Beam Cooling

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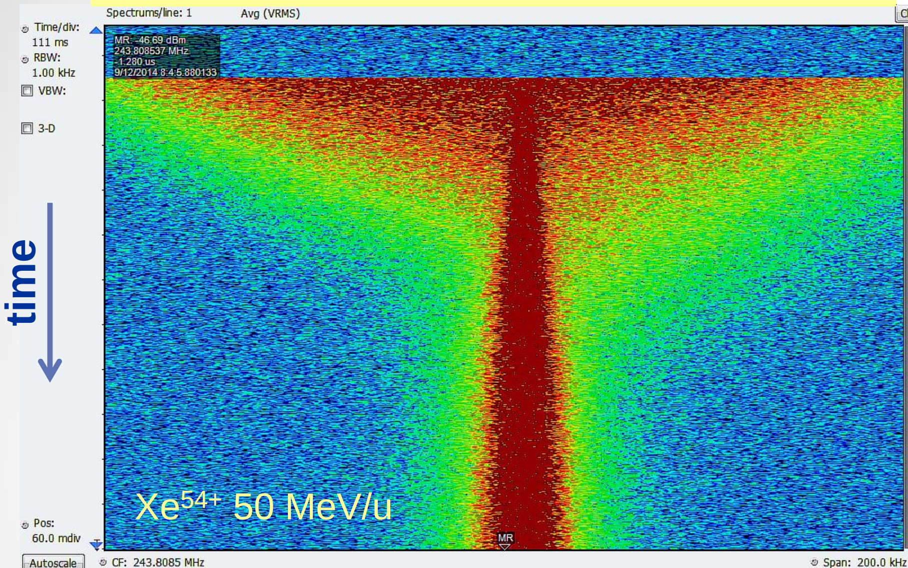
Cooling

longitudinal (momentum) cooling

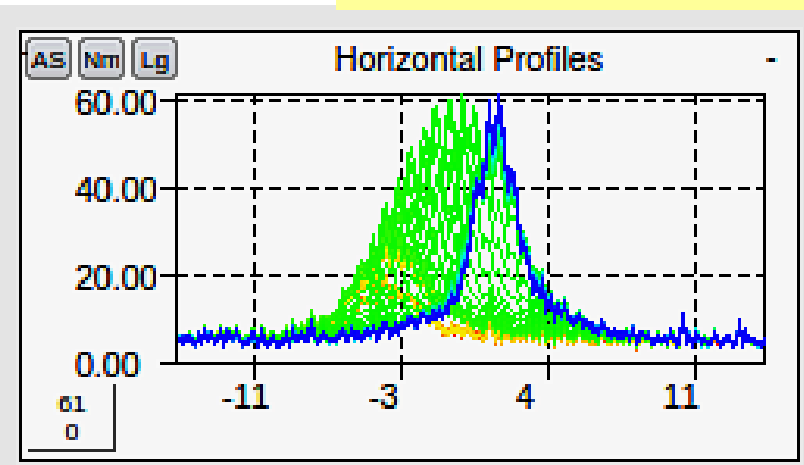


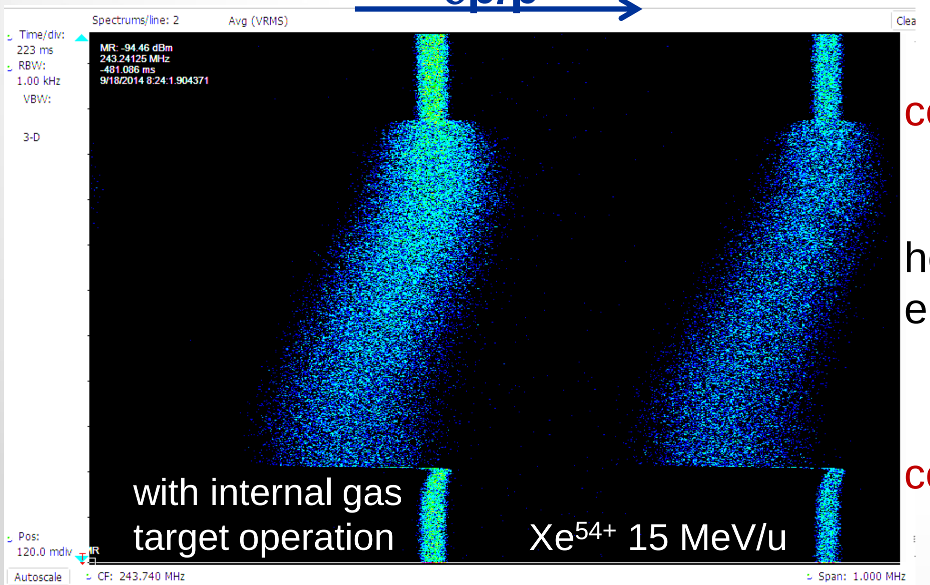
injection into storage ring

time

δp/p

transverse cooling





cooling **off**

heating (spread) and energy loss (shift)

cooling **on**

cooling:
good energy definition
small beam size
⇒ highest precision

Beam Cooling

Introduction

1. Electron Cooling

2. Ionization Cooling

3. Laser Cooling

4. Stochastic Cooling

Beam Cooling

Beam cooling is synonymous for a reduction of beam temperature

Temperature is equivalent to terms as phase space volume, emittance and momentum spread

Beam Cooling processes are not following Liouville‘s Theorem:

`in a system where the particle motion is controlled by external conservative forces the phase space density is conserved´

(This neglect interactions between beam particles.)

Beam cooling techniques are non-Liouvillean processes which violate the assumption of a conservative force.

e.g. interaction of the beam particles with other particles (electrons, photons, matter)

Cooling Force

Generic (simplest case of a) ooling Force:

$$F_{x,y,s} = -\alpha_{x,y,s} v_{x,y,s}$$

$v_{x,y,s}$ velocity in the rest frame of the beam

non conservative, cannot be described by a Hamiltonian

For a 2D subspace distribution function $f(z, z', t)$

$$F_z = -\alpha_z v_z \qquad z = x, y, s \qquad v_z = v_0 \cdot z'$$

$$\frac{df(z, z', t)}{dt} = -\lambda_z f(z, z', t) \qquad \lambda_z \text{ cooling (damping) rate}$$

in a circular accelerator:

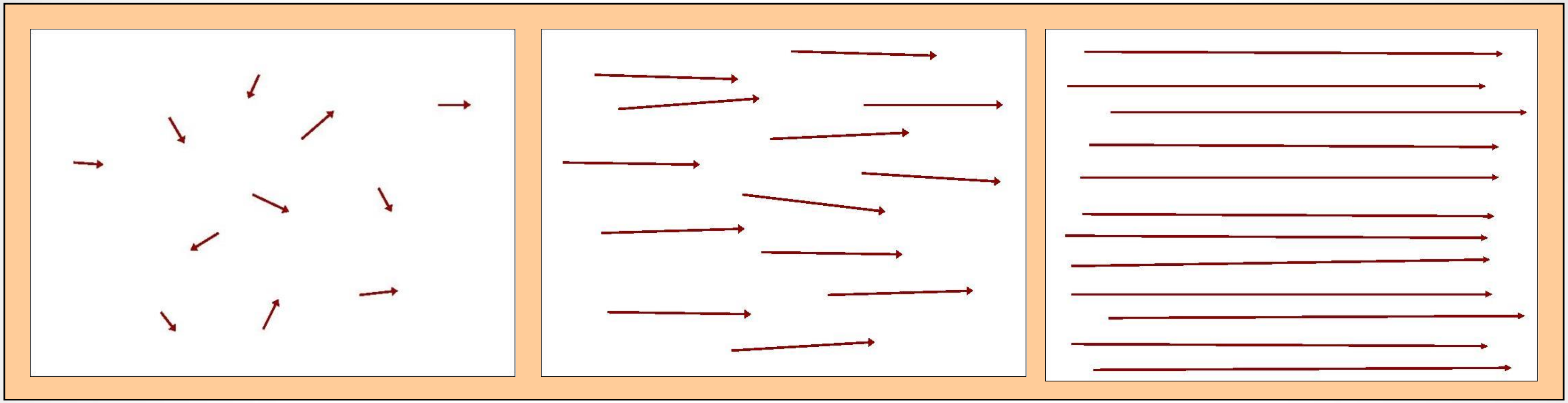
Transverse (emittance) cooling rate $\epsilon_{x,y}(t_0 + t) = \epsilon_{x,y}(t_0)\, e^{-\lambda_{x,y} t}$

Longitudinal (momentum spread) cooling rate $\frac{\delta p_\parallel}{p_0}(t_0 + t) = \frac{\delta p_\parallel}{p_0}(t_0)\, e^{-\lambda_\parallel t}$

Beam Temperature

Where does the beam temperature originate from?

The beam particles are generated in a 'hot' source



at rest (source) **at low energy** **at high energy**

In a standard accelerator the beam temperature is not reduced (thermal motion is superimposed the average motion after acceleration)

but: many processes can heat up the beam

e.g. heating by mismatch, space charge, intrabeam scattering, internal targets, residual gas, external noise

Beam Temperature Definition

Longitudinal beam temperature

$$\frac{1}{2}k_B T_{\|} = \frac{1}{2}mv_{\|}^2 = \frac{1}{2}mc^2\beta^2(\frac{\delta p_{\|}}{p})^2$$

Transverse beam temperature

$$\frac{1}{2}k_B T_{\perp} = \frac{1}{2}mv_{\perp}^2 = \frac{1}{2}mc^2\beta^2\gamma^2\theta_{\perp}^2$$

$$\theta_{\perp} = \frac{v_{\perp}}{\beta c}, \qquad \theta_{\perp}(s) = \sqrt{\frac{\epsilon}{\beta_{\perp}(s)}}$$

Distribution function

$$f(v_{\perp}, v_{\|}) \propto \exp(-\frac{mv_{\perp}^2}{2k_B T_{\perp}} - \frac{mv_{\|}^2}{2k_B T_{\|}})$$

Particle beams can be anisotropic: $k_B T_{\|} \neq k_B T_{\perp}$

e.g. due to laser cooling or the distribution of the electron beam

Don‘t confuse: beam energy $\leftrightarrow$ beam temperature

(e.g. a beam of energy 100 GeV can have a temperature of 1 eV)

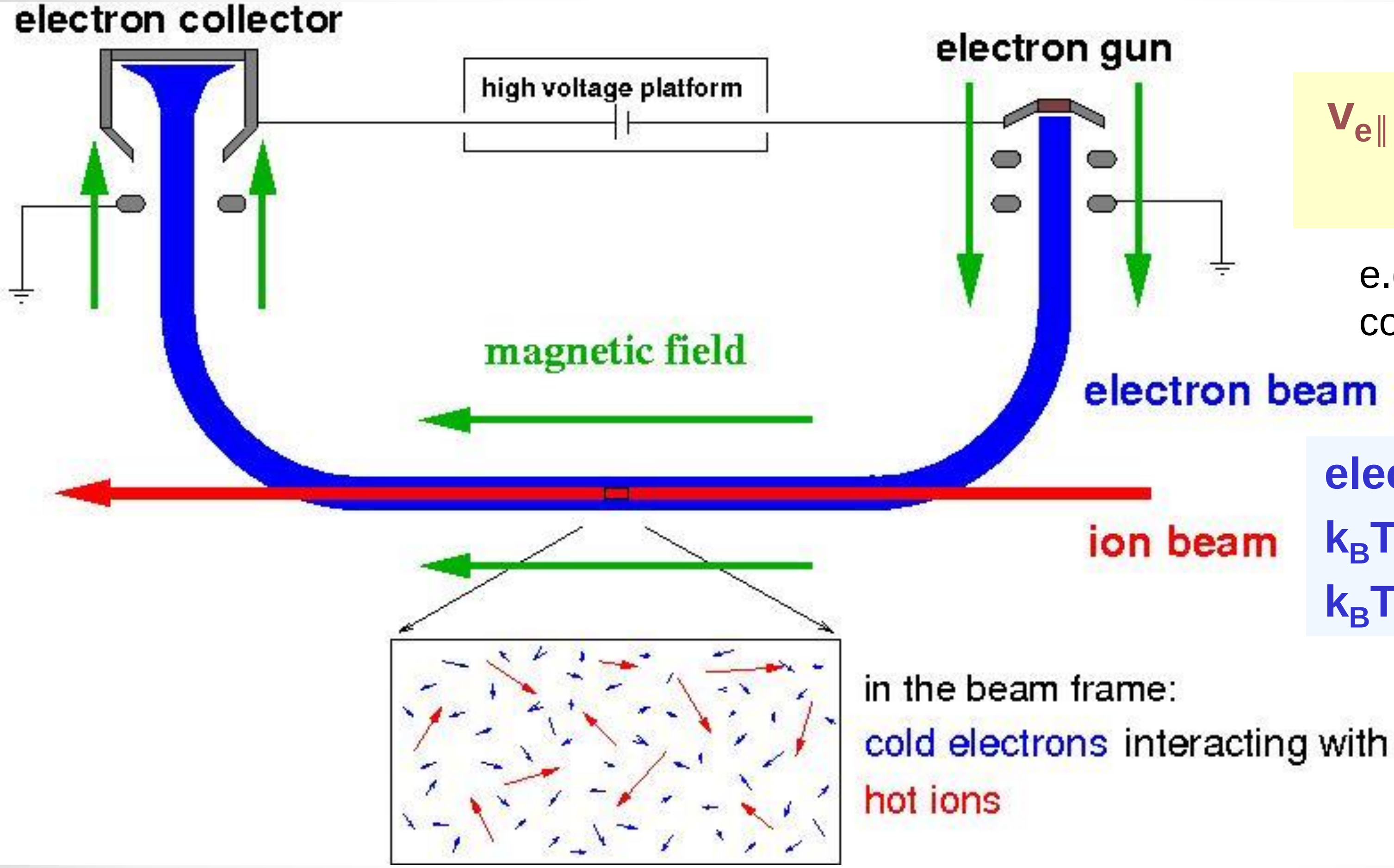
Benefits of Beam Cooling

- Improved beam quality
  - Precision experiments
  - Luminosity increase

- Compensation of heating
  - Experiments with internal target
  - Colliding beams

- Intensity increase by accumulation
  - Weak beams from source can be enhanced
  - Secondary beams (antiprotons, rare isotopes)

1. Electron Cooling



$v_{e\parallel} = \beta_e c = \beta_i c = v_{i\parallel}$

$E_e = m_e/M_i \cdot E_i$

e.g.: 220 keV electrons
cool 400 MeV/u ions

electron temperature

$k_B T_\perp \approx 0.1$ eV

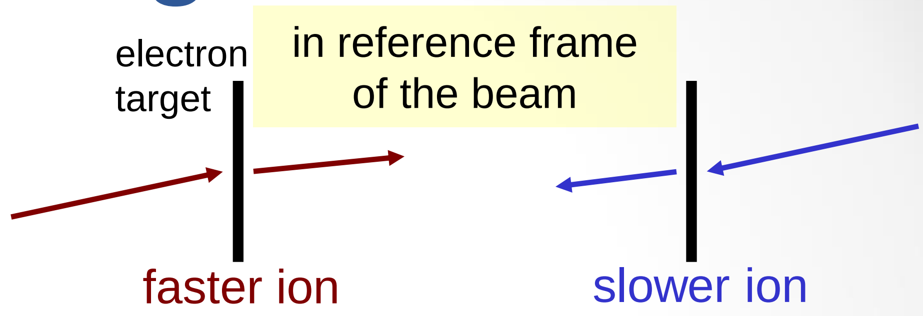
$k_B T_\parallel \approx 0.1 - 1$ meV

superposition of a cold intense electron beam with the same velocity

momentum transfer by Coulomb collisions
cooling force results from energy loss in the co-moving gas of free electrons

Simple Derivation of the Electron Cooling Force

Analogy: energy loss in matter
(electrons in the shell)

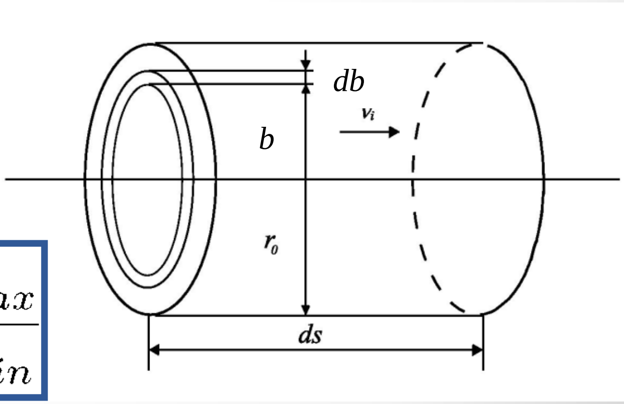


Rutherford scattering: $2\ tan(\frac{\theta}{2}) = \frac{2Z_1Z_2e^2}{4\pi\epsilon_0\Delta pvb}$ $\quad Z_1 = Q\ (ion),\ \ Z_2 = -1\ (electron)$

Energy transfer: $\Delta E(b) = \frac{(\Delta p)^2}{2m_e} \simeq \frac{2Q^2e^4}{(4\pi\epsilon_0)^2m_ev^2}\frac{1}{b^2} \quad (for\ \ b \gg b_{min})$

Minimum impact parameter: $b_{min} = \frac{Qe^2}{(4\pi\epsilon_0)^2m_ev^2}$

from: $\Delta E(b_{min}) = \Delta E_{max} \simeq 2m_ev^2$



Energy loss:

$$-\frac{dE}{dx} = 2\pi\int_{b_{min}}^{b_{max}} bn_e\Delta E\,db = \frac{4\pi Q^2e^4}{(4\pi\epsilon_0)^2m_ev^2}n_e\ln\frac{b_{max}}{b_{min}}$$

Coulomb logarithm $L_C=\ln\,(b_{max}/b_{min})$ ≈10 (typical value)

Characteristics of the Electron Cooling Force

$$\vec{F}(\vec{v_i}) = -\frac{4\pi Q^2 e^4 n_e}{(4\pi\epsilon_0)^2 m_e} \int L_C(\vec{v}_{rel}) f(\vec{v_e}) \frac{\vec{v}_{rel}}{v_{rel}^3} d^3\vec{v_e}$$

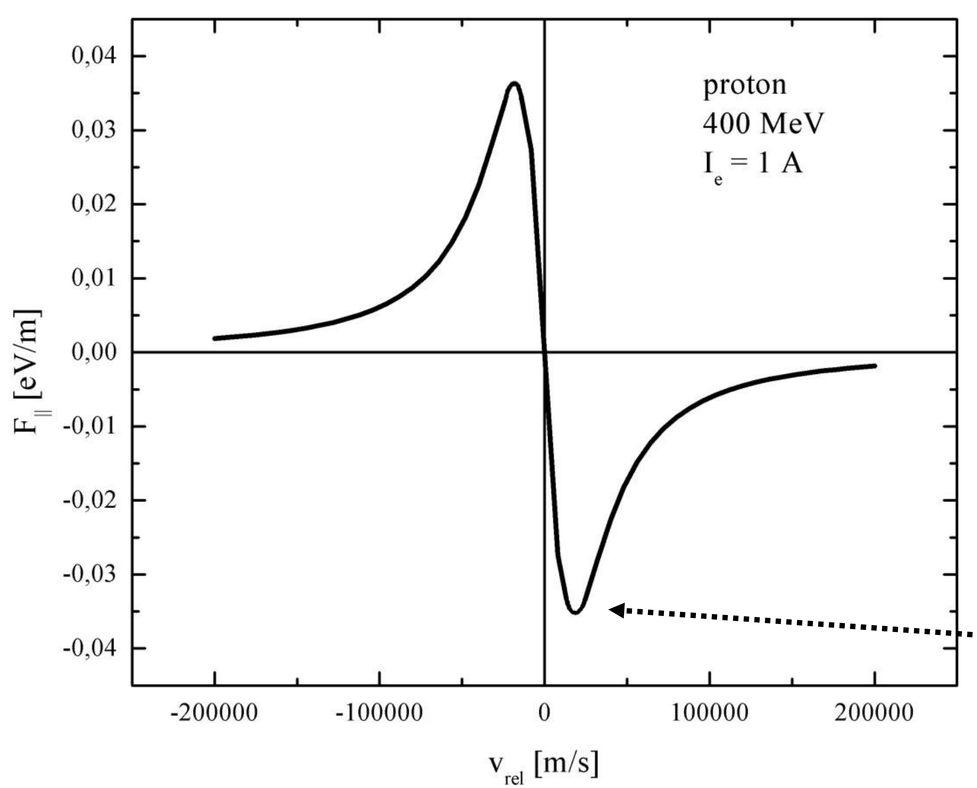
$$\vec{v}_{rel} = \vec{v_i} - \vec{v_e}$$

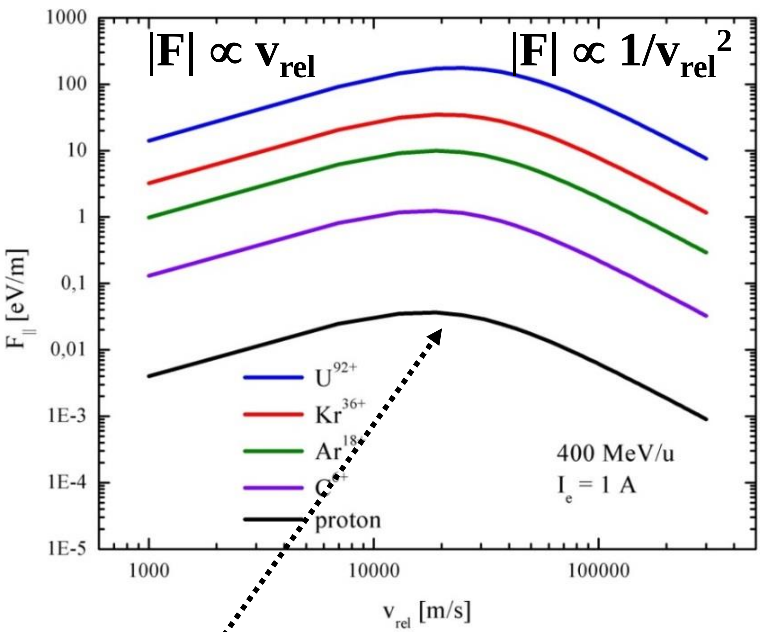
cooling force F

for small relative velocity: $\propto v_{rel}$

for large relative velocity: $\propto v_{rel}^{-2}$

increases with charge: $\propto Q^2$





maximum of cooling force at effective electron temperature

Electron Cooling Time

first estimate: (Budker 1967) $\tau = \frac{3}{8\sqrt{2\pi} n_e Q^2 r_e r_i c L_C}\left(\frac{k_B T_e}{m_e c^2} + \frac{k_B T_i}{m_i c^2}\right)^{3/2}$

for large relative velocities

cooling time $\tau_z \propto \frac{A}{Q^2}\frac{1}{n_e \eta}\beta^3\gamma^5\theta_z^3$ $\begin{cases} \theta_{x,y} = \frac{v_{x,y}}{\gamma\beta c} \\ \theta_{\parallel} = \frac{v_{\parallel}}{\gamma\beta c} \end{cases}$

cooling rate (τ^{-1}):

- slow for hot beams $\propto \theta^3$
- decreases with energy $\propto \gamma^{-2}$ ($\beta\cdot\gamma\cdot\theta$ is conserved)
- linear dependence on electron beam intensity n_e and cooler length $\eta = L_{ec}/C$
- favorable for highly charged ions Q^2/A
- independent of hadron beam intensity

for small relative velocities

cooling rate is constant and maximum at small relative velocity

$F \propto v_{rel} \Rightarrow \tau = \Delta t = p_{rel}/F = \text{constant}$

Models of the Electron Cooling Force

- binary collision model

description of the cooling process by successive collisions of two particles and integration over all interactions
analytic expressions become very involved, various regimes (multitude of Coulomb logarithms)

- dielectric model

interaction of the ion with a continuous electron plasma (scattering off of plasma waves)
fails for small relative velocities and high ion charge

- an empiric formula (Parkhomchuk) derived from experiments:

$$\vec{F} = -4\frac{n_e}{m_e}\frac{(Qe^2)^2}{(4\pi\epsilon_0)^2}\ln\left(\frac{b_{max}+b_{min}+r_c}{b_{min}+r_c}\right)\frac{\vec{v}_{ion}}{(v_{ion}^2+v_{eff}^2)^{3/2}}$$

$$b_{min} = \frac{Qe^2/4\pi\epsilon_0}{m_e v_{ion}^2}; \quad b_{max} = \frac{v_{ion}}{min(\omega_{pe}, 1/T_{cool})}, \quad v_{eff}^2 = v_{e,\parallel}^2 + v_{e,\perp}^2$$

Electron Beam Properties

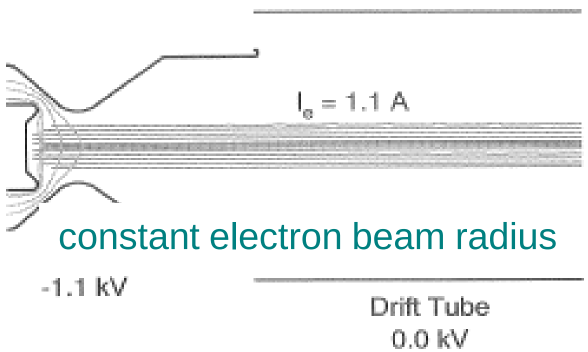
electron beam temperature

transverse $k_B T_\perp = k_B T_{cat}$, with transverse expansion ($\propto B_c/B_{gun}$)

longitudinal $k_B T_{//} = (k_B T_{cat})^2/4E_0 << k_B T_\perp$ lower limit : $k_B T_\parallel \geq 2e \frac{n_e^{1/3}}{4\pi\epsilon_0}$

typical values: $k_B T_\perp \approx 0.1$ eV (1100 K), $k_B T_{//} \approx 0.1$ - 1 meV

Gun

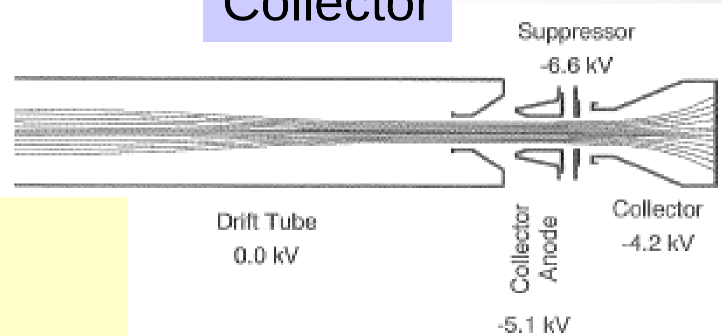


constant electron beam radius

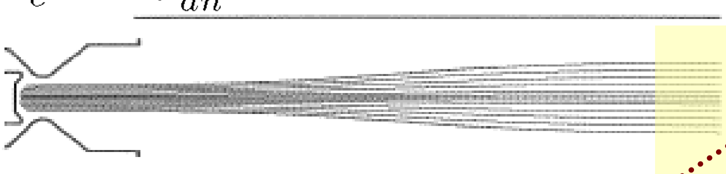
electron beam confined by longitudinal magnetic field (from gun to collector)

Cooling Section

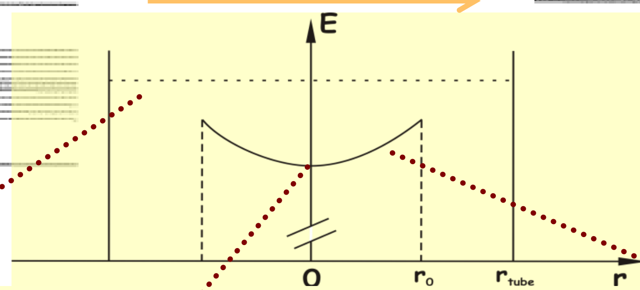
Collector



$I_e = P U_{an}^{3/2}$



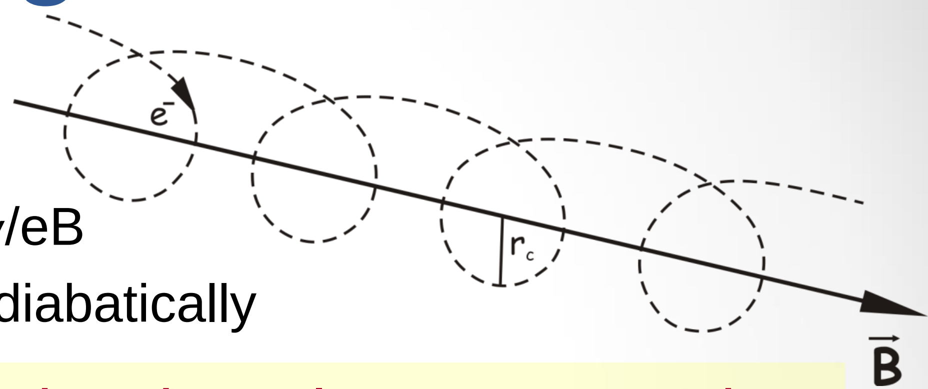
transversely expanded electron beam



radial variation of electron energy due to space charge:

$$E(r) = eU_{cat} - \underline{n_e} \pi r_0^2 r_e m_e c^2 [1 + 2\ln(r_{tube}/r_0)] + \underline{n_e} \pi r_e m_e c^2 r^2$$

Electron Motion in Longitudinal Magnetic Field



single particle cyclotron motion

cyclotron frequency $\omega_c = eB/\gamma m_e$

cyclotron radius $r_c = v_\perp/\omega_c = (k_B T_\perp m_e)^{1/2}\ \gamma/eB$

electrons follow the magnetic field line adiabatically

important consequence: for interaction times long compared to the cyclotron period the ion does not sense the transverse electron temperature $\Rightarrow$ **magnetized cooling ($T_{eff} \approx T_\parallel << T_\perp$)**

electron beam space charge:

transverse electric field + B-field $\Rightarrow$ azimuthal drift

$$v_{azi} = r\omega_{azi} = r\frac{2\pi r_e n_e c^2}{\gamma\omega_c}$$

$\Rightarrow$ electron and ion beam should be well centered

Favorable for optimum cooling (small transverse relative velocity):

- high parallelism of magnetic field lines $\Delta B_\perp/B_0$
- large beta function (small divergence) in cooling section

Imperfections and Limiting Effects in Electron Cooling

technical issues:

ripple of accelerating voltage

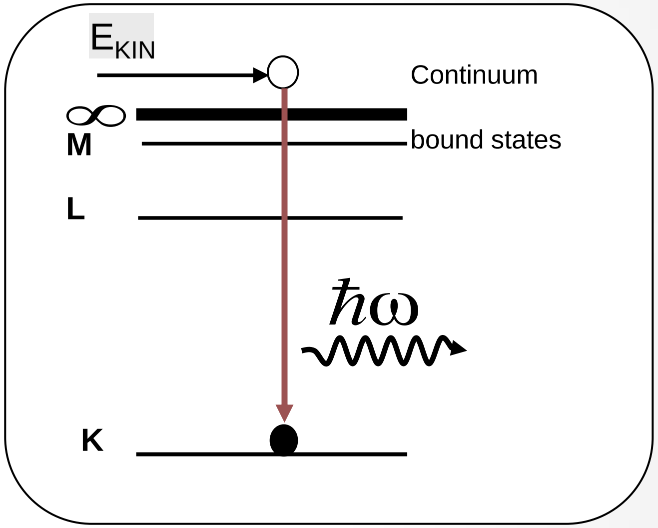
magnetic field imperfections

beam misalignment

space charge of electron beam and compensation

physical limitation:

Radiative Electron Capture (REC)



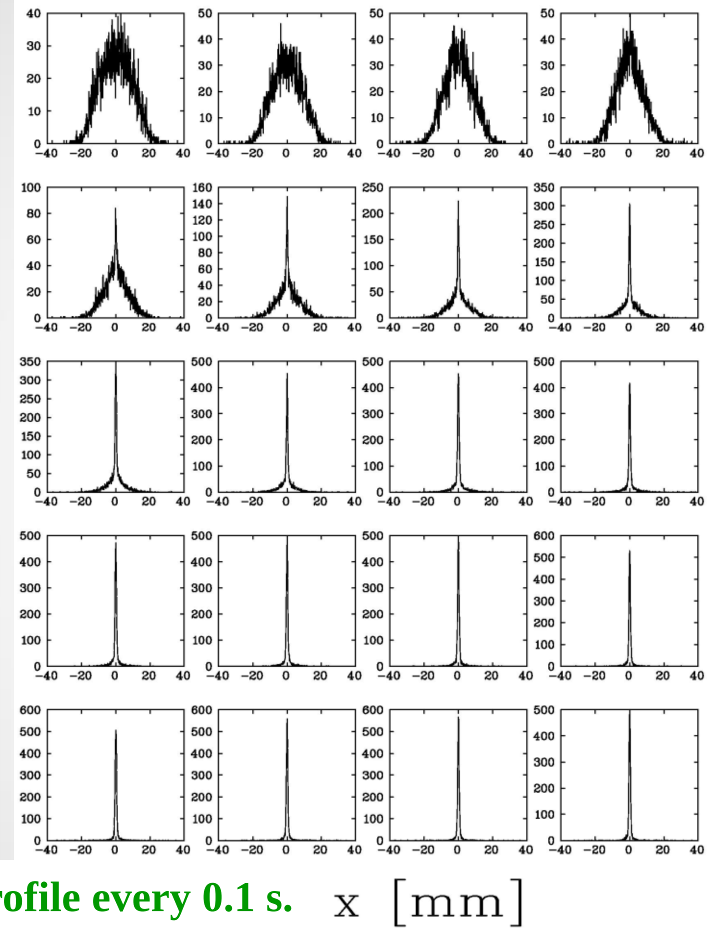
losses by recombination (REC)

loss rate $\tau^{-1} = \gamma^{-2} \alpha_{REC} n_e \eta$

$$\alpha_{REC} = \frac{1.92 \times 10^{-13} Q^2}{\sqrt{k_B T}} \left(\ln \frac{5.66 Q}{\sqrt{k_B T}} + 0.196 \left(\frac{k_B T}{Q^2}\right)^{1/3} \right) [cm^3 s^{-1}]$$

Examples of Electron Cooling

fast transverse cooling at TSR, Heidelberg



profile every 0.1 s.

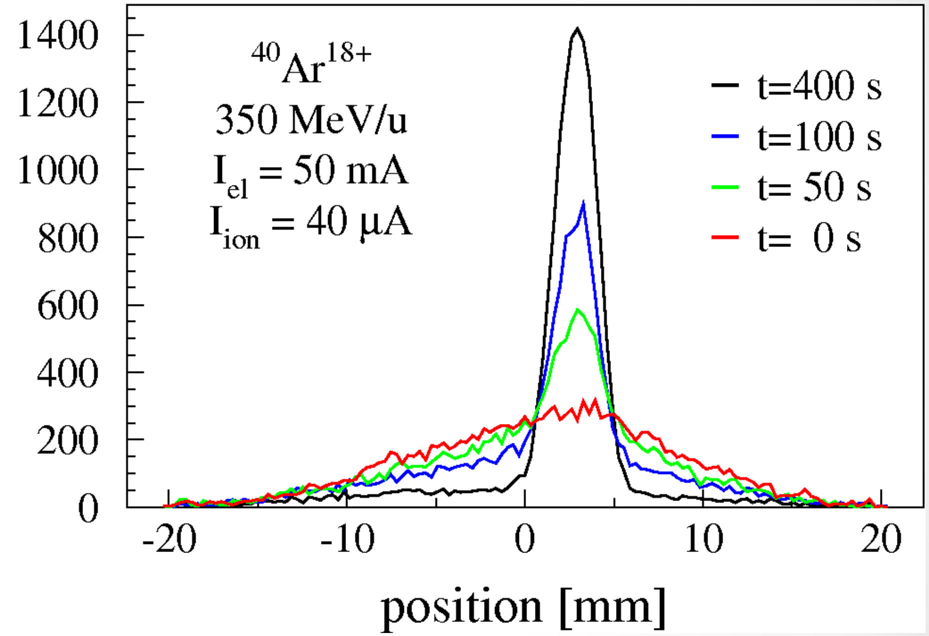
cooling of 6.1 MeV/u C^{6+} ions

0.24 A, 3.4 keV electron beam

n_e = 1.56 ×10^7 cm^{-3}

measured with residual gas ionization beam profile monitor

transverse cooling at ESR, Darmstadt



cooling of 350 MeV/u Ar^{18+} ions

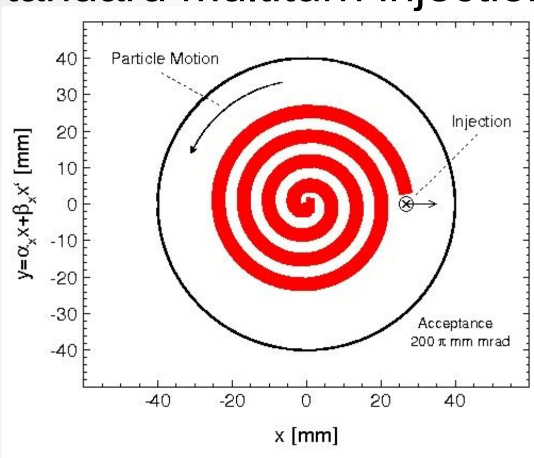
0.05 A, 192 keV electron beam

n_e = 0.8 ×10^6 cm^{-3}

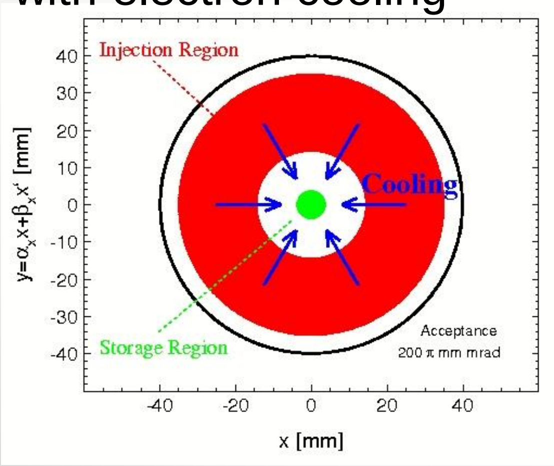
note! time scale cooling times vary

Accumulation of Heavy Ions by Electron Cooling

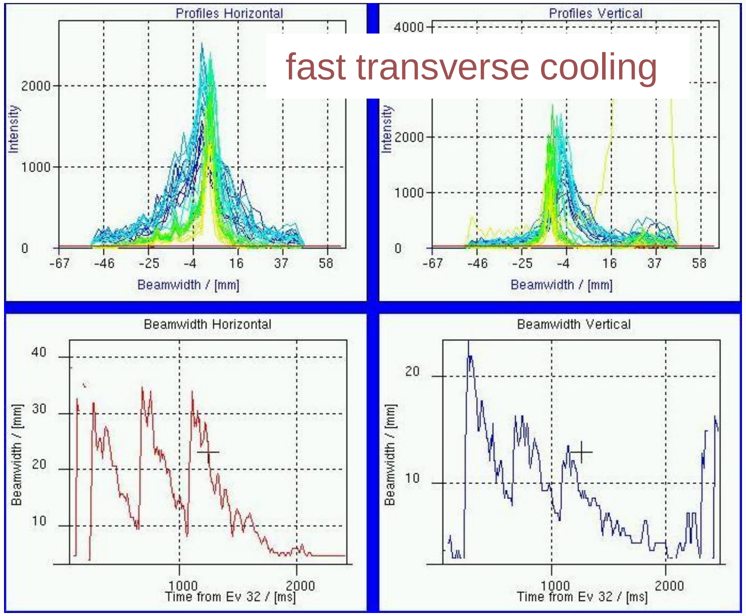
standard multiturn injection



fast accumulation by repeated multiturn injection with electron cooling

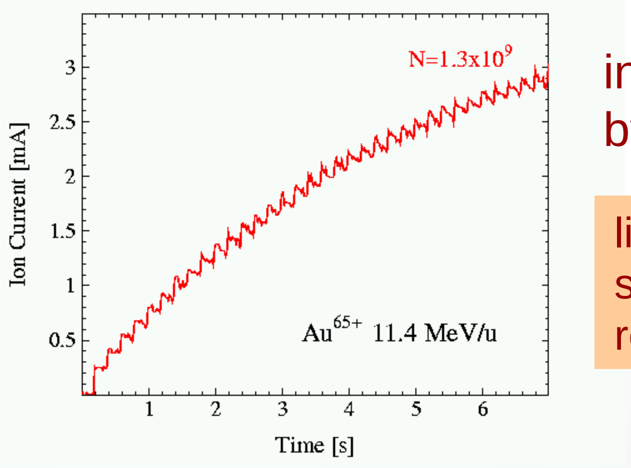


horizontal **vertical**



profile

beam size



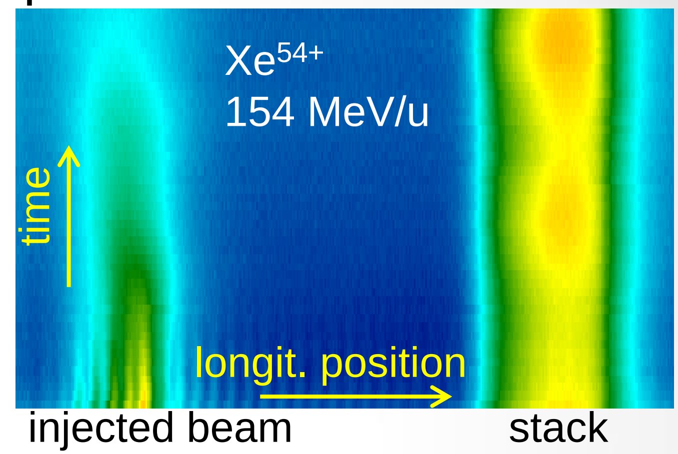
intensity increase in 5 s by a factor of ≈ 10

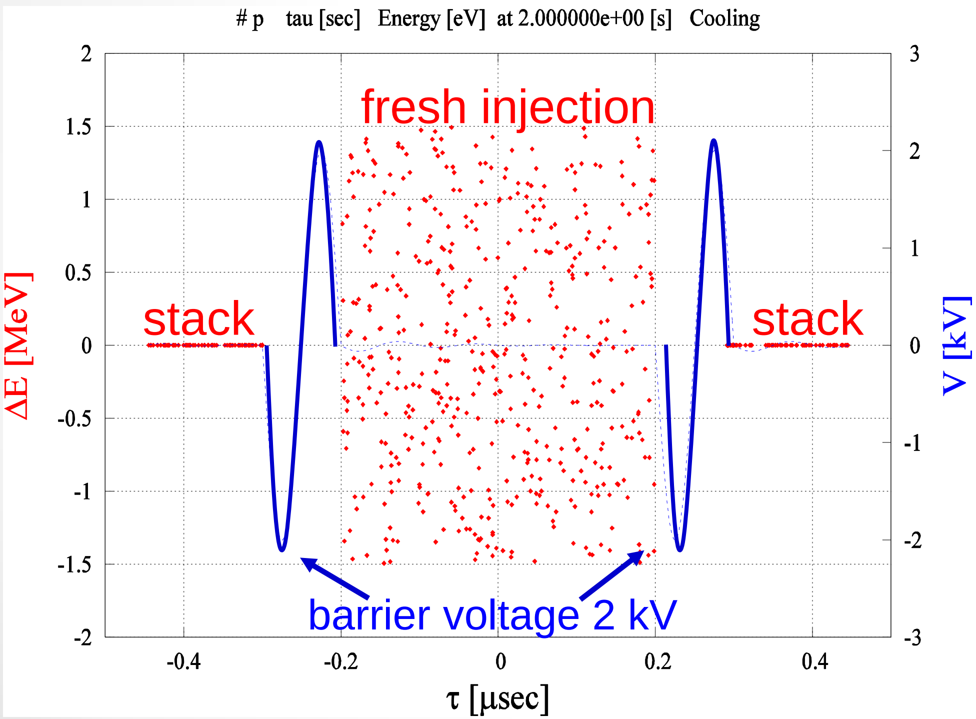
limitations:
space charge tune shift
recombination (REC)

Accumulation of Secondary Particles

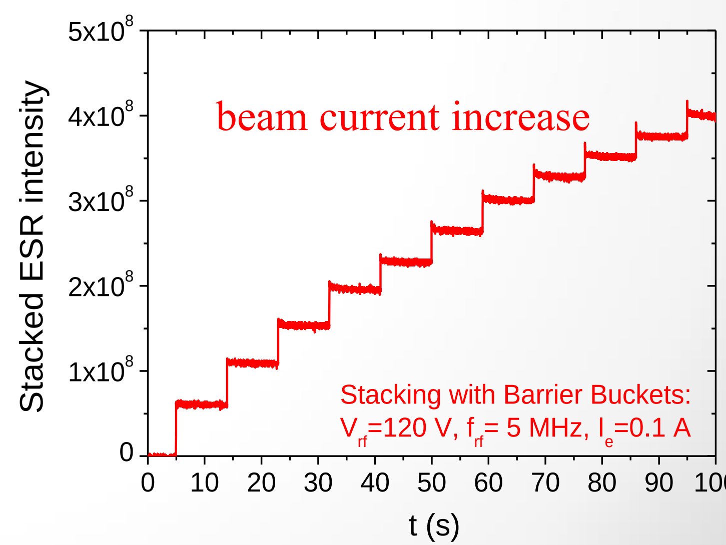
basic idea: confine stored beam to a fraction of the circumference, inject into gap and apply cooling to merge the two beam components
⇒ fast increase of intensity (for secondary beams)

experimental verification at ESR



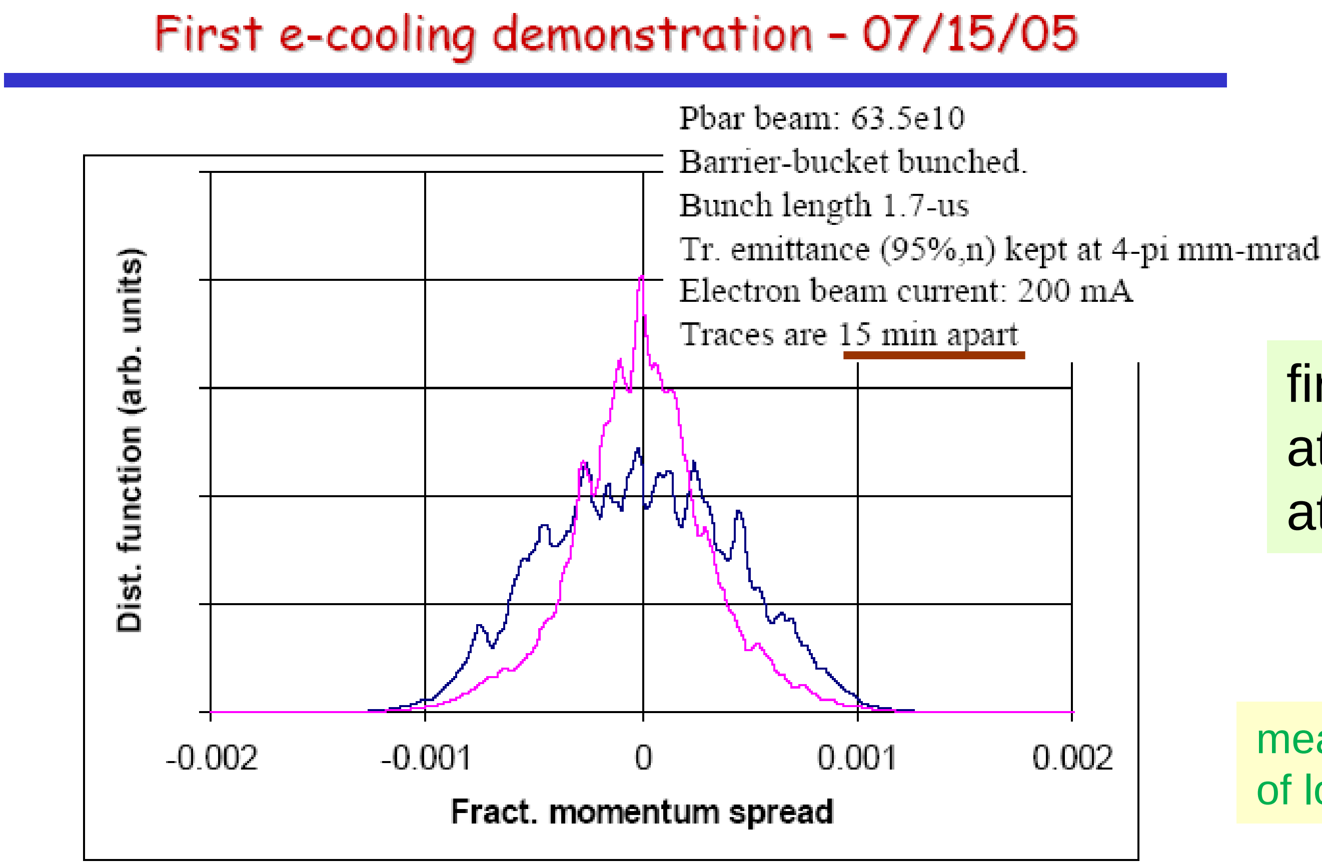


simulation of longitudinal stacking with barrier buckets and electron cooling



Examples of Electron Cooling

high energy electron cooling of 8 GeV antiprotons
longitudinal cooling with 0.2 A, 4.4 MeV electron beam



first electron cooling
at relativistic energy
at Recycler, FNAL

measured by detection
of longitudinal Schottky noise

Electron Cooling Systems

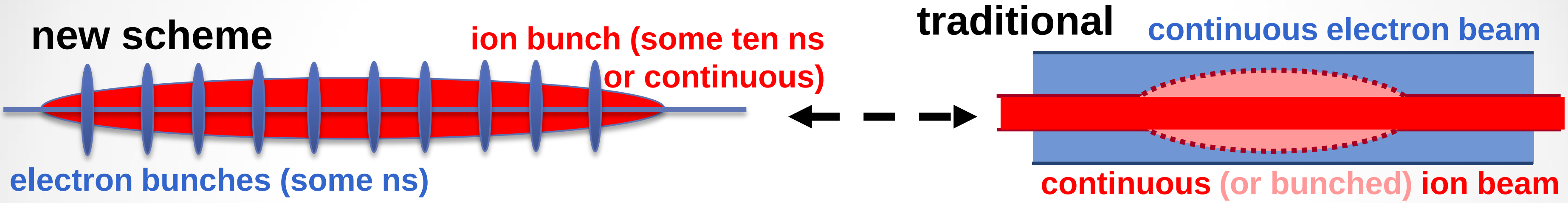
Low Energy: 35 keV SIS/GSI

Medium Energy:
300 keV
ESR/GSI

High Energy:
4.3 MeV Recycler/FNAL

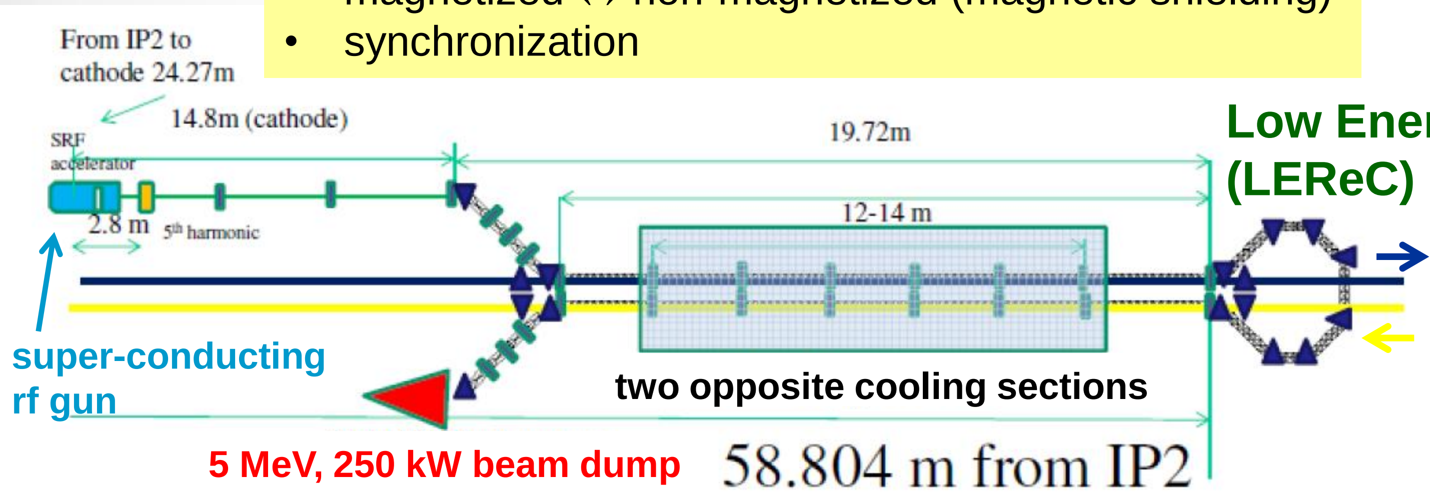
Bunched Beam Electron Cooling

Electron cooling with electrostatic acceleration is limited in energy (5-10 MeV). A bunched electron beam offers the extension of the electron cooling method to higher energy (linear rf accelerator).



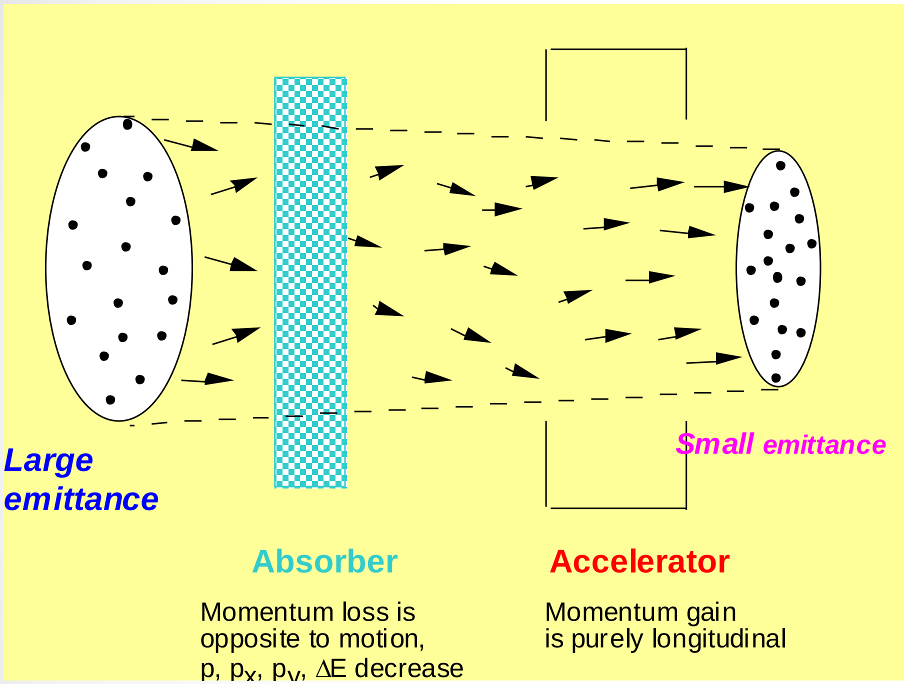
Issues:
- high intensity bunches (production, transport)
- momentum spread and emittance of bunches
- beam alignment
- magnetized ↔ non-magnetized (magnetic shielding)
- synchronization

Low Energy RHIC e-Cooler (LEReC) project at BNL

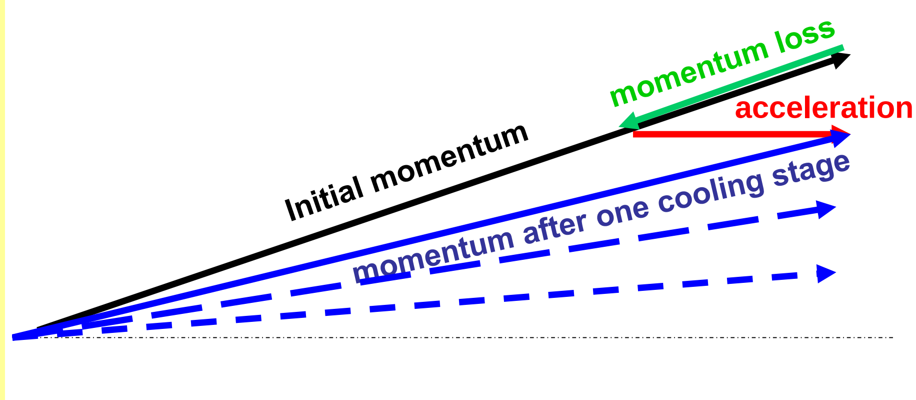


2. Ionization Cooling

energy loss in solid matter



proposed for muon cooling



not useful for heavy particles
due to strong interaction with matter

transverse cooling

$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2 E}\frac{dE}{ds}\epsilon_N + \frac{\beta\gamma\beta_\perp}{2}\frac{\langle\theta_{rms}^2\rangle}{ds}$$

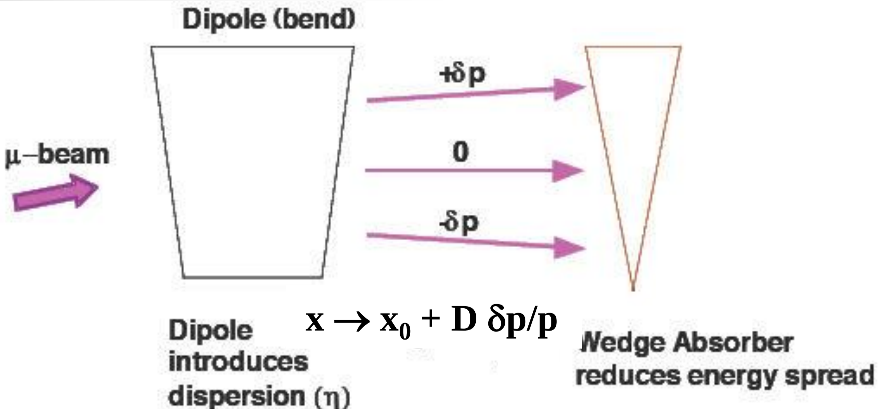
$$= -\frac{1}{\beta^2 E}\frac{dE}{ds}\epsilon_N + \frac{\beta_\perp E_s^2}{2\beta^3 m_\mu c^2 L_R E}$$

small $\beta_\perp$ at absorber in order to minimize multiple scattering

large L_R, (dE/ds) $\Rightarrow$ light absorbers (H_2)

Ionization Cooling

increased longitudinal cooling
by longitudinal-transverse emittance exchange



$$\frac{d\sigma_E^2}{ds} = -2\frac{\partial(dE/ds)}{\partial E}\sigma_E^2 + \frac{d\langle\Delta E_{rms}^2\rangle}{ds}$$

cooling term　　heating term

cooling, if $\frac{\partial(dE/ds)}{\partial E} > 0$

emittance exchange

increased longitudinal cooling

$$\frac{\partial\frac{dE}{ds}}{\partial E} \Rightarrow \frac{\partial\frac{dE}{ds}}{\partial E}|_0 + \frac{dE}{ds}\frac{D\rho'}{\beta c p \rho_0}$$

reduced transverse cooling

$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2 E}\frac{dE}{ds}(1 - \frac{D\rho'}{\rho_0})\epsilon_N$$

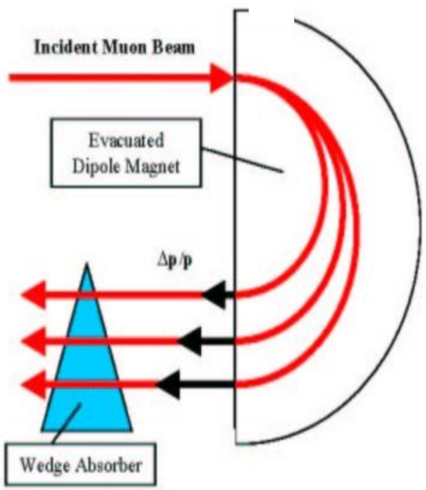


Figure 1. Use of a Wedge Absorber for Emittance Exchange

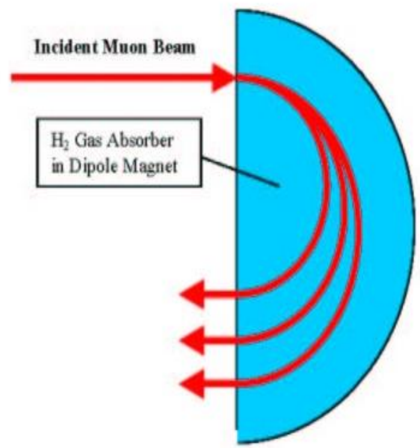
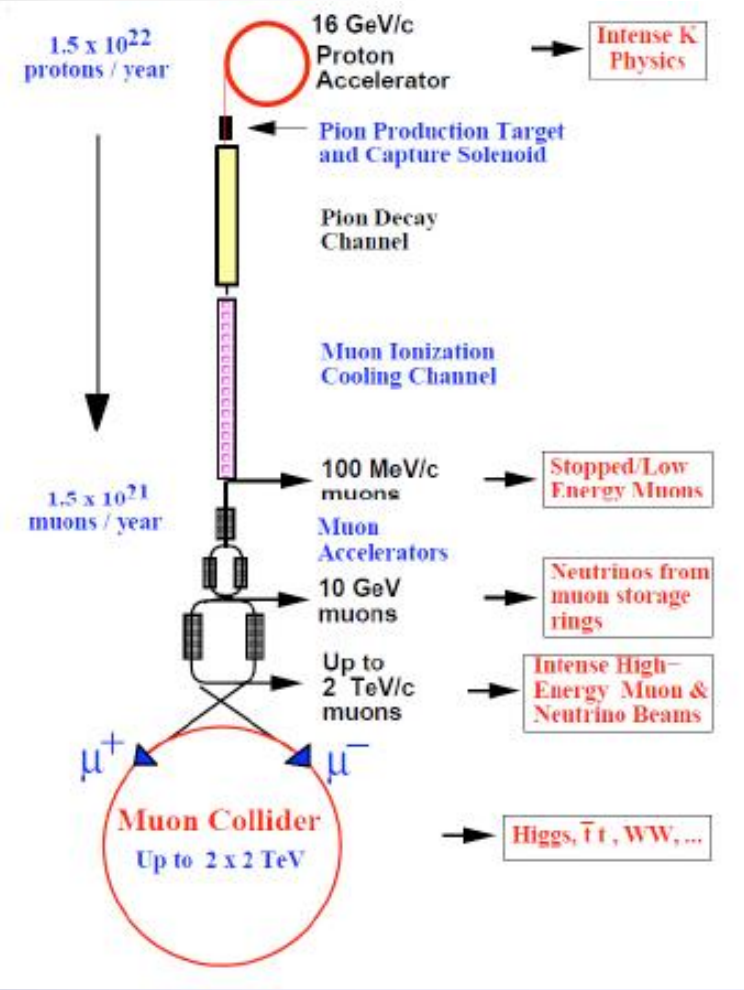


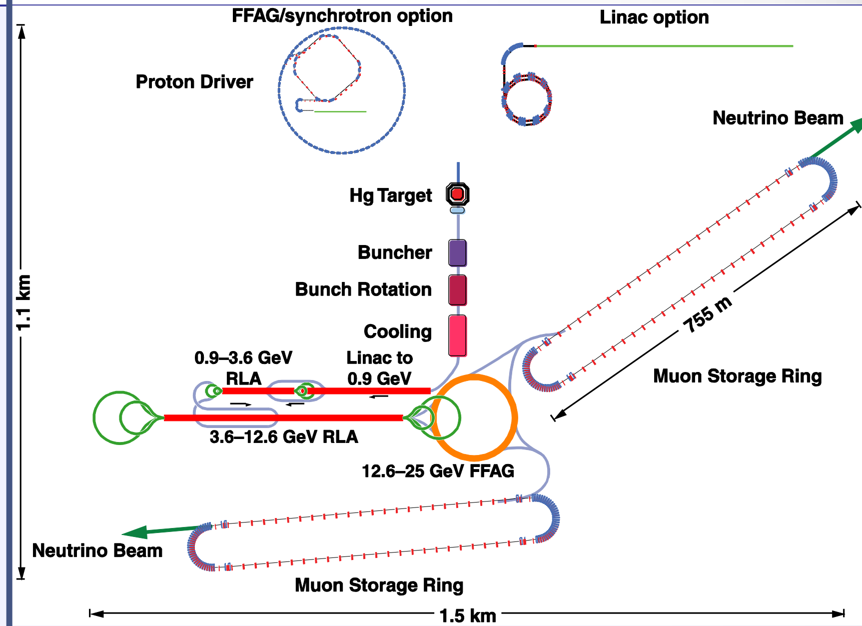
Figure 2. Use of Continuous Gaseous Absorber for Emittance Exchange

Scenarios with Ionization Cooling

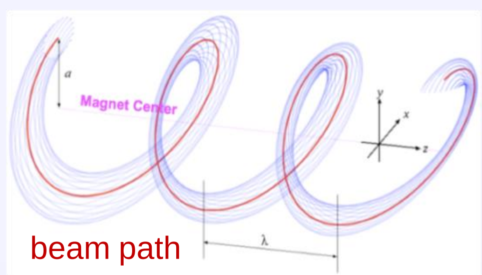
Muon Collider



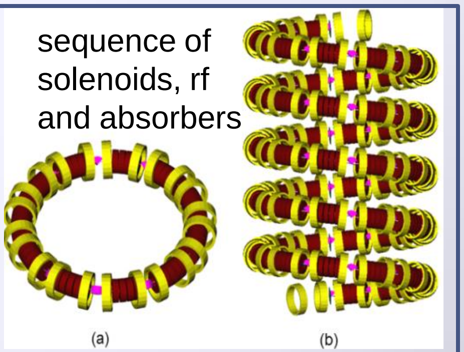
Neutrino Factory



helical cooling channel

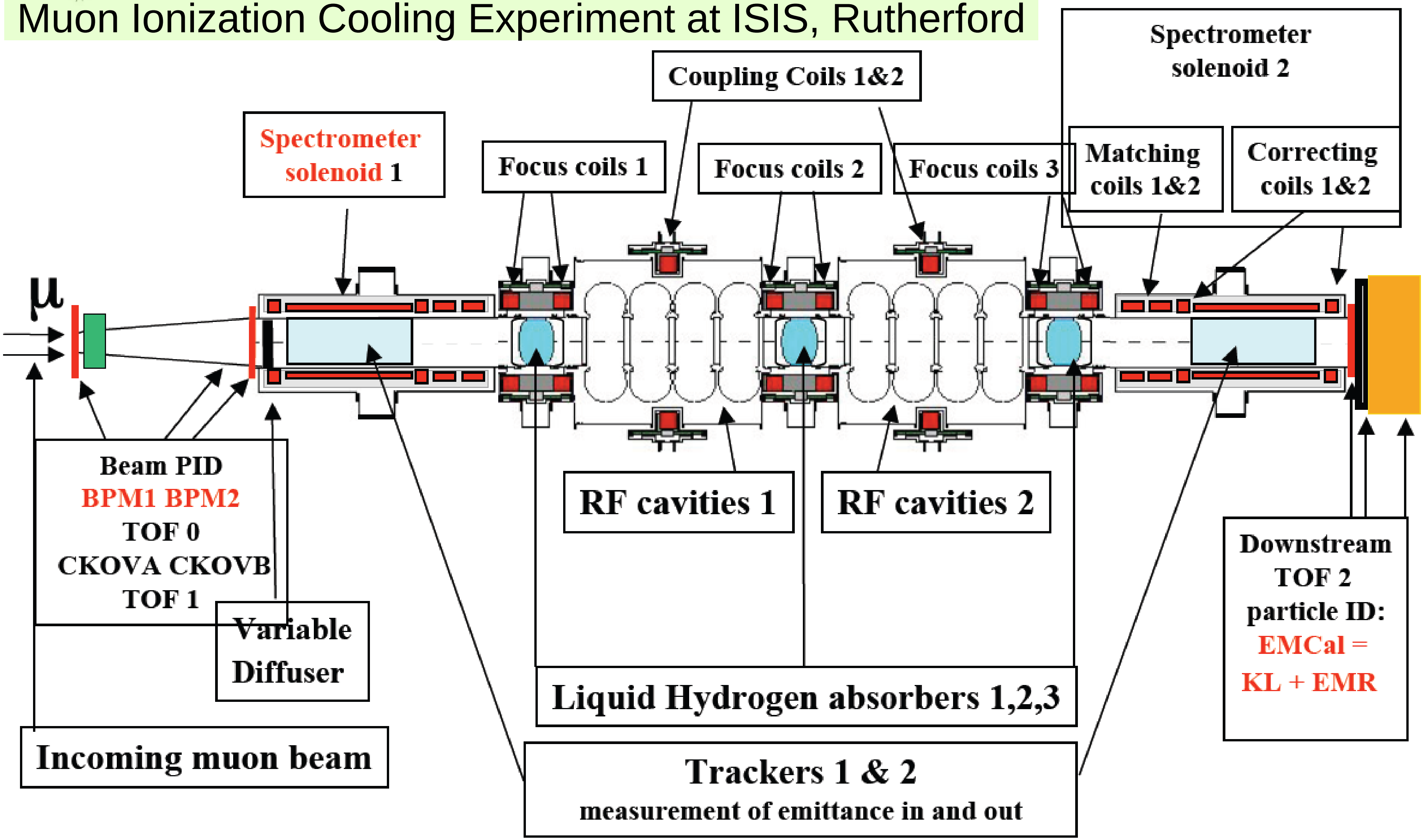


sequence of solenoids, rf and absorbers



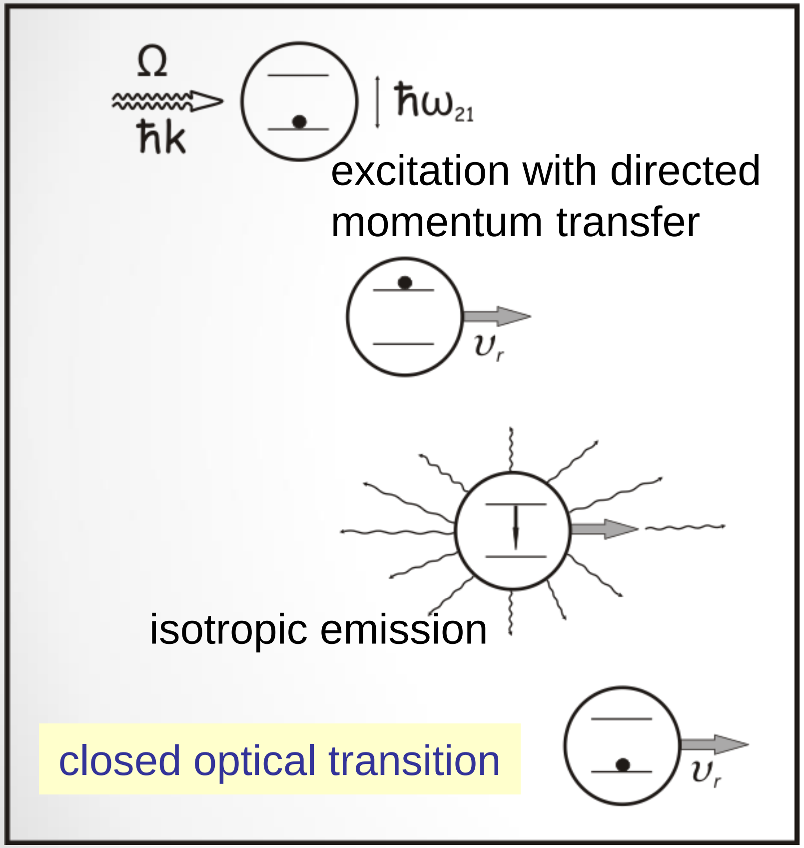
MICE

Muon Ionization Cooling Experiment at ISIS, Rutherford

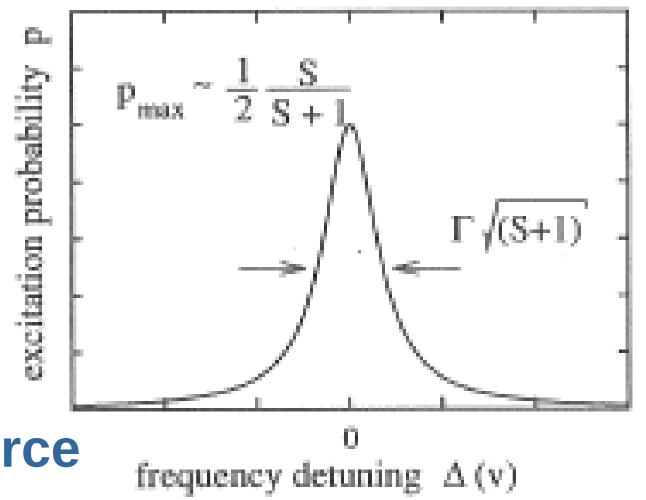


3. Laser Cooling

$$\Omega = \gamma\omega_{21}(1 - \beta\cos\theta)$$



the directed excitation and isotropic emission result in a transfer of velocity v_r



cooling force

$$\vec{F}(\vec{v},\vec{k}) = \frac{\hbar\vec{k}}{2} S\Gamma \frac{(\Gamma/2)^2}{(\omega - \omega_{21} - \vec{v}\,\vec{k}) + (\Gamma/2)^2(1+S)}$$

Lorentzian with width Γ/k ~ 10 m/s

minimum temperature $T_D = \dfrac{\hbar\Gamma}{2k_B}$ (Doppler limit)
typical 10^{-5} – 10^{-4} K

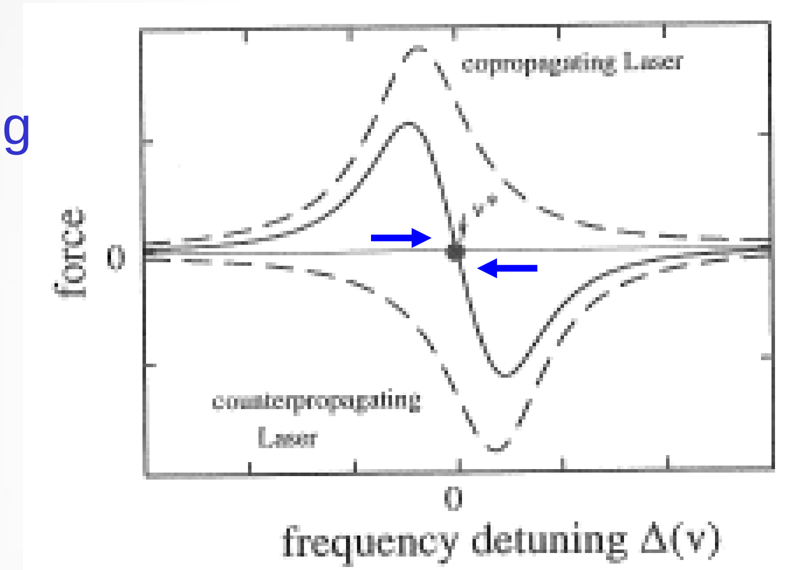
typical cooling time ~ 10 μs

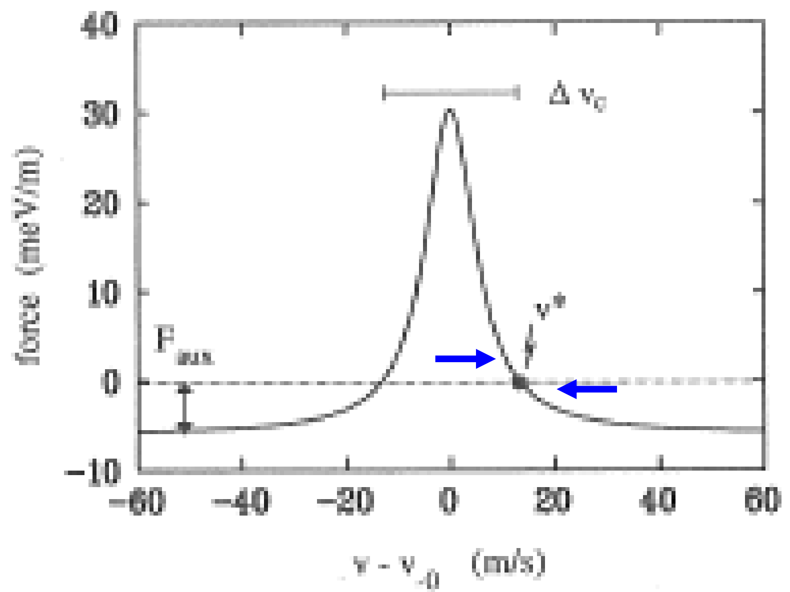
drawback: only longitudinal cooling

Laser Cooling

a single laser does not provide cooling (only acceleration or deceleration)

schemes
for cooling





two counter-propagating lasers (matched to beam velocity)

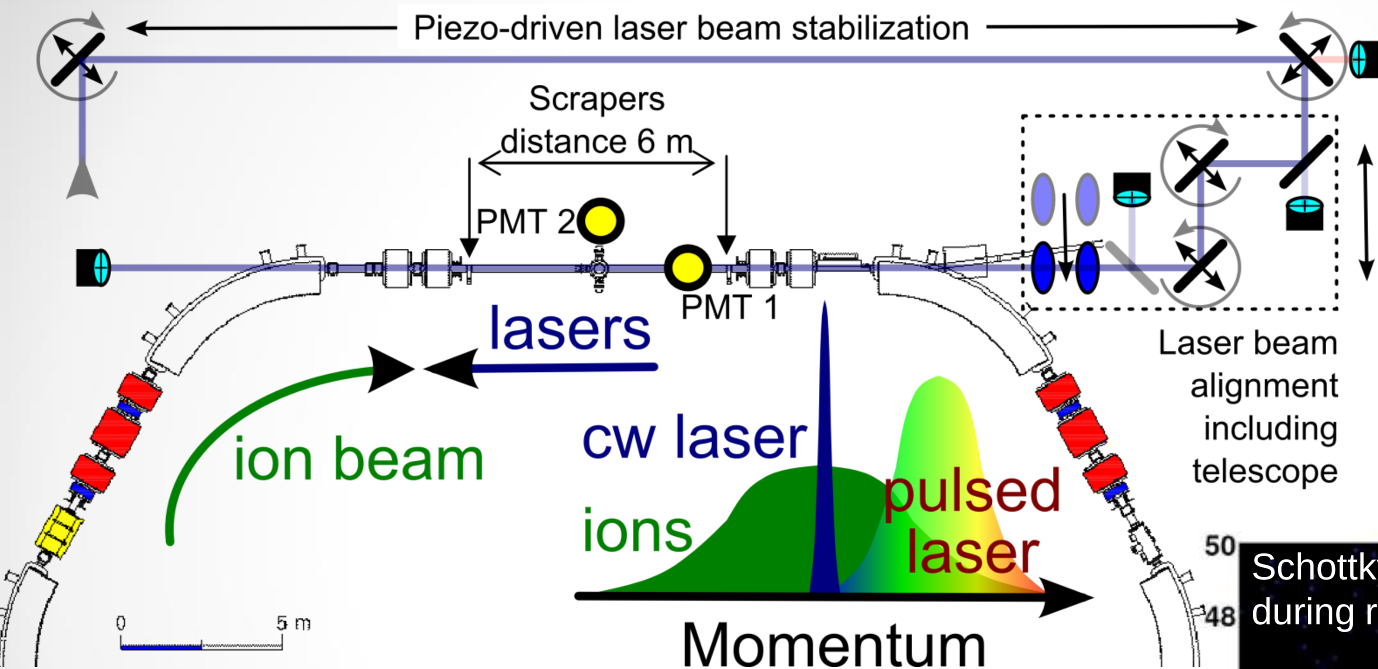
auxiliary force (betatron core, rf)

capture range of laser is limited ⇒ frequency sweep (snowplow)

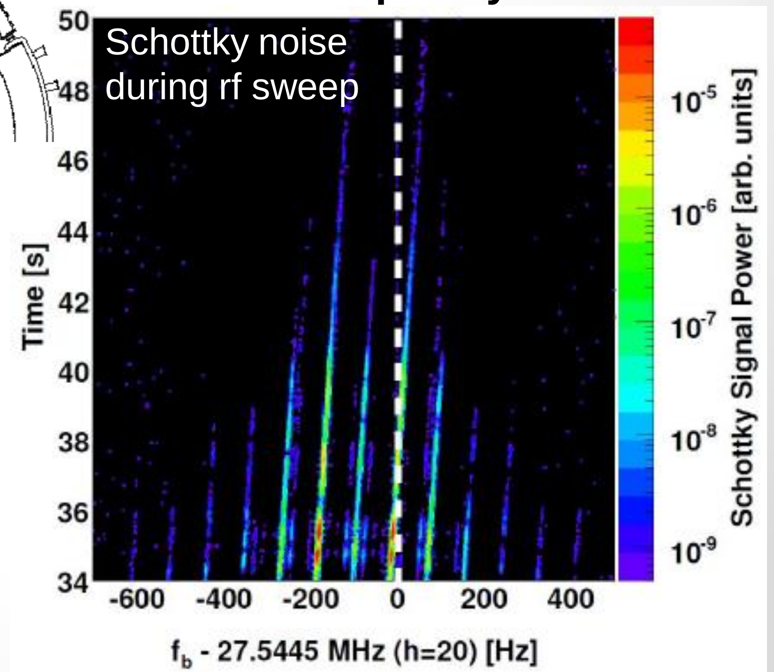
ions studies so far: $^{7}\mathbf{Li}^{1+}$, $^{9}\mathbf{Be}^{1+}$, $^{24}\mathbf{Mg}^{1+}$, $^{12}\mathbf{C}^{3+}$

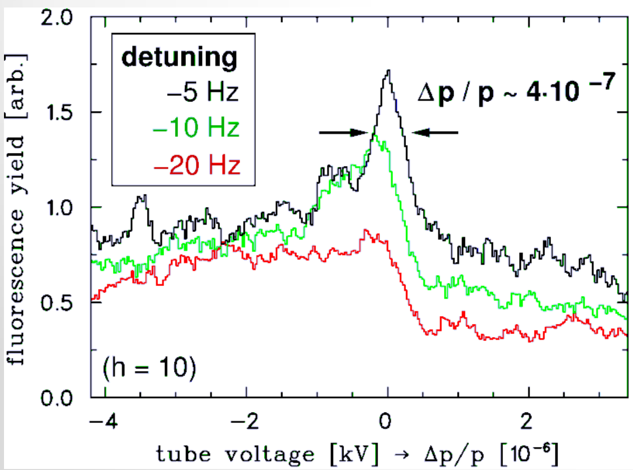
in future: Li-like heavy ions at relativistic energies
large relativistic energy ⇒ large excitation energy in PRF

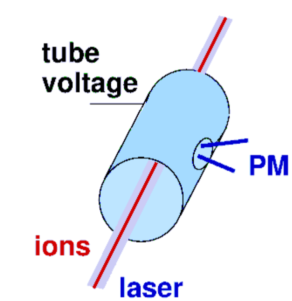
Laser Cooling of C^{3+} at the ESR



Argon ion laser (257.3 nm) frequency doubled



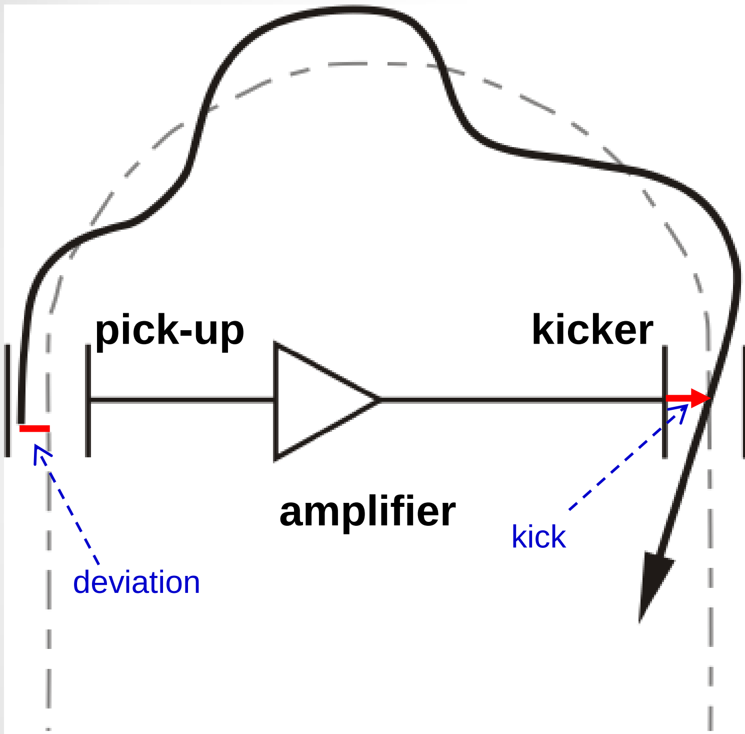




fluorescence light detection

4. Stochastic Cooling

First cooling method which was successfully used for beam preparation



S. van der Meer, D. Möhl, L. Thorndahl et al.
(1925 – 2011) (1936-2012)

Conditions:

Betatron motion phase advance
(pick-up to kicker): $(n + ½)\ \pi$

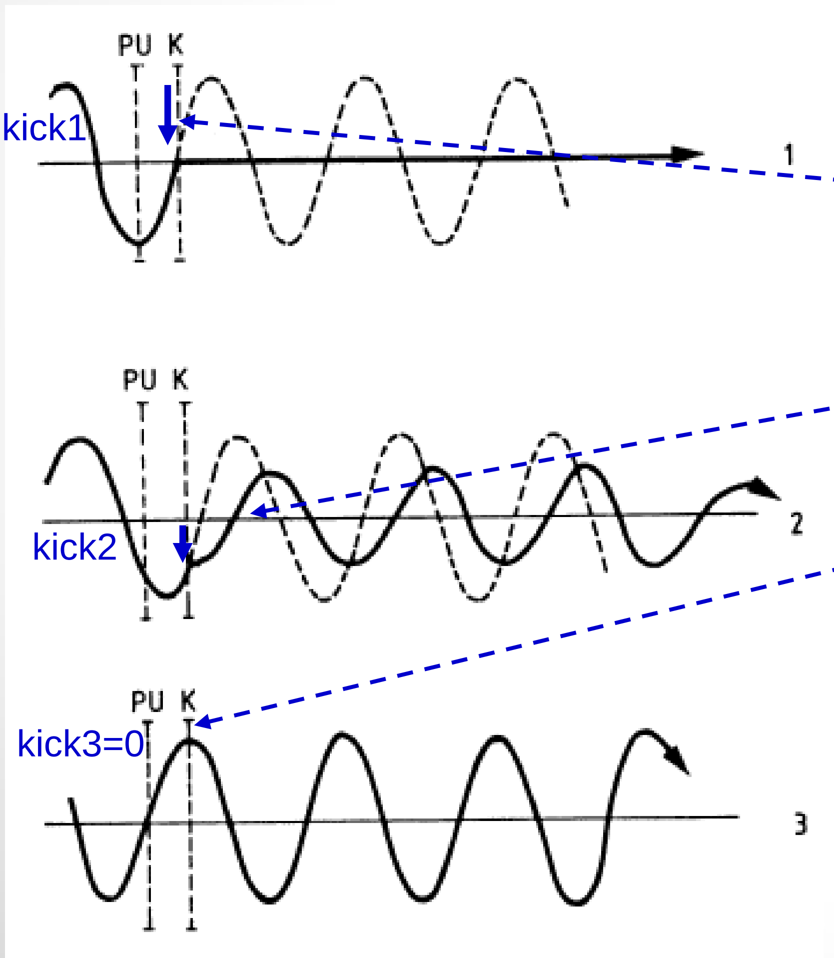
Signal travel time = time of flight of particle
(between pick-up and kicker)

Sampling of sub-ensemble of total beam

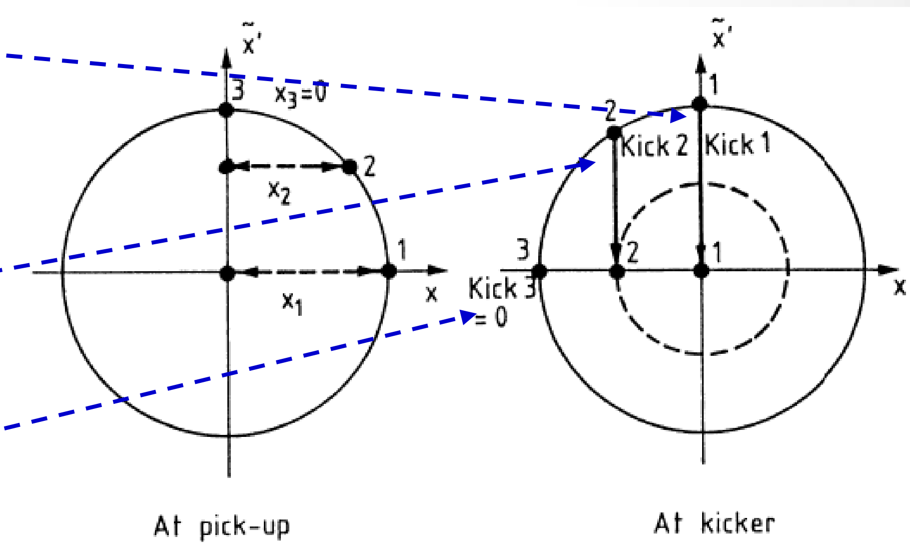
Principle of transverse cooling:
measurement of deviation from ideal orbit
is used for correction kick (feedback)

Stochastic Cooling

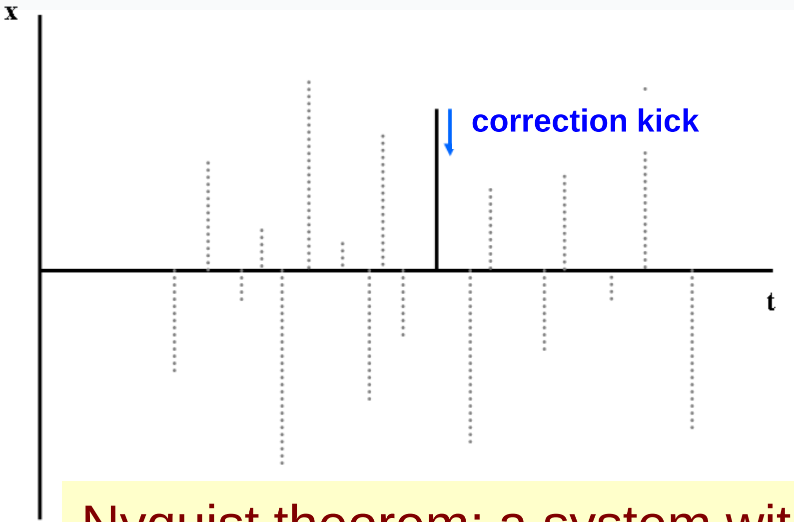
single particle betatron motion
along storage ring
without and with correction kick



projection to two-dimensional
horizontal phase area



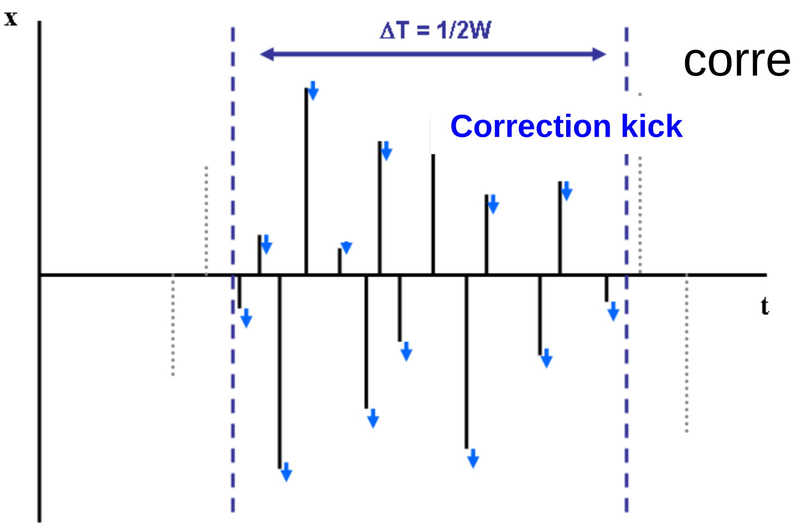
Stochastic Cooling



correction kick
(unlimited resolution)

$$\Delta x = g \times x$$

Nyquist theorem: a system with a band-width $\Delta f = W$ in frequency domain can resolve a minimum time duration $\Delta T = 1/(2W)$



correction kick $\Delta x = \frac{g}{N_s} \times \sum_{i=1..N_s} x_i \; , \quad N_s = N \frac{\Delta T}{T_0} = \frac{N}{2WT_0}$

For exponential damping ($x(t)=x(t_0) \exp(-(t-t_0)/\tau)$):

$$\tau^{-1} = T_0^{-1} \times \frac{\Delta x}{x} = \frac{g2W}{N}, \; if \sum_{i=1..N_s} x_i = x$$

cooling rate $\tau^{-1} \leq \frac{2W}{N} \quad if \; g \leq 1$

Stochastic Cooling

some refinements of cooling rate formula

noise: thermal or electronic noise adds to beam signal

mixing: change of relative longitudinal position of particles due to momentum spread

cooling rate $\lambda = \tau^{-1} = \frac{2W}{N}(\underbrace{2g}_{\text{cooling}} - \underbrace{g^2(M+U)}_{\text{heating}})$

M mixing factor

U noise to signal ratio

maximum of cooling rate

$$\lambda_{max} = \frac{2W}{N}\frac{1}{M+U}$$

$$\frac{d\lambda}{dg} = 0 \Rightarrow g = \frac{1}{M+U}$$

further refinement (wanted ↔ unwanted mixing):

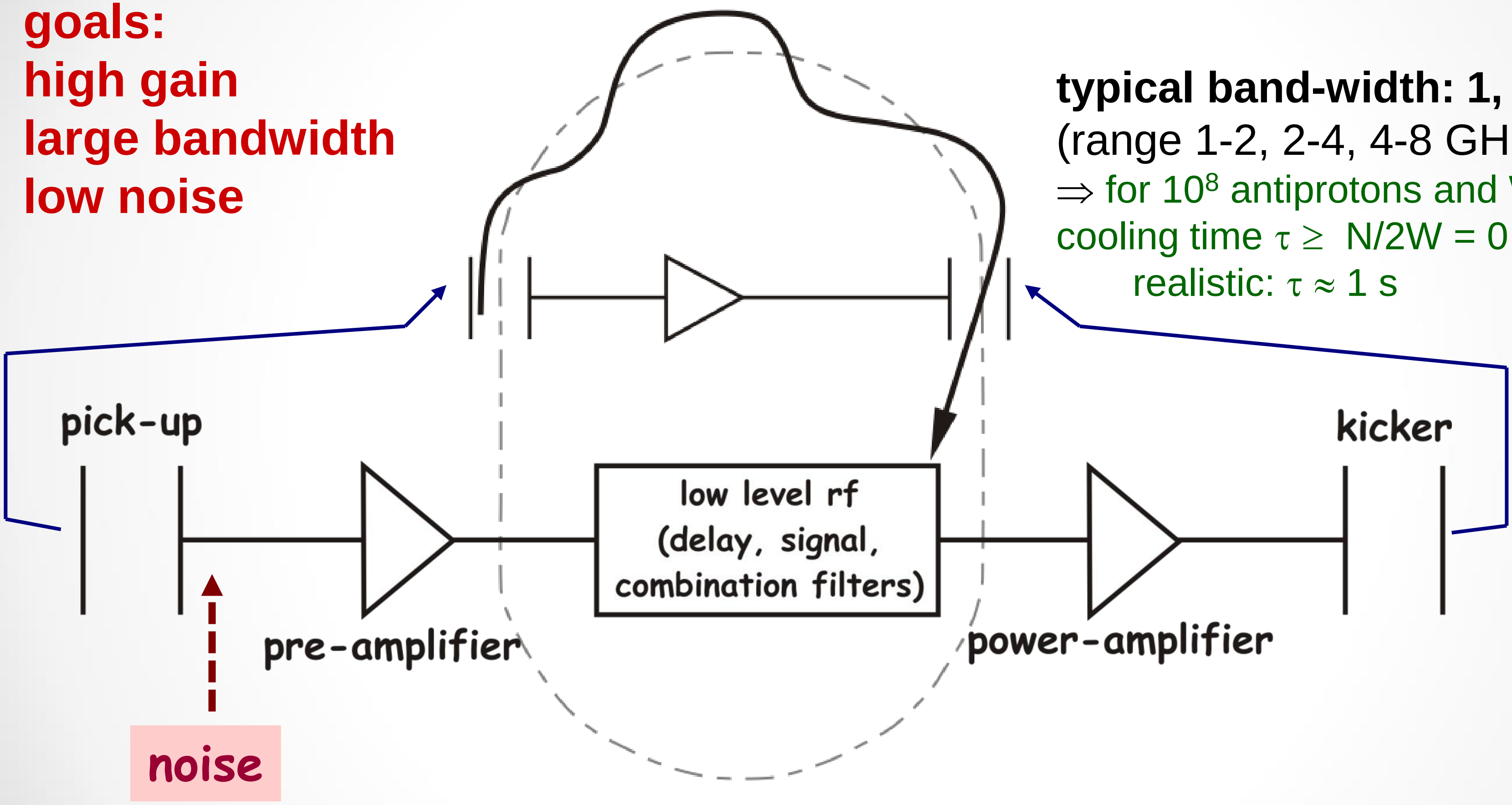
with wanted mixing M (kicker to pick-up)
and unwanted mixing $\tilde{M}$ (pick-up to kicker)

$$\lambda = \tau^{-1} = \frac{2W}{N}(2g(1-\tilde{M}^2) - g^2(M+U))$$

Stochastic Cooling Circuit

goals:
high gain
large bandwidth
low noise

typical band-width: 1, 2, 4 GHz
(range 1-2, 2-4, 4-8 GHz)
⇒ for 10^8 antiprotons and W = 1 GHz
cooling time $\tau \geq$ N/2W = 0.05 s
realistic: $\tau \approx$ 1 s



Transfer Function:

$$Z_{pick-up} \cdot G_{pick-up}(E) \cdot H(t_{delay}) \cdot F(E) \cdot G \cdot G_{kicker}(E) \cdot Z_{kicker}$$

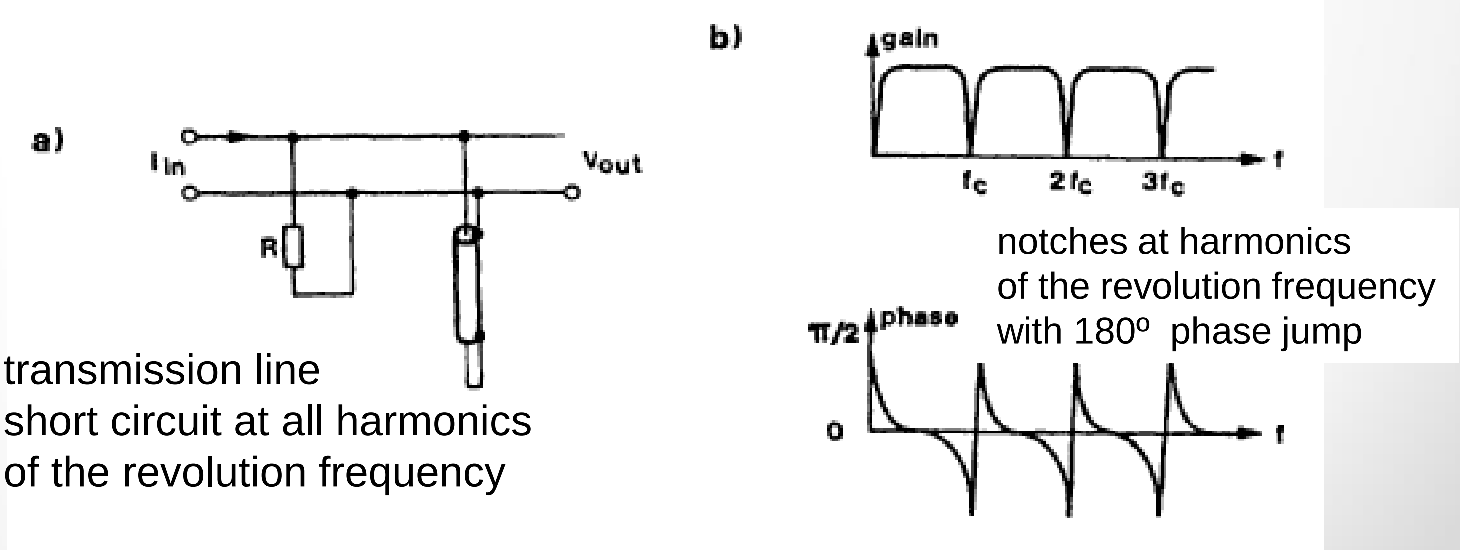
Longitudinal Stochastic Cooling

1) **Palmer cooling**

pick-up in dispersive section detects horizontal position
⇒ acceleration/deceleration kick corrects momentum deviation

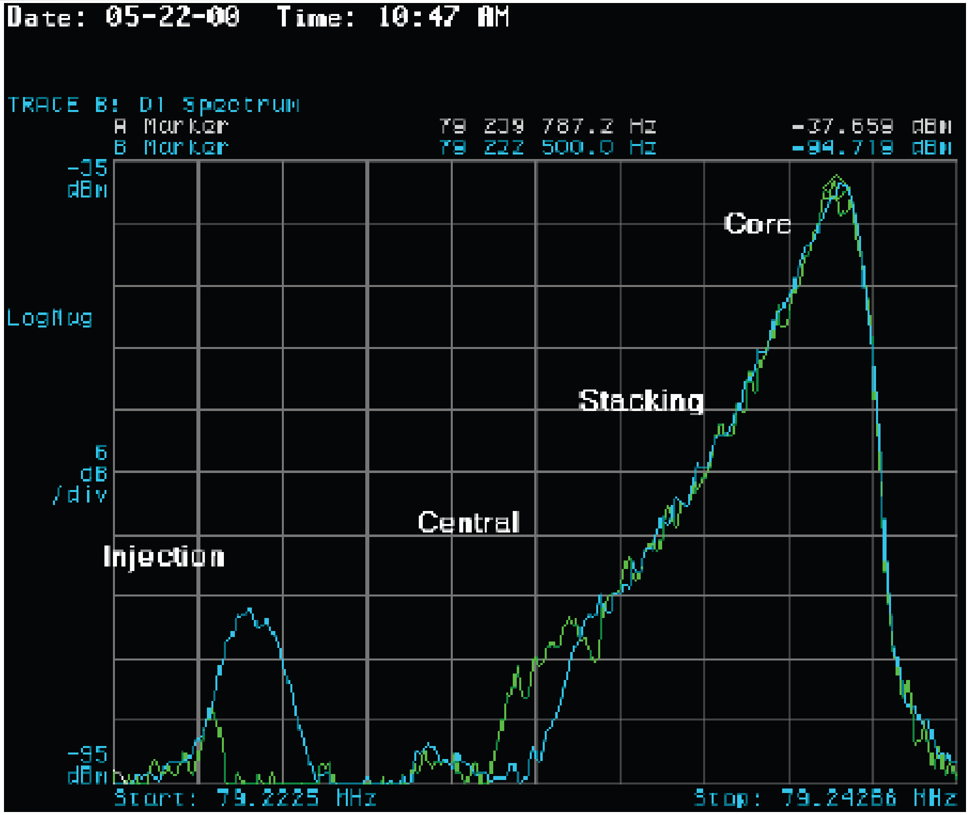
2) **Notch filter cooling**

filter creates notches at the harmonics of the nominal revolution frequency
⇒ particles are forced to circulate at the nominal frequency

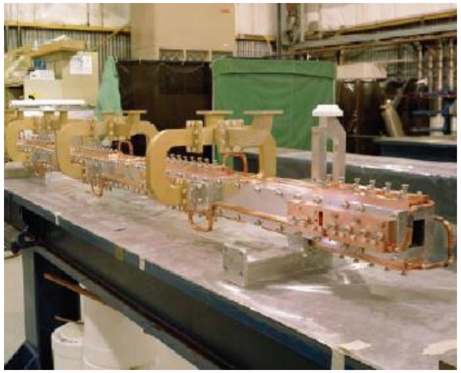


Antiproton Accumulation by Stochastic Cooling

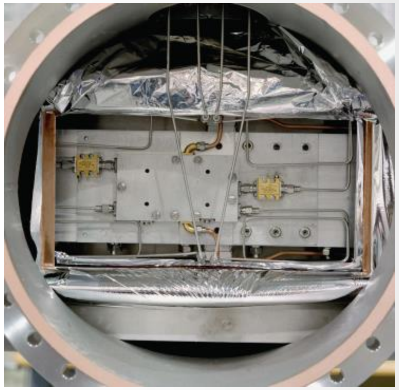
accumulation of 8 GeV antiprotons at Accumulator, FNAL, shut down 09/2011
similar facility AC/AA at CERN, shut down 11/1996



momentum distribution of accumulated antiproton beam



kicker array



cryogenic microwave amplifier

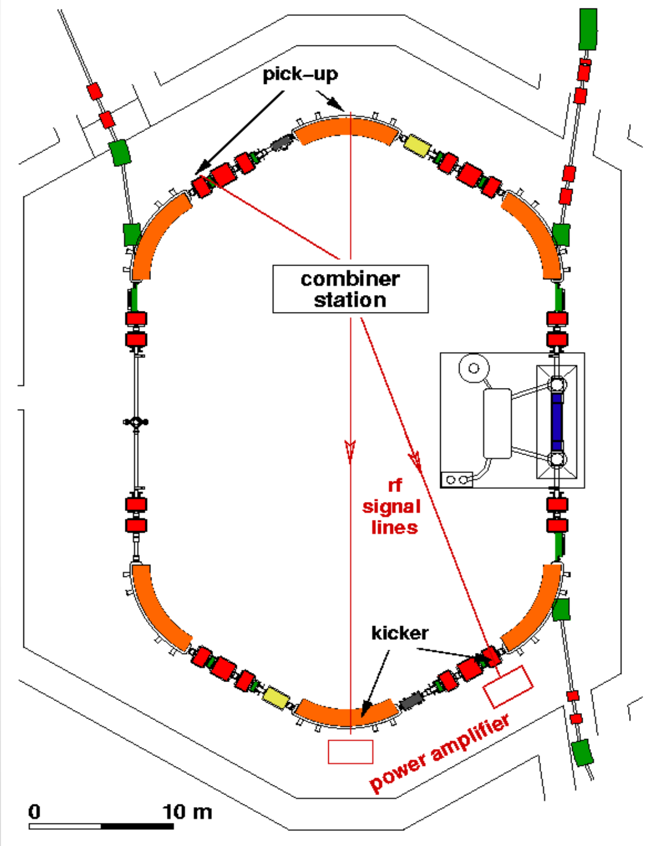
microwave electronics

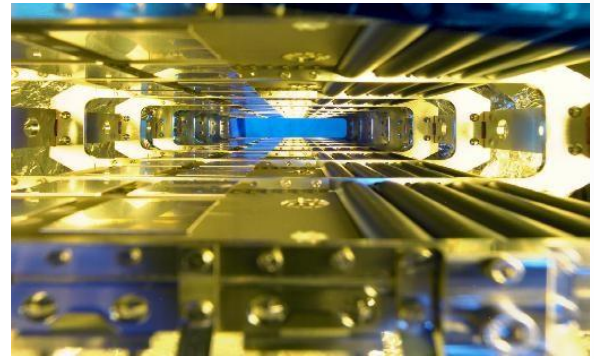
power amplifiers (TWTs)

Stochastic Cooling of Rare Isotopes at GSI

fast pre-cooling of hot fragment beams

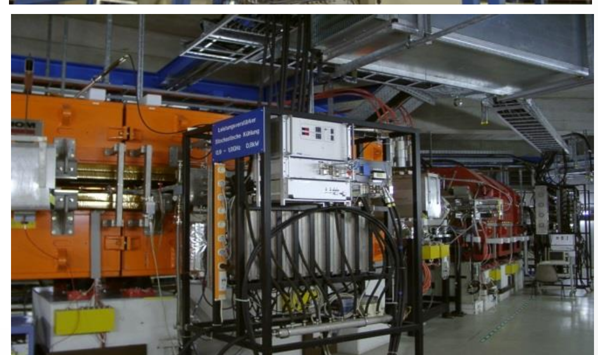
energy 400 (-550) MeV/u
bandwidth 0.8 GHz (range 0.9-1.7 GHz)
$\delta p/p = \pm 0.35\ \%$ → $\delta p/p = \pm 0.01\ \%$
$\varepsilon = 10 \times 10^{-6}$ m → $\varepsilon = 2 \times 10^{-6}$ m





electrodes installed inside magnets

combination of signals from electrodes



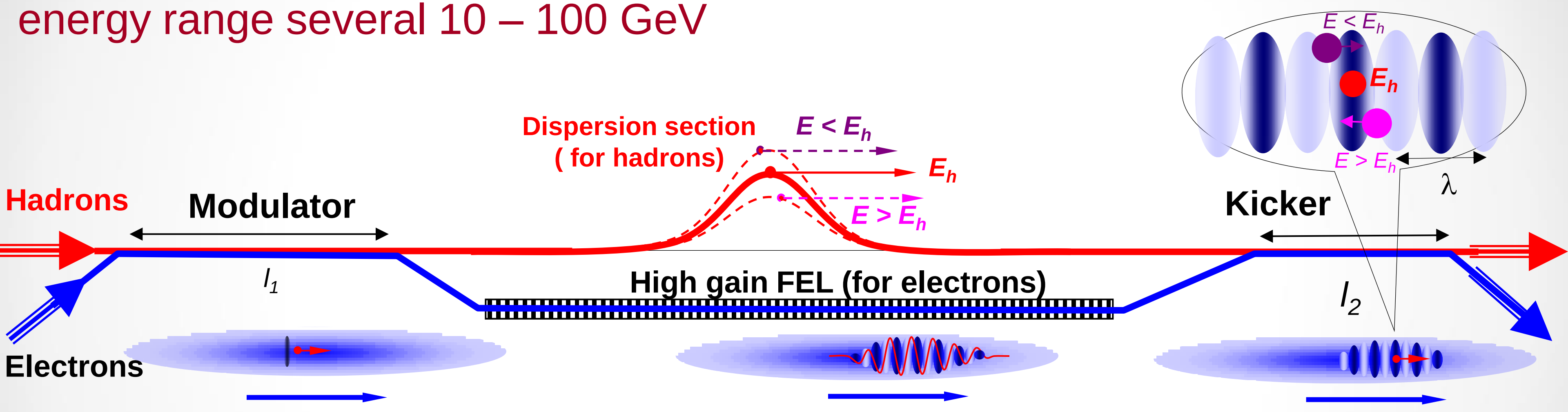
power amplifiers for generation of correction kicks

Coherent Electron Cooling

A combination of electron and stochastic cooling concepts

proposed for fast cooling at highest energies

energy range several 10 – 100 GeV



- The Coherent Electron Cooling system has three major subsystems
  - **modulator**: the ions imprint a "density bump" on the electron distribution
  - **amplifier**: FEL interaction amplifies a density bump by orders of magnitude
  - **kicker**: the amplified & phase-shifted electron charge distribution is used to correct the velocity offset of the ions

Comparison of Cooling Methods

	Stochastic Cooling	Electron Cooling
Useful for:	low intensity beams	low energy
		all intensities
	hot (secondary) beams	warm beams (pre-cooled)
	high charge	high charge
	full 3 D control	bunched beams
Limitations: /problems	high intensity beams	space charge effects
	beam quality limited	recombination losses
	bunched beams	high energy

laser cooling (of incompletely ionized ions)
and ionization cooling (of muons) are quite particular
and not general cooling methods

Trends in Beam Cooling

Stochastic cooling was mainly developed for the production of high intensity antiproton beams for colliders (CERN, FNAL, 1972 – 2011).
It is still in operation at AD (CERN), COSY (FZJ) and ESR (GSI).
It will also be used in the FAIR project (Germany) for cooling of antiprotons and rare isotope beams.

First demonstration of bunched beam stochastic cooling (2008) with ions (BNL) made it also attractive for ion colliders.
Now it is proposed for the collider of the Russian NICA project.

Electron cooling was and still is used in low energy storage rings for protons, ions, secondary beams (antiprotons, rare isotopes).

Electron cooling is interesting for low energy storage rings, but also application at higher energies (MeV electron energies) is envisaged after the successful demonstration of the 4 MeV electron cooler at FNAL.

Other cooling methods, like muon (ionization) cooling or coherent electron cooling are under investigation, but are still far from implementation in a full scale machine.

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Biannual Workshops on Beam Cooling: e. g. COOL'15, Jefferson Lab, USA