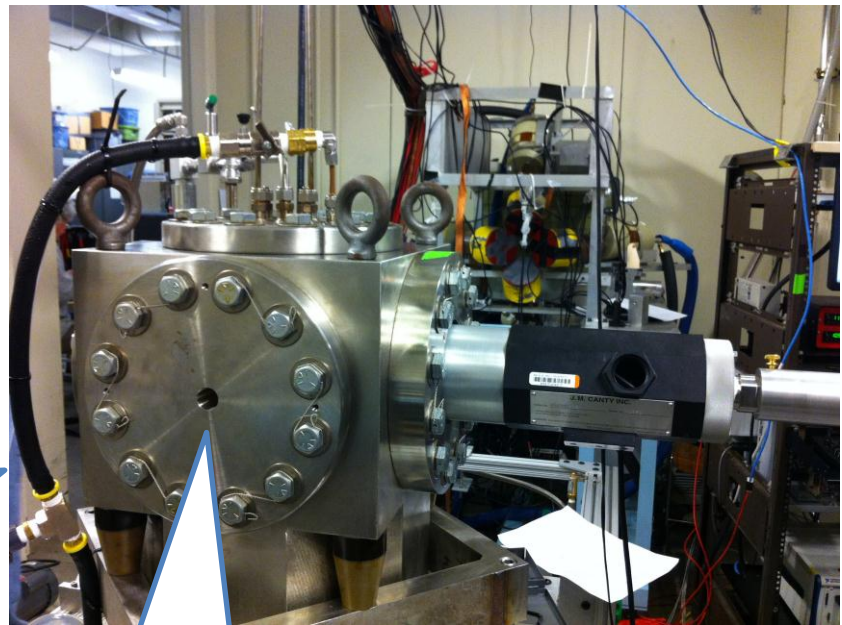
2D  
Spectrometer

Mott  
Polarimeter

Bubble  
Chamber  
location



5D  
Spectrometer



Bubble  
Chamber at  
HIGS

Photon Beam  
Entrance



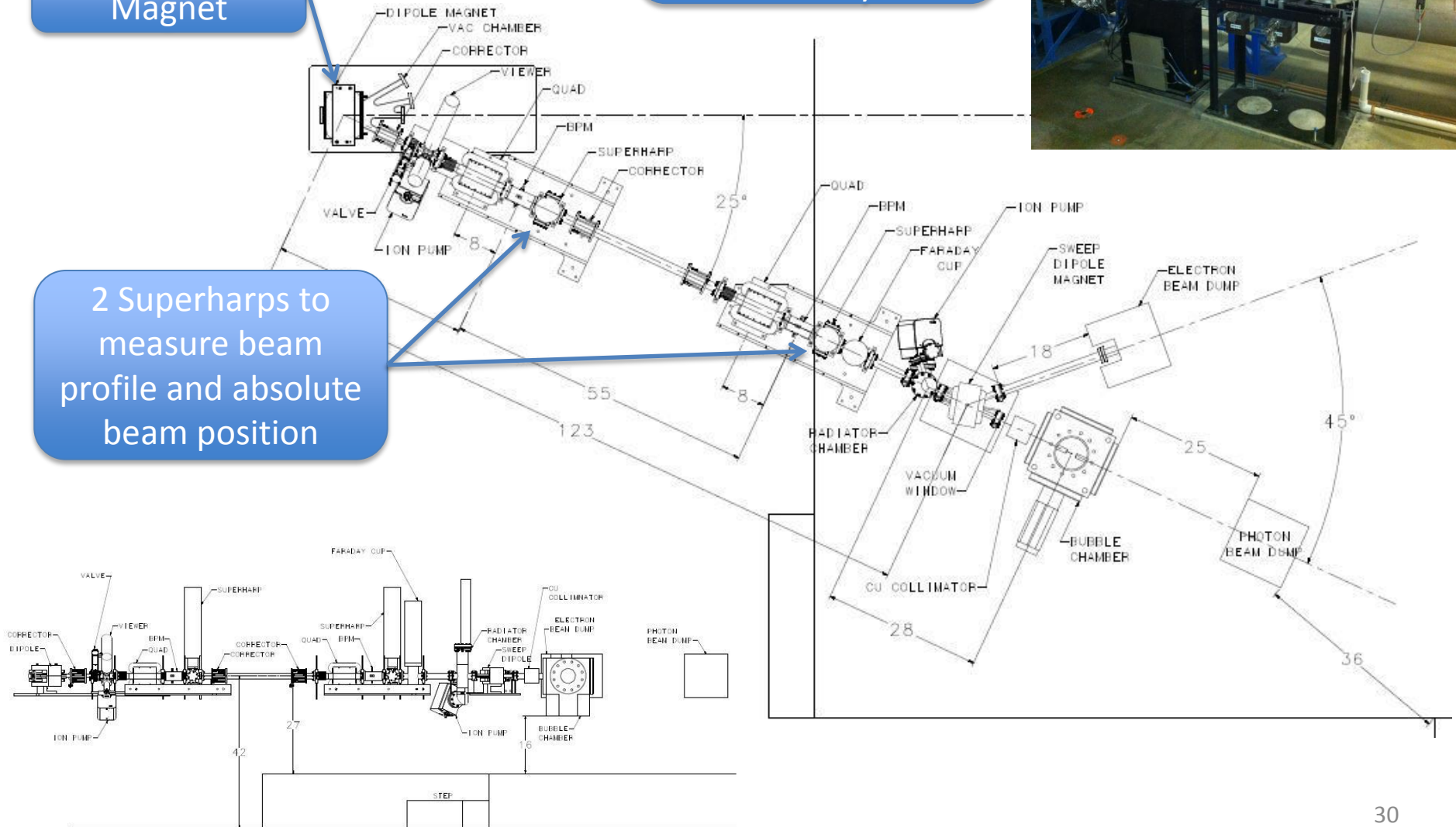
# BEAMLINE

Replace Dipole Magnet

New Fast Valve to protect from vacuum failure in front of ¼ Cryo-unit

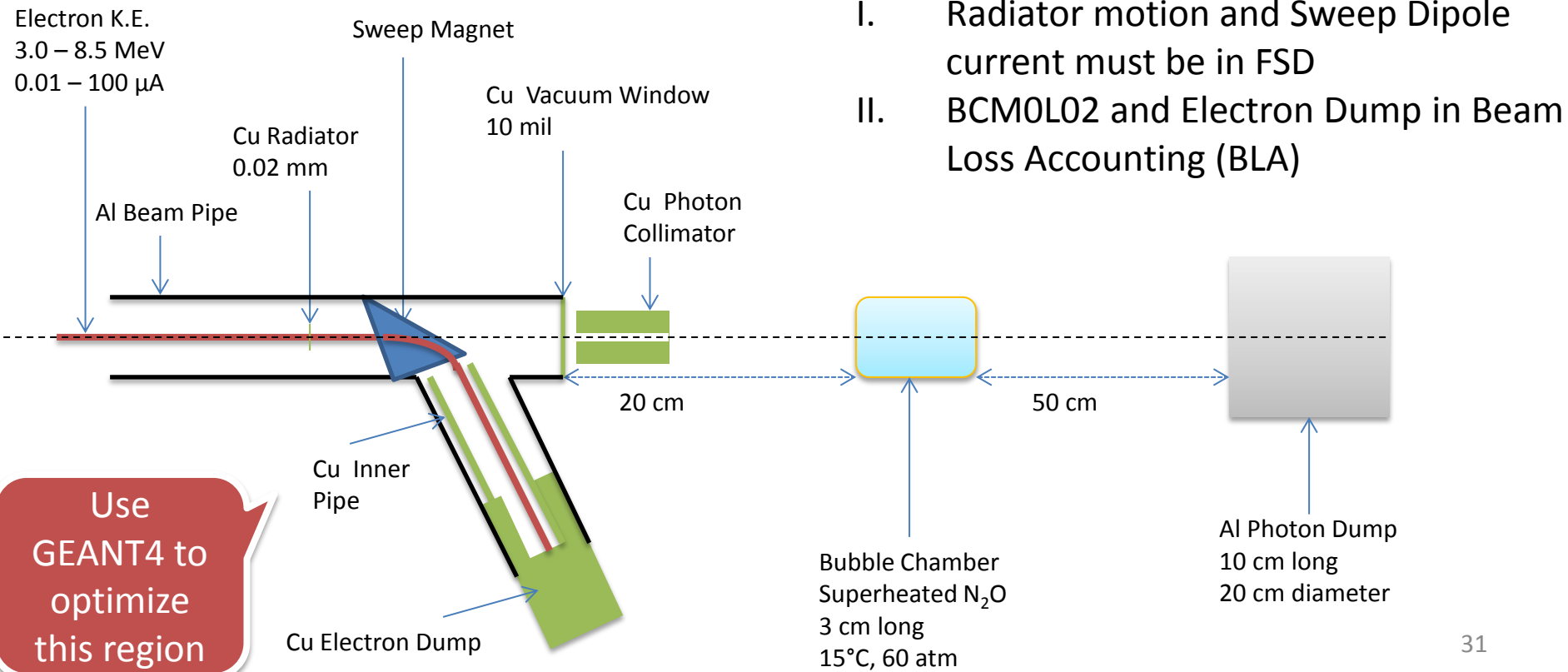


2 Superharps to measure beam profile and absolute beam position



# SCHEMATICS

- Power deposited in radiator (100  $\mu$ A and 8.5 MeV) :
  - I. 0.02 mm: Energy loss = 21 keV, P = 2.1 W
  - II. 0.10 mm: Energy loss = 112 keV, P = 11 W
- Pure Copper and Aluminum (high neutron threshold):
  - I.  $^{63}\text{C}(\gamma, n)$  threshold = 10.86 MeV
  - II.  $^{27}\text{Al}(\gamma, n)$  threshold = 13.06 MeV



- I. Radiator motion and Sweep Dipole current must be in FSD
- II. BCMOL02 and Electron Dump in Beam Loss Accounting (BLA)

# BEAM REQUIREMENTS

## I. Beam Properties at Radiator:

Beam Kinetic Energy, (MeV)	7.9 – 8.5
Beam Current ( $\mu\text{A}$ )	0.01 – 100
Absolute Beam Energy	<0.1%
Relative Beam Energy	<0.02%
Energy Resolution (Spread), $\sigma_T/T$	0.06%
Beam Size, $\sigma_{x,y}$ (mm)	1 – 2

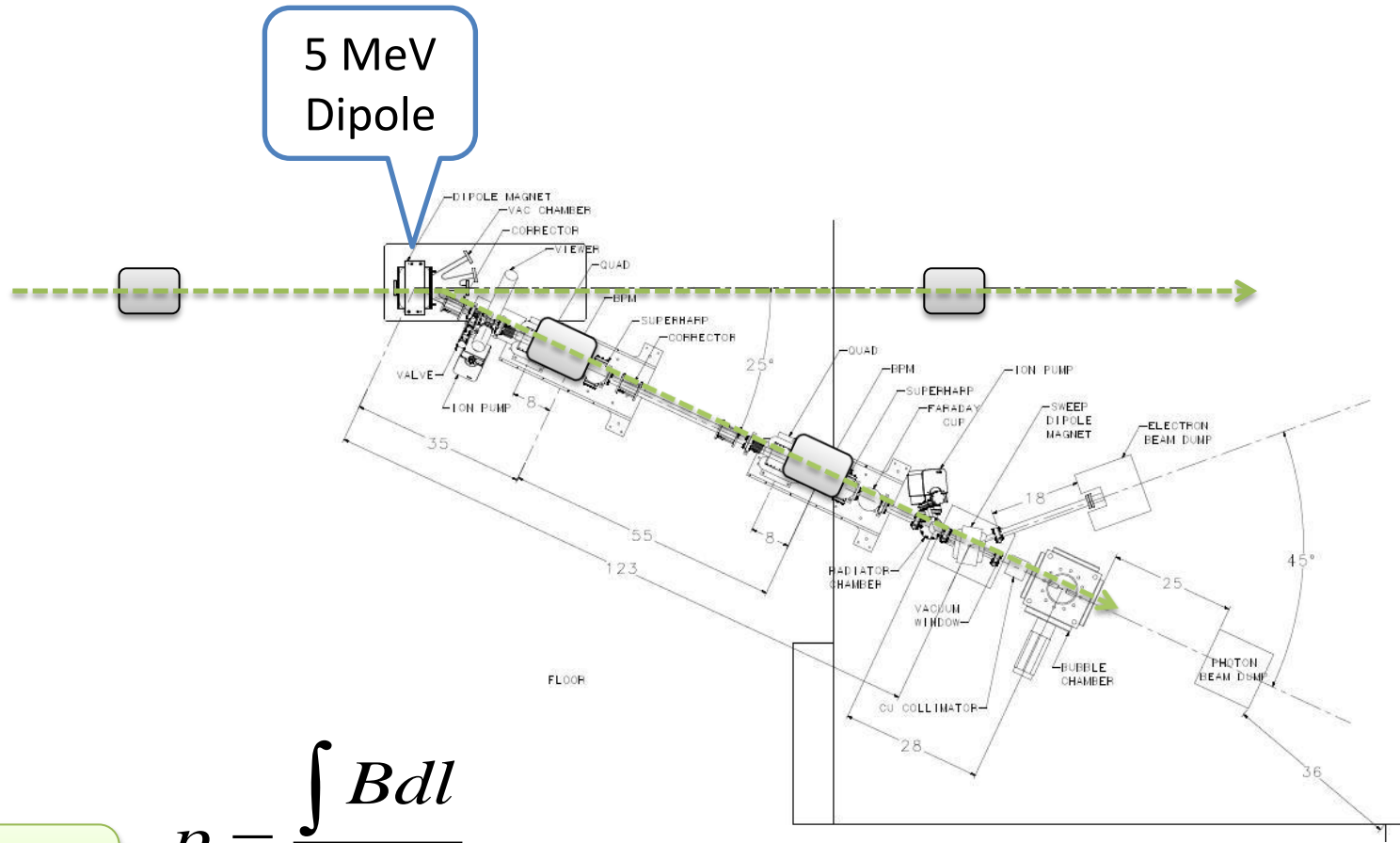
II. PEPPo achieved  $p=8.25$  MeV/c or K.E.=7.75 MeV. Maximum stable  $\frac{1}{4}$ - cryounit cavity gradients achieved: 8.4 MV/m and 6.1 MV/m (7.25 MV/m average). Vacuum in the beam line indicates that field emission and desorbed gas are the most problematic, but improve with processing.

III. Helium process the  $\frac{1}{4}$ -cryounit



# ABSOLUTE BEAM ENERGY

□ BPM



Electron Beam Momentum

$$p = \frac{\int Bdl}{\theta}$$

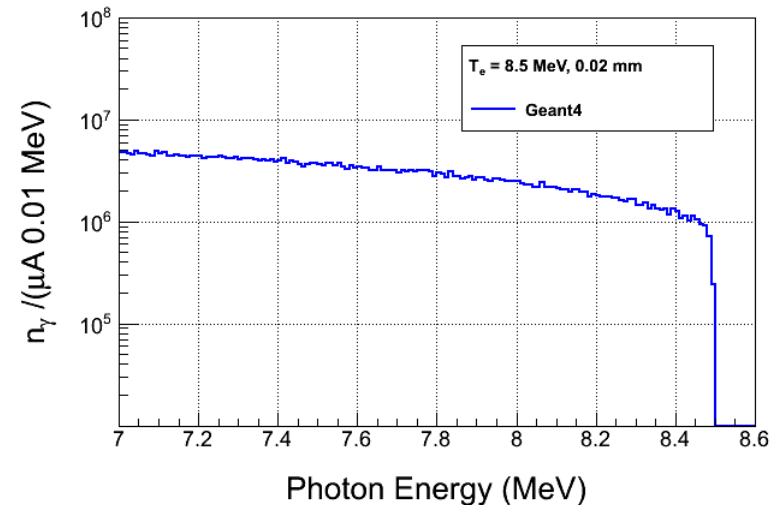
Parameter	Term	Now	Goal
Dipole – linearity	$\delta B/B$	0.25%	0.02%
Dipole – spatial	$\delta BL/BL$	0.10%	0.02%
Dipole – reproduce	$\delta B/B$	0.10%	0.02%
Dipole – power supply	$\delta I/I$	0.20%	0.02%
Position – surveys	$\delta \theta/\theta$	0.01%	0.01%
Position – BPM calibration	$\delta \theta/\theta$	0.05%	0.05%
Stray magnetic field	$\delta \theta/\theta$	0.05%	0.05%
<b>TOTAL</b>	<b><math>\delta P/P</math></b>	<b>0.36%</b>	<b>&lt;0.10%</b>

## Goal:

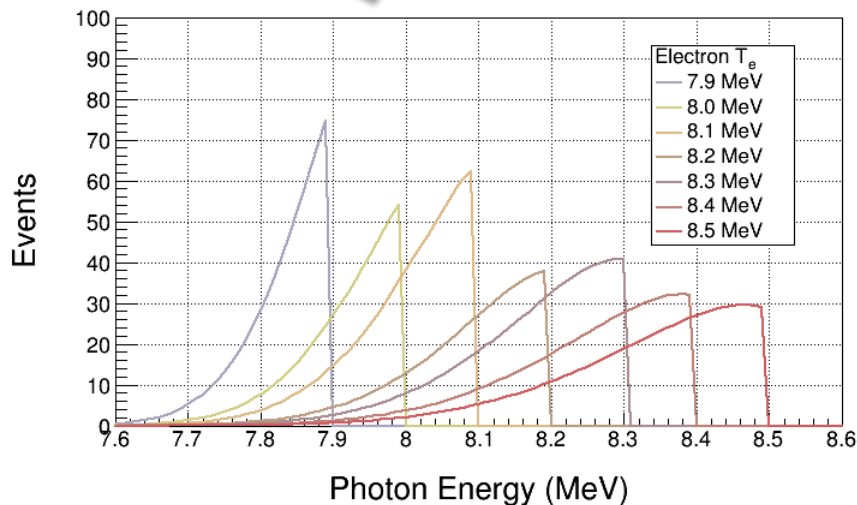
- I. Jay Benesch designed and now fabricating higher quality dipole (more uniformity, higher field)
- II. New Hall Probe: 0.01% accuracy, resolution to 2 ppm, and a temperature stability of 10 ppm/°C
- III. Relative beam energy error: <0.02%

# BREMSSTRAHLUNG BEAM

- Use both GEANT4 and FLUKA to calculate Bremsstrahlung spectra
- Monte Carlo simulation of bremsstrahlung at radiotherapy energies is well studied, accuracy: 5%



Bremsstrahlung  
Peaks



- $^{16}\text{O}(\gamma, \alpha)^{12}\text{C}$  is ideal case for Bremsstrahlung beam and Penfold – Leiss Unfolding :
- I. Very steep; only photons near endpoint contribute to yield
  - II. No-structure (resonances)

# GEANT4 SIMULATION

- Both GEANT4 and FLUKA use models that calculate wrong photo–nuclear cross sections. Both do not allow for user’s cross sections.
  - I. Use GEANT4 and FLUKA to produce the photon spectrum impinging on the super heated liquid.
  - II. Fold the above photon spectrum with our cross sections in stand-alone codes.
- Use GEANT4 to design Radiator/Collimator/Dump
- Geometry in GEANT4:

# PENFOLD-LEISS CROSS SECTION UNFOLDING

- Measure Yields at:  $E = E_1, E_2, \dots, E_n$  where,

$$E_i - E_{i-1} = \Delta, i = 2, n$$

$$Y(E_i) = \int_{th}^{E_i} n_\gamma(E_i, k) \sigma(k) dk \approx \sum_{j=1}^i N_\gamma(E_i, \Delta, E_j) \sigma(E_j)$$

- The solution can be written in two forms:

$$\sigma_i = \frac{1}{N_{ii}} \left[ y_i - \sum_{j=1}^{i-1} (N_{ij} \sigma_j) \right]$$

- Or, Matrix form:

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix} = \begin{bmatrix} N_{\gamma,11} & 0 & \cdots & 0 \\ N_{\gamma,21} & N_{\gamma,22} & \cdots & 0 \\ \vdots & \ddots & \ddots & 0 \\ N_{\gamma,n1} & N_{\gamma,n2} & \cdots & N_{\gamma,nn} \end{bmatrix} \begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \vdots \\ \sigma_n \end{bmatrix}$$

$$[Y] = [N] \bullet [\sigma]$$

$$[\sigma] = [N]^{-1} \bullet [Y]$$

# STATISTICAL ERROR PROPAGATION

- Note:  $\frac{dy_i}{y_i} = \frac{1}{\sqrt{y_i}}$        $\frac{dN_{ij}}{N_{ij}} = \frac{1}{\sqrt{N_{ij}}} \approx 0$

$$dy_i = \sqrt{y_i} \qquad dy_i = \sqrt{y_i + 2y_i^{bg}}$$

In case of  
background  
Subtraction

- With:

$$[B] = [N]^{-1}$$

$$[\sigma] = [B] \bullet [Y]$$

- Then:

$$[d\sigma^2] = [B] \bullet [dY^2] \bullet [B]^T$$

- Where:

$$[dY^2] = \begin{bmatrix} y_1 & 0 & \cdots & 0 \\ 0 & y_2 & \cdots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & y_n \end{bmatrix}$$

$$\begin{aligned} \text{var}(y_i, y_i) &= y_i \\ \text{cov}(y_i, y_j) &= 0 \end{aligned}$$

$$[d\sigma^2] = \begin{bmatrix} d\sigma_1^2 & \text{cov}(\sigma_1, \sigma_2) & \cdots & \text{cov}(\sigma_1, \sigma_n) \\ \text{cov}(\sigma_2, \sigma_1) & d\sigma_2^2 & \cdots & \text{cov}(\sigma_2, \sigma_n) \\ \vdots & \ddots & \ddots & \vdots \\ \text{cov}(\sigma_n, \sigma_1) & \text{cov}(\sigma_n, \sigma_2) & \cdots & d\sigma_n^2 \end{bmatrix}$$

Although,

$$\begin{aligned} \text{cov}(y_i, y_j) &= 0, \\ \text{cov}(\sigma_i, \sigma_j) &\neq 0 \end{aligned}$$

$$(d\sigma_i)^2 = \frac{1}{N_{ii}^2} \left[ dy_i^2 + \sum_{j=1}^{i-1} (N_{ij} d\sigma_j)^2 + \sum_{k=1}^{i-1} \sum_{l=1}^{i-1} N_{ik} \text{cov}(\sigma_k, \sigma_l) N_{il} \right]$$

For mono-  
chromatic  
beam

$$\left( \frac{d\sigma_i}{\sigma_i} \right)^2 = \left( \frac{dy_i}{y_i} \right)^2 = \frac{1}{y_i}$$

# RESULTS

- I. Radiator Thickness = 0.02 mm
- II. Bubble Chamber Thickness = 3.0 cm. Number of  $^{16}\text{O}$  nuclei =  $3.474e22 / \text{cm}^2$
- III. Background subtraction of  $^{18}\text{O}(\gamma, \alpha)^{14}\text{C}$  .  $^{17}\text{O}(\gamma, n)^{16}\text{O}$ : Still to do

$$[N] = \begin{bmatrix} 3.267e14 & 0 & 0 & 0 & 0 & 0 & 0 \\ 9.782e13 & 6.439e13 & 0 & 0 & 0 & 0 & 0 \\ 5.013e13 & 3.858e13 & 2.539e13 & 0 & 0 & 0 & 0 \\ 1.494e13 & 1.236e13 & 9.514e12 & 6.258e12 & 0 & 0 & 0 \\ 8.540e12 & 7.369e12 & 6.097e12 & 4.692e12 & 3.086e12 & 0 & 0 \\ 3.801e12 & 3.370e12 & 2.908e12 & 2.406e12 & 1.852e12 & 1.217e12 & 0 \\ 2.075e12 & 1.875e12 & 1.663e12 & 1.435e12 & 1.187e12 & 9.137e11 & 6.004e11 \end{bmatrix}$$

Electron Beam K. E.	Beam Current ( $\mu\text{A}$ )	Time (hour)	$y_i$	$dy_i$ (no bg)	$dy_i/y_i$ (no bg, %)	$dy_i$ (with bg)	$dy_i/y_i$ (with bg, %)
7.9	100	100	545	23	4.2	134	24.6
8.0	100	20	581	24	4.1	77	13.3
8.1	80	10	852	29	3.4	60	7.0
8.2	20	10	634	25	3.9	40	6.3
8.3	10	10	812	28	3.4	39	4.8
8.4	4	10	746	27	3.6	36	4.8
8.5	2	10	763	28	3.7	32	4.2



# SYSTEMATIC ERROR PROPAGATION

- For absolute beam energy uncertainty of  $\delta E$  ( $= 0.1\%$ ) and zero relative beam energy uncertainty:

$$\frac{dy_i}{y_i} = \frac{y_i(E_i + \delta E) - y_i(E_i)}{y_i(E_i)}$$

$$\frac{dN_{ij}}{N_{ij}} = \frac{N_{ij}(E_i + \delta E) - N_{ij}(E_i)}{N_{ij}(E_i)}$$

$$E_0 = 7.8 + \delta E$$

$$E_i = E_0 + i\Delta$$

$E_i$ (MeV)	$dy_i/y_i$ (%)	$d\sigma_i/\sigma_i$ (%)
7.9	12.5	12.6
8.0	10.8	10.5
8.1	9.3	9.1
8.2	8.0	7.1
8.3	7.0	6.3
8.4	6.3	5.8
8.5	5.6	5.2

This is the cross section dependence on energy

- Accounted for  $dN_{ij}$  due to energy error when calculating  $dy_i$

$$\approx \frac{\delta E}{i\Delta}$$

$$\left[ \frac{dN_{ij}}{N_{ij}} \right] = \begin{bmatrix} 0.100 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0.058 & 0.050 & 0 & 0 & 0 & 0 & 0 \\ 0.041 & 0.039 & 0.033 & 0 & 0 & 0 & 0 \\ 0.031 & 0.031 & 0.029 & 0.025 & 0 & 0 & 0 \\ 0.025 & 0.025 & 0.025 & 0.023 & 0.020 & 0 & 0 \\ 0.021 & 0.021 & 0.021 & 0.021 & 0.020 & 0.017 & 0 \\ 0.018 & 0.018 & 0.018 & 0.018 & 0.018 & 0.017 & 0.022 \end{bmatrix}$$

- With:

$$[B] = [N]^{-1}$$

$$[\sigma] = [B] \bullet [Y]$$

- Then:

$$[d\sigma^2] = [B] \bullet \left( [dY^2] + [dN^2] \bullet [\sigma^2] \right) \bullet [B]^T$$

- Where:

Note: Correlation Coefficient = 1

$$\text{var}(y_i, y_i) = (dy_i)^2$$

$$\text{cov}(y_i, y_j) = \rho_{ij} dy_i dy_j$$

$$[dY^2] = \begin{bmatrix} (dy_1)^2 & dy_1 dy_2 & \cdots & dy_1 dy_n \\ dy_2 dy_1 & (dy_2)^2 & \cdots & dy_n dy_n \\ \vdots & \ddots & \ddots & \vdots \\ dy_n dy_1 & dy_n dy_2 & \cdots & (dy_n)^2 \end{bmatrix}$$

No point-to-point systematic

$$[d\sigma^2] = \begin{bmatrix} d\sigma_1^2 & \text{cov}(\sigma_1, \sigma_2) & \cdots & \text{cov}(\sigma_1, \sigma_n) \\ \text{cov}(\sigma_2, \sigma_1) & d\sigma_2^2 & \cdots & \text{cov}(\sigma_2, \sigma_n) \\ \vdots & \ddots & \ddots & \vdots \\ \text{cov}(\sigma_n, \sigma_1) & \text{cov}(\sigma_n, \sigma_2) & \cdots & d\sigma_n^2 \end{bmatrix}$$

$$[dN^2] = \begin{bmatrix} (dN_{11})^2 & 0 & \cdots & 0 \\ (dN_{21})^2 & (dN_{22})^2 & \cdots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ (dN_{n1})^2 & (dN_{n2})^2 & \cdots & (dN_{nn})^2 \end{bmatrix}$$

$$[\sigma^2] = \begin{bmatrix} \sigma_1^2 & 0 & \cdots & 0 \\ 0 & \sigma_2^2 & \cdots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & \sigma_n^2 \end{bmatrix}$$

# SYSTEMATIC ERROR PROPAGATION

$$\begin{aligned} (d\sigma_i)^2 \cong & \frac{1}{N_{ii}^2} \left[ dy_i^2 - 2dy_i \sum_{j=1}^{i-1} N_{ij} d\sigma_j \right. \\ & + \sum_{j=1}^{i-1} (N_{ij} d\sigma_j)^2 + \sum_{k=1}^{i-1} \sum_{l=1}^{i-1} N_{ik} \text{cov}(\sigma_k, \sigma_l) N_{il} \\ & \left. + \sum_{j=1}^{i-1} (dN_{ij} \sigma_j)^2 + (dN_{ii} \sigma_i)^2 \right] \end{aligned}$$

No point-to-point systematic

$\text{cov}(y_i, y_j) \neq 0,$   
 $\text{cov}(\sigma_i, \sigma_j) \neq 0$

# OTHER SYSTEMATIC ERRORS

Beam Current, $\delta I/I$	3%
Photon Flux, $\delta\phi/\phi$	5%
Radiator Thickness, $\delta R/R$	3%
Bubble Chamber Thickness, $\delta T/T$	3%
Bubble Chamber Efficiency, $\varepsilon$	5%

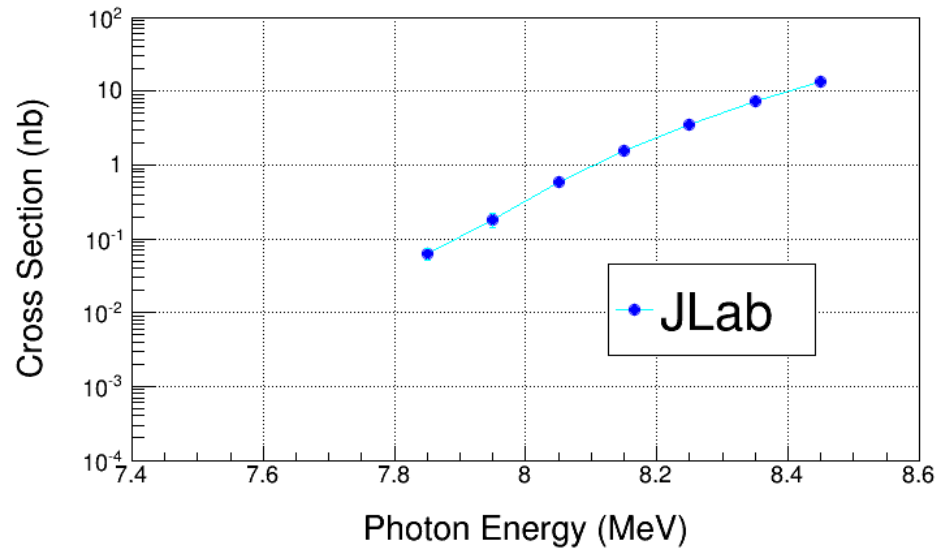
Simulation

- Then:

$$(dy_i)^2 = (dy_i(\delta E))^2 + \left[ \left( \frac{\delta I}{I} \right)^2 + \left( \frac{\delta R}{R} \right)^2 + \left( \frac{\delta T}{T} \right)^2 + \varepsilon^2 \right] y_i^2$$

$$(dN_{ij})^2 = \left( \frac{\delta\phi}{\phi} \right)^2 N_{ij}^2$$

Electron Beam K. E.	Cross Section (nb)	Stat Error (no bg, %)	Stat Error (with bg, %)
7.9	0.046	4.4	24.5
8.0	0.185	6.0	20.7
8.1	0.58	6.3	14.7
8.2	1.53	8.2	13.8
8.3	3.49	9.1	13.3
8.4	7.2	10.6	13.8
8.5	13.6	12.2	14.8



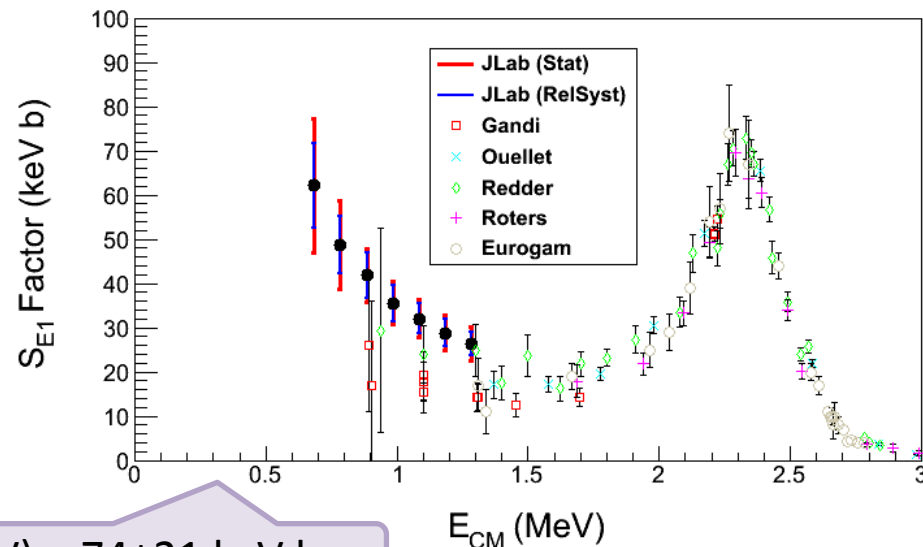
Electron Beam K. E.	Cross Section (nb)	Sys Error (Energy, %)	Sys Error (Total, %)
7.9	0.046	12.5	15.3
8.0	0.185	10.2	13.5
8.1	0.58	8.3	12.2
8.2	1.53	7.0	11.4
8.3	3.49	6.0	10.7
8.4	7.2	5.3	10.5
8.5	13.6	4.7	10.1

**Note:** Relative systematic errors do not get amplified in PL Unfolding

# THE $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ S-Factor

- Statistical Error: dominated by background subtraction from  $^{18}\text{O}(\gamma, \alpha)^{14}\text{C}$  (depletion = 5,000)

Electron Beam K. E.	Gamma Energy (MeV)	$E_{CM}$ (MeV)	Cross Section (nb)	$S_{E1}$ Factor (keV b)	Stat Error (%)	Sys Error (Total, %)
7.9	7.85	0.69	0.046	62.2	24.5	15.3
8.0	7.95	0.79	0.185	48.7	20.7	13.5
8.1	8.05	0.89	0.58	41.8	14.7	12.2
8.2	8.15	0.99	1.53	35.5	13.8	11.4
8.3	8.25	1.09	3.49	32.0	13.3	10.7
8.4	8.35	1.19	7.2	28.8	13.8	10.5
8.5	8.45	1.29	13.6	26.3	14.8	10.1



$$S_{E1}(300 \text{ keV}) = 74 \pm 21 \text{ keV b}$$



# BACKGROUNDS

## I. Background from oxygen isotopes and nitrogen in N<sub>2</sub>O:

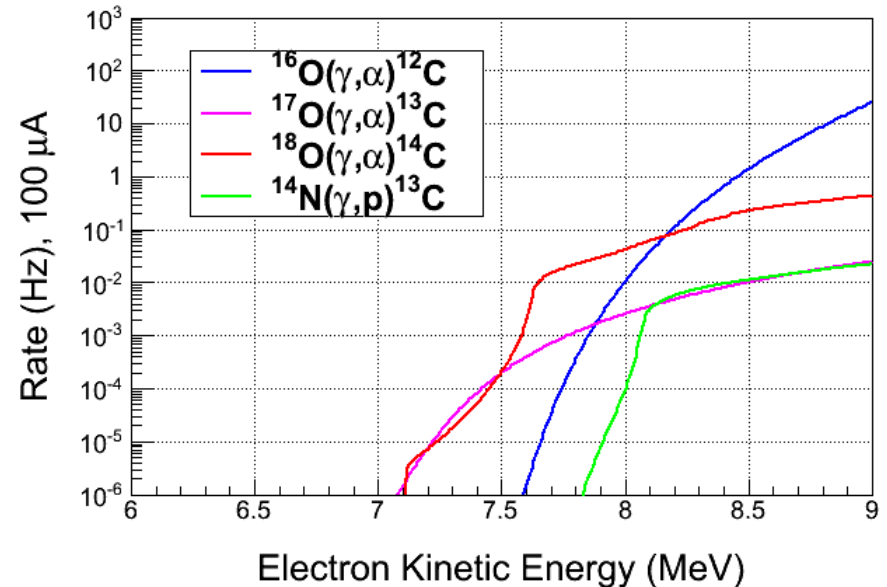
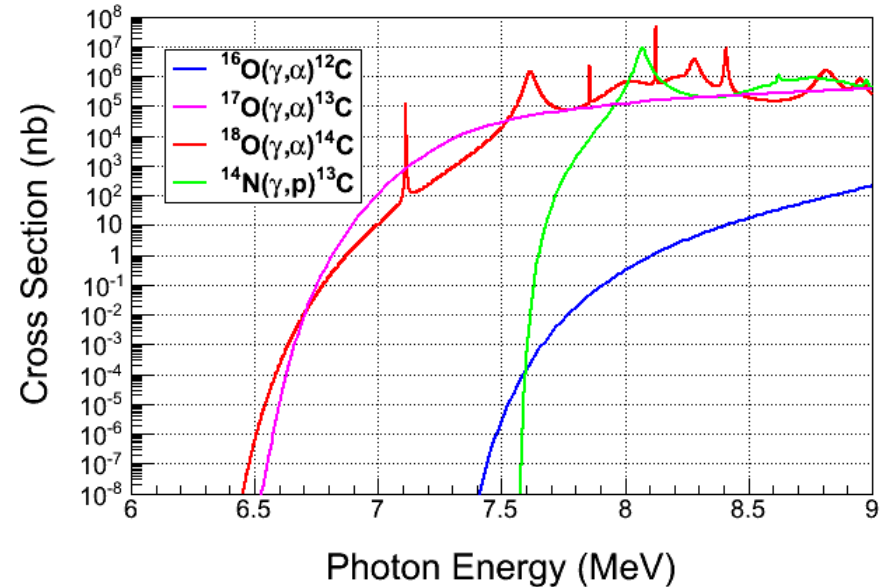
- $^{18}\text{O}(\gamma, \alpha)^{14}\text{C}$
- $^{17}\text{O}(\gamma, \alpha)^{13}\text{C}$
- $^{14}\text{N}(\gamma, p)^{13}\text{C}$

### ➤ Natural Abundance:

- I.  $^{17}\text{O}$ : 0.038%
- II.  $^{18}\text{O}$ : 0.205%

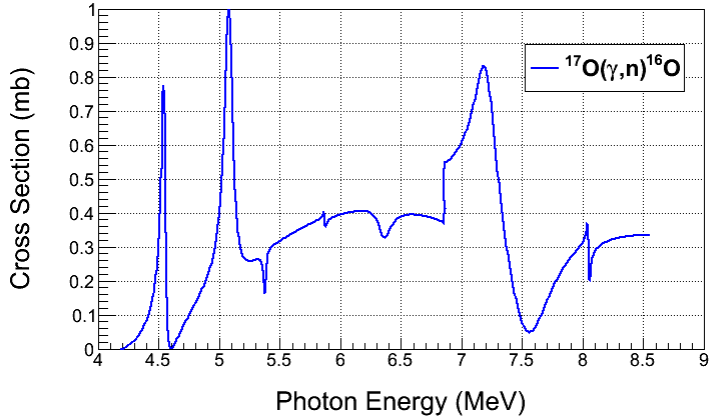
### ➤ Expected Rates:

- I.  $^{17}\text{O}(\gamma, \alpha)^{13}\text{C}$ , depletion=5,000
- II.  $^{18}\text{O}(\gamma, \alpha)^{14}\text{C}$ , depletion=5,000
- III.  $^{14}\text{N}(\gamma, p)^{13}\text{C}$ , detection eff.=  $10^{-8}$



## II. Background from:

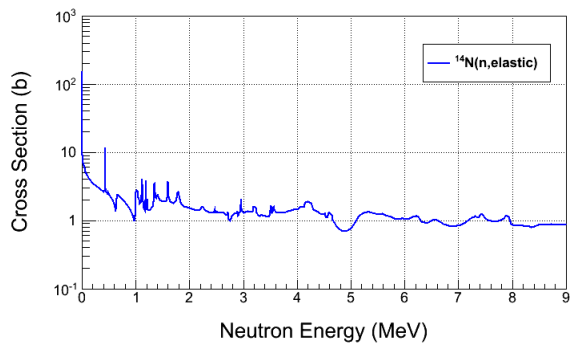
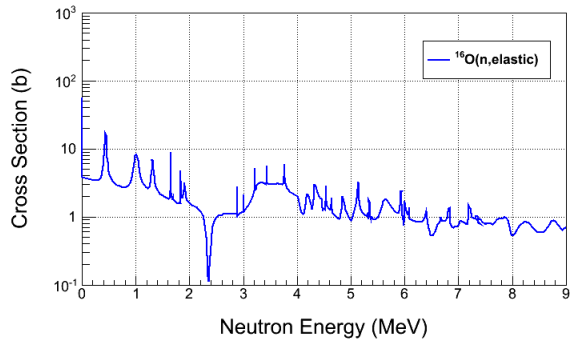
- $^{17}\text{O}(\gamma,n)^{16}\text{O}$  and secondary (n,n) neutron–nucleus elastic scattering



## III. Cosmic–ray background:

- $\mu^\pm$ –nuclear
- neutron–nuclear elastic scattering

➤ Reject neutron background using the acoustic signal (500 factor)



# ION ENERGY DISTRIBUTIONS

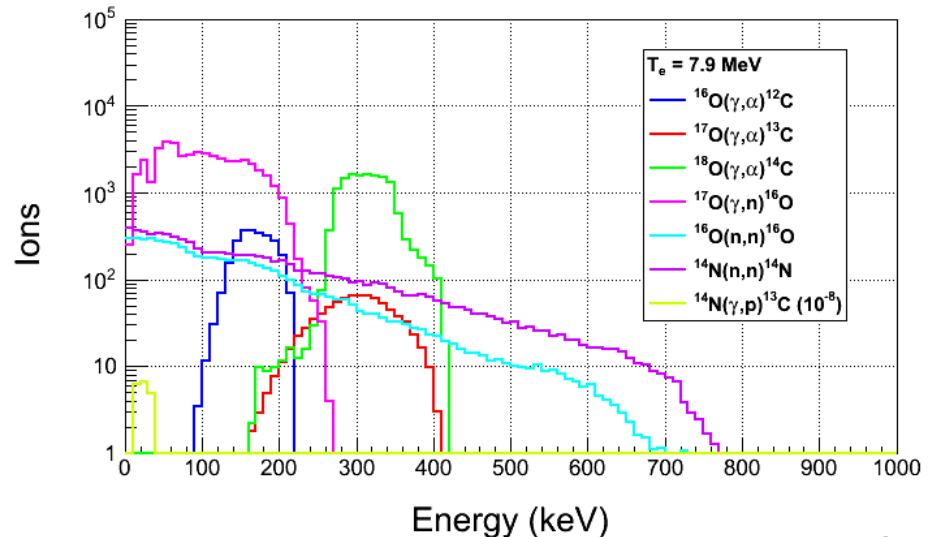
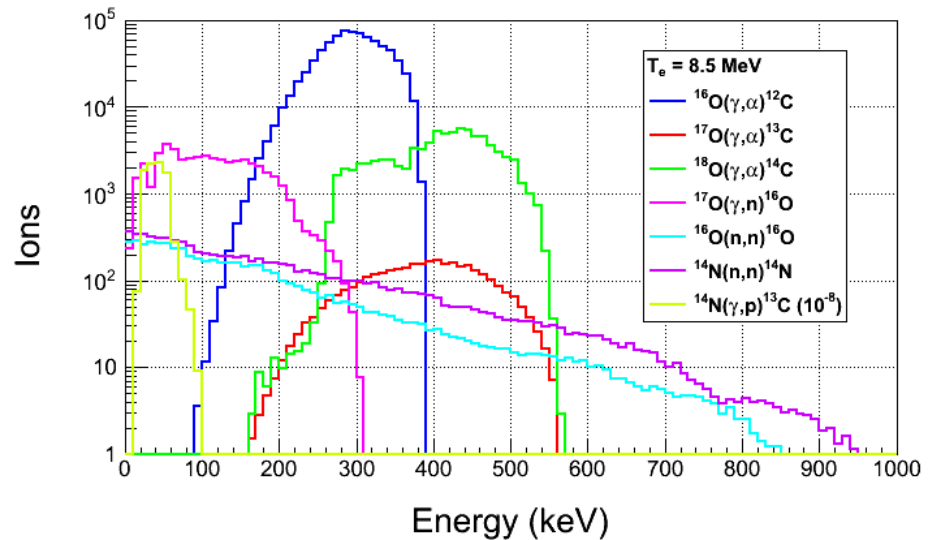
➤ Suppress background  
with Bubble Chamber threshold

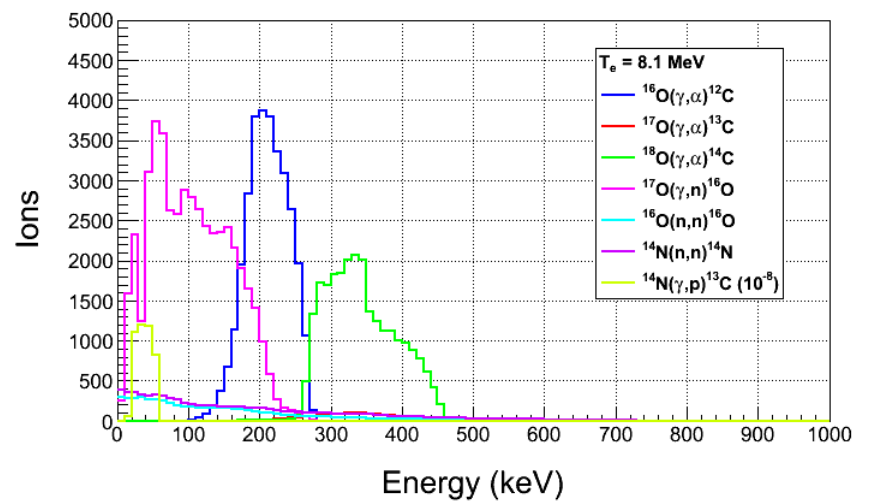
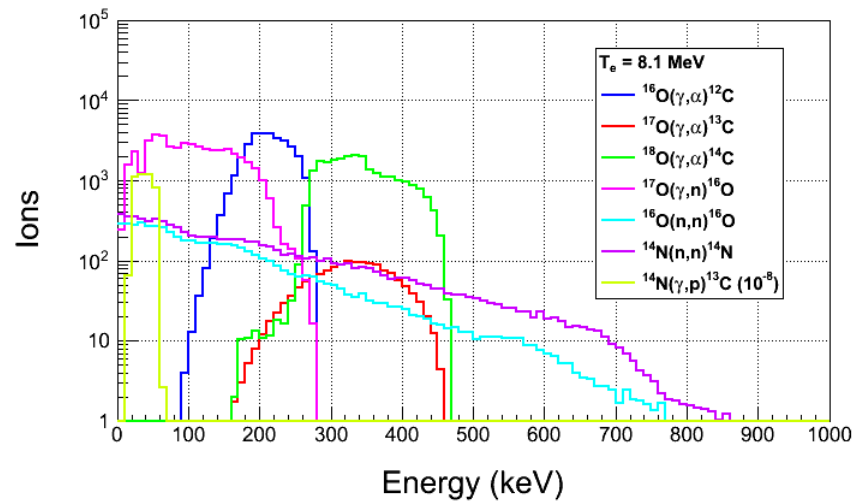
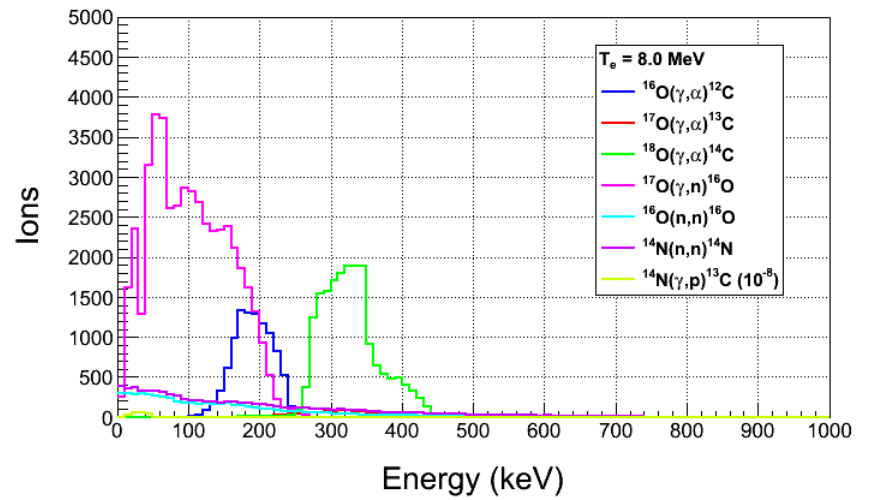
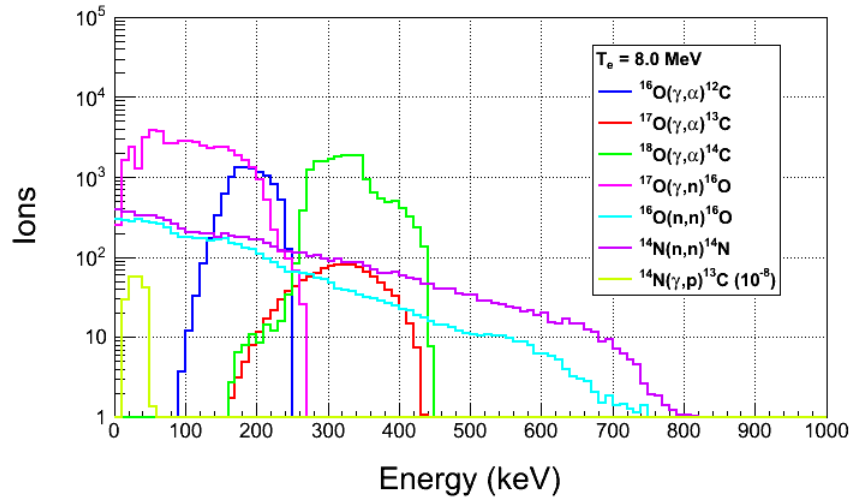
➤ Calculated with Depletion:

- I.  $^{17}\text{O}$  depletion = 5,000
- II.  $^{18}\text{O}$  depletion = 5,000

➤ Threshold Efficiency (function of superheat):

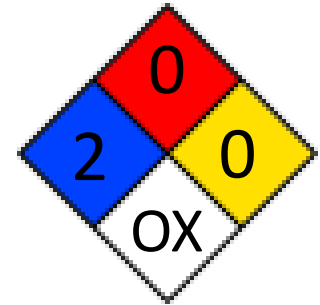
Particle	Efficiency
$e^\pm$	$<10^{-11}$
$\gamma$	$<10^{-11}$
$(\gamma, n)$	$2 \times 10^{-3}$





# SAFETY

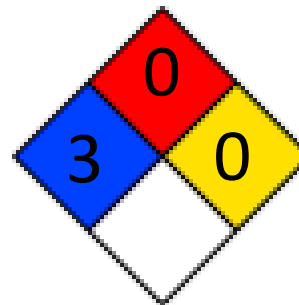
- Super heated liquid  $N_2O$ , Nitrous oxide (laughing gas)
  - I. At room temperature, it is a colorless, non-flammable gas, with a slightly sweet odor and taste



- High pressure system:
  - I. Design Authority: Dave Meekins
  - II. T =
  - III. P =

- Buffer liquid: Mercury

- I. Closed system
- II. Volume: 135 mL



# SUMMARY AND OUTLOOK

- Test N<sub>2</sub>O Bubble Chamber at HIGS (February 2014)
- Perform  $^{18}\text{O}(\gamma,\alpha)^{14}\text{C}$  and  $^{17}\text{O}(\gamma,\alpha)^{13}\text{C}$  experiments at HIGS (Summer 2014)
- Test Bubble Chamber at JLab with Bremsstrahlung beam (October 2014)
- If successful, run depleted N<sub>2</sub>O bubble chamber at JLab  $^{16}\text{O}(\gamma,\alpha)^{12}\text{C}$
  
- Bubble Chamber issues:
  - Piezo–electric acoustical signal
  - Deadtime study (now  $\tau \pm d\tau = 10.0 \pm 0.9$  s)
  - Measure O-isotopes depletion
  
- Background tests:
  - Measure cosmic–ray background
  - Study chamber efficiency vs. superheat

# BACKUP SLIDES



# COST ESTIMATE

- I. New beamline components:
  - I. New Dipole Magnet and Hall Probe
  - II. 2 Super Harps
  - III. Fast Valve
- II. Summary of labor cost by group:

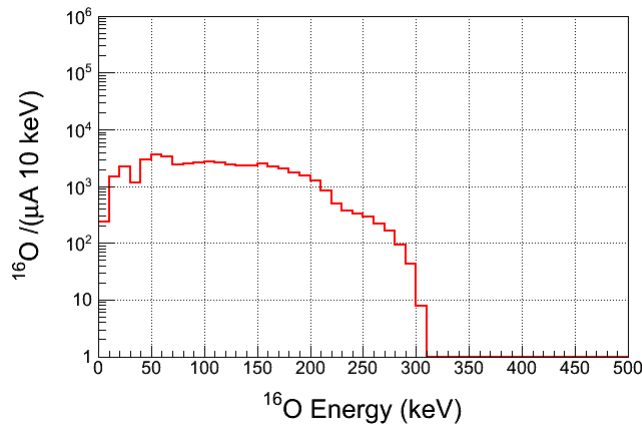
Group	Labor
Survey & Alignment	3 wks x 2
Magnet Test	1 wk x 2
Engineering Design	16 wks
Software	3 wks x 2
EES	6 wk x 2
EH&Q	4 wks

Item	Material Procurement	Shop	Labor
New Dipole Magnet	Dipole Magnet (\$8,000) Hall Probe System (\$10,000)		Design (2 week) Mapping (1 week) EESDC (1 week) Alignment (2 days)
New Beamline	2 Super Harps (20,000) Fast Valve (\$23,000)	Pipes + Pedestals (\$20,000)	Design (6 weeks) Alignment (1 week) Software (6 weeks) EES (6 weeks)
Radiator (cooled ladder, FSD)	0.02 and 0.10 mm Cu foils (\$2,000)	\$4,000	Design (2 week) Alignment (2 days)
Sweep Dipole			
Electron Dump	Pure Cu (\$5,000)	Dump + Pipes (\$15,000)	Design (4 weeks) Alignment (1 day)
Cu Collimator	Pure Cu (\$5,000)	Collimator + Stand (\$5,000)	Design (1 week) Alignment (1 day)
Photon Dump & Stand	Pure Al (\$3,000)	\$4,000	Design (1 week) Alignment (1 day)
Safety Review			4 weeks
Install			6 weeks
Bubble Chamber			Alignment (1 week)
<b>Total</b>	<b>\$76,000</b>	<b>\$48,000</b>	<b>\$80,000</b>
Indirect G&A (55.65%)	\$42,300	\$26,400	\$42,500
Indirect Stat & Fringe (57.15%)			\$45,700
<b>Total</b>	<b>\$118,300</b>	<b>\$74,400</b>	<b>\$168,200</b>

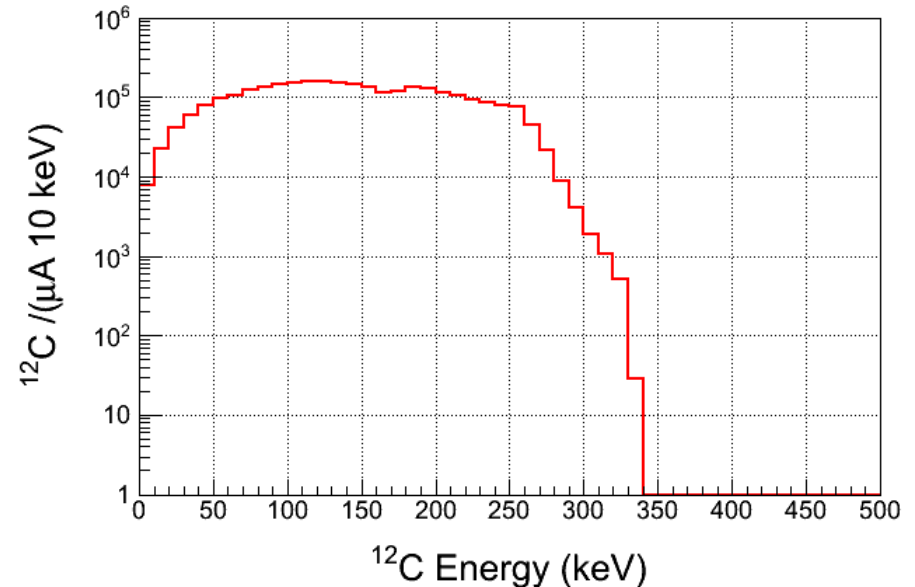
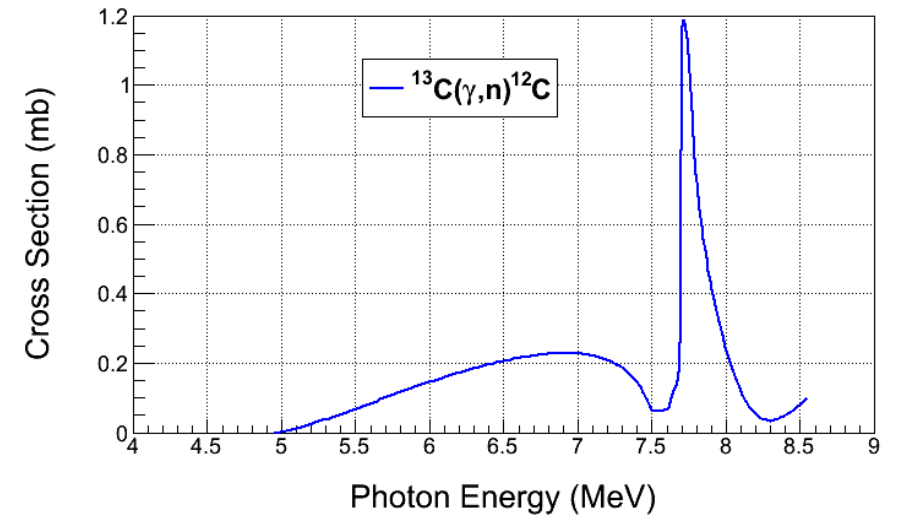
# CO<sub>2</sub> SUPERHEATED LIQUID?

- Natural Abundance: <sup>13</sup>C: 1.07%
- Depletion: <sup>13</sup>C depletion=1,000
- <sup>13</sup>C(γ,n)<sup>12</sup>C Background

For comparison, <sup>17</sup>O(γ,n)<sup>16</sup>O



- <sup>12</sup>C(γ,2α)α Background



# WATER SUPERHEATED LIQUID?

- Etching of glass vessel by superheated H<sub>2</sub>O
- T = 250°C
- P = 68 atm



