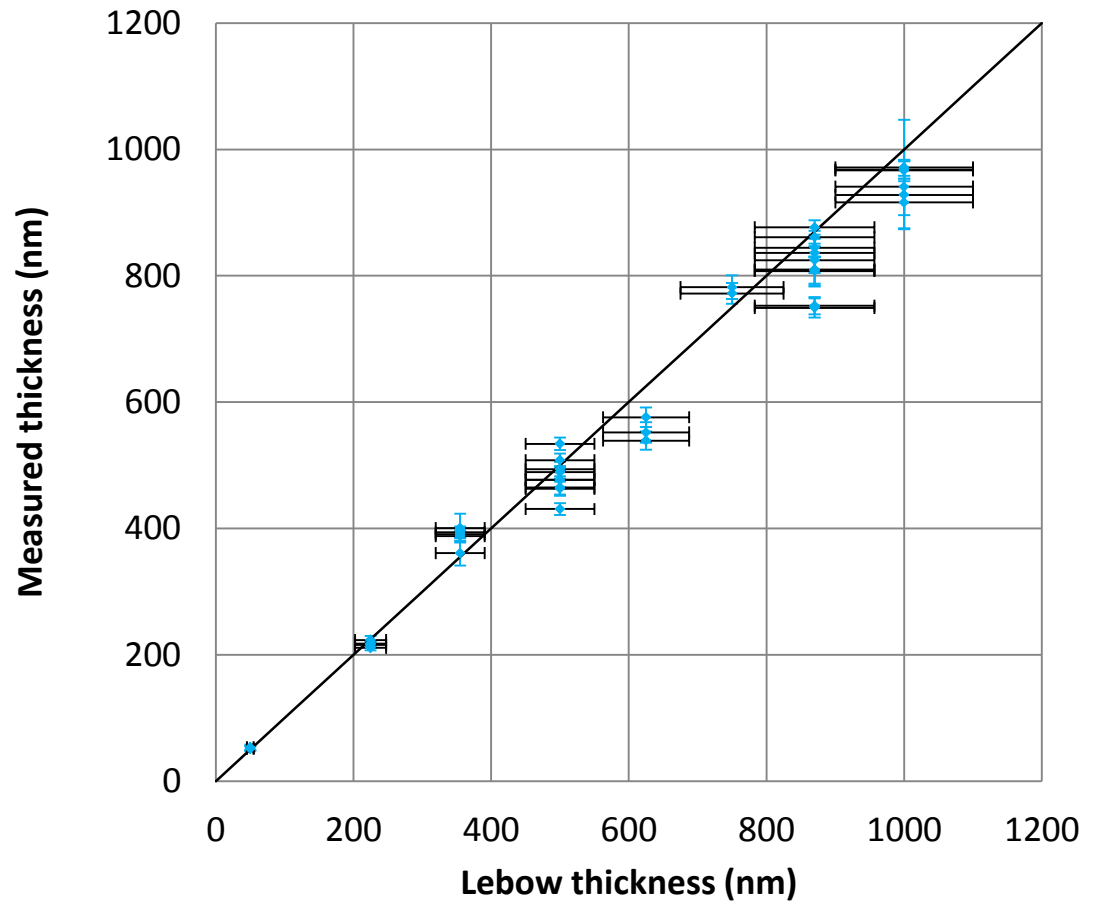


# Foil thickness measurements more uncertainties captured

29July2015

# Old slide: First pass at data error bars

Foil	Lebow (nm)
5385B	1000
3057C	870
5134B	750
7028B	625
5275C	500
5613A	350
7029B	225
6809B	50



# Sources of uncertainty in measurement

1. Inherent limitations of the sample preparation and measurement in the FESEM
  - a. FESEM resolution: 1.2 nm machine specifications
  - b. Image tilt**
  - c. Uncertainty in magnification/working distance
2. Limitations on analyzing the image
  - a. Pixel resolution:  $\pm 4$  pixels estimated, varies from  $\pm 2.5 - 40$  nm depending on scale**
  - b. Reproducibility between different analyses of same image**
  - c. Differences between images that should be the same
  - d. Differences between images that should be similar (tilt, translation)
3. Errors or problems introduced in the preparation of the samples
  - a. Sample mounting flatness, uniformity
  - b. Any deformation during cleaving? Did it snap nicely or pull?
4. Uncertainties that have to be bounded by Lebow specifications
  - a. Uniformity across entire sample: quote  $\leq 2\%$**
  - b. Uniformity between samples within a batch: quote  $\leq 5\%$

Boldface items included previously

# FESEM measurement uncertainties

1b:

- Tilt (pitch) of  $\pm 5^\circ$  introduced – none of the images appear to have pitch greater than  $\pm 5^\circ$
- For a tilt of  $\pm 5^\circ$ , we'd expect to measure 99.6% of the actual thickness of the foil.
- 0.4% uncertainty added to all for possible misalignments in tilt

1c:

- Tilting can change the working distance of the edge of the foil.
- Calculated for sample stage 25 mm, hinged at back edge. Change in working distance no more than 0.1 mm for tilts of  $\pm 5^\circ$ , or  $\sim 1\%$  of  $\sim 10$  mm working distance
- Tilt induced working distance uncertainty of 1% added

1d:

- Working distance knob specifies working distance to 0.1 mm. This adjusts focus
- Out of focus images can be about 1 “click” of the focus knob off.
- This accounted for by 0.1 mm/working distance for each image  $\sim 1\%$

# Image analysis uncertainties

2a:

- Line length assumed to be no better than  $\pm 2$  pixels at each end,
- Pixel – nm conversion for each image used
- **\*\*Note – this has been assumed constant across images with different magnifications and still needs to be addressed\*\***

2b:

- The same image was analyzed 2-3 times typically.
- Each measurement has an uncertainty
- Percent uncertainty for each measurement were used, average percent uncertainty of the weighted mean of the measurements is quoted here to get one number for each foil

2c:

- Some of the foils have multiple images of the same area at nominally the same tilt and location: perhaps focus or magnification was changed, but these should yield the same value since it is the same foil.
- The standard deviation of data sets in nominally identically conditions used here (smaller set of data than in 2d).

2d:

- Some of the foils have images made of different spots: different samples (center, edge) or translations along one sample.
- The standard deviation of all the data sets at different locations is used to get this uncertainty

# Sample prep and Lebow consistency

3a: Sample mounting flatness and uniformity need to be considered and assigned an uncertainty. Not sure how to quantify this

3b: if we are systematically stretching or pulling the foil when we try to cleave the gold along with the silicon substrate, we should assign a value to this: it will only make them thinner, and we see a trend toward all the thicker foils measuring thinner than the Lebow quote. This systematic could affect the fit of the line.

4a: Lebow quotes the non-uniformity across each foil at less than 2%. If we are getting non-uniformities in 2d greater than 2%, it is likely our technique rather than the foils and we need to reconcile these numbers.

4b: Lebow only guarantees that sibling foils are identical to less than 5%. We could have cases where this could be our leading cause, and if we find elastic rates that deviate significantly from the FESEM measurements, this could be a factor.

# Error contributions

All measurements in nm

foil	Lebow (nm)	Meas (nm)	1a: FE-SEM res.	1b: tilt 0.4% mea thick	1c: working distance due to tilt	1d: working distance or focus – 0.1 mm/ WD	2a: pixel res.	2b: re-analy. same image	2c: diff btwn similar images	2d: varia. btwn diff configs	3: ??? stretch, foil mnt issues	4a: lebow foil unifor m 2%	4b: Lebow batch uniform. 5%
5385	1000	<b>943.7</b>	1.2	3.7	9.2	8.5	40.0	31.0	29.0	6.5		20.0	50.0
3057	870	<b>836.8</b>	1.2	3.3	8.3	8.3	8.0	13.8	7.1	5.6		17.4	43.5
5134	750	<b>774.6</b>	1.2	3.1	7.7	6.9	10.0	13.2	9.1	9.1		15.0	37.5
7028	625	<b>561.2</b>	1.2	2.2	5.6	4.6	8.0	12.6	8.0	8.0		12.5	31.3
5275	500	<b>487.6</b>	1.2	2.0	4.9	4.3	8.0	8.4	3.4	2.9		10.0	25.0
5613	355	<b>389.4</b>	1.2	1.6	3.9	3.4	8.0	6.6	4.5	4.5		7.1	17.8
7029	225	<b>215.2</b>	1.2	0.9	2.2	1.9	2.6	2.7	1.9	1.9		4.5	11.3
6809	50	<b>52.0</b>	1.2	0.2	0.5	0.4	2.6	3.2	2.3	2.3		1.0	2.5

FESEM  
uncertainties

Image analysis  
uncertainties

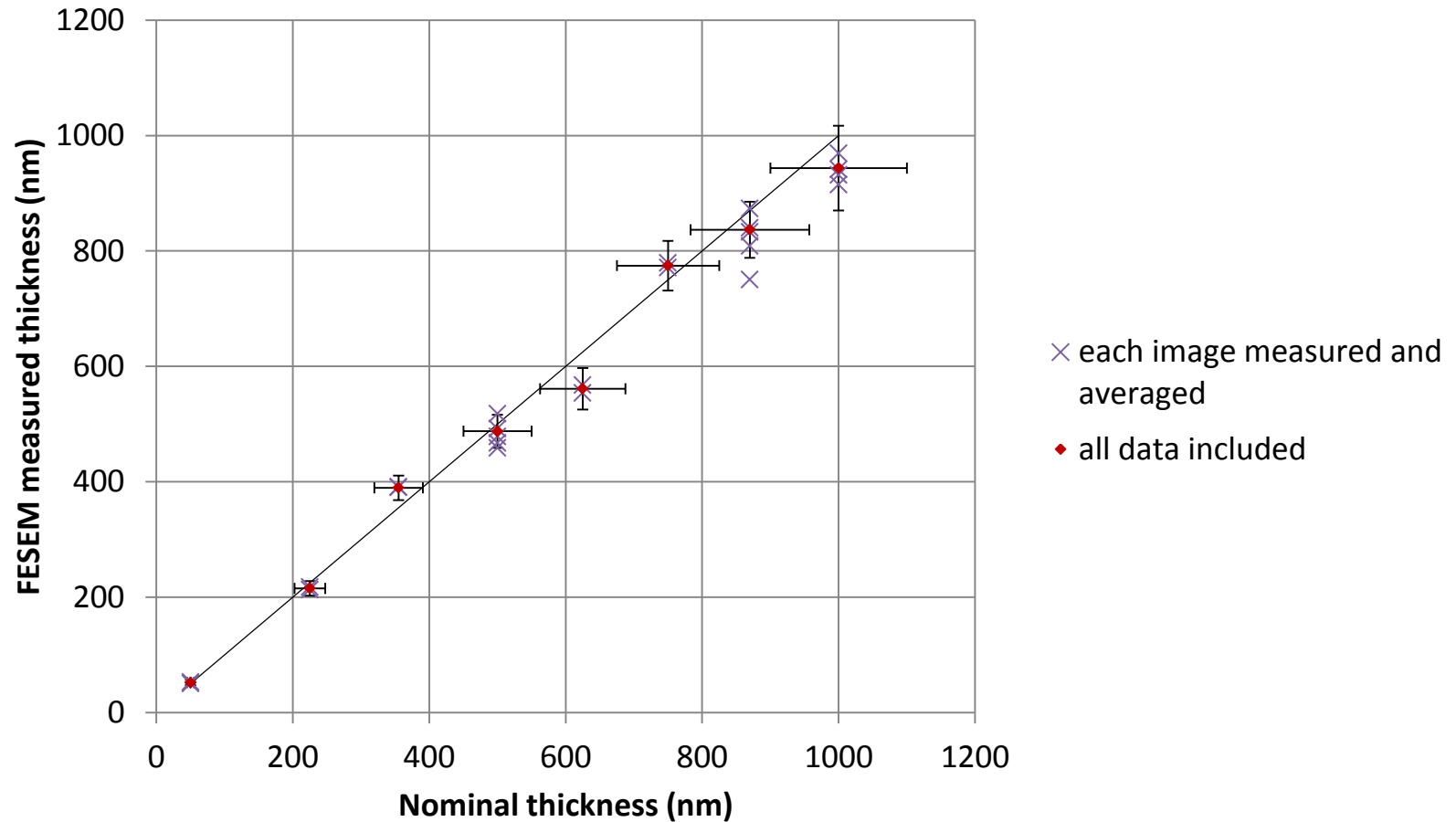
Quoted batch  
and  
sibling uniformity

# Combining uncertainties

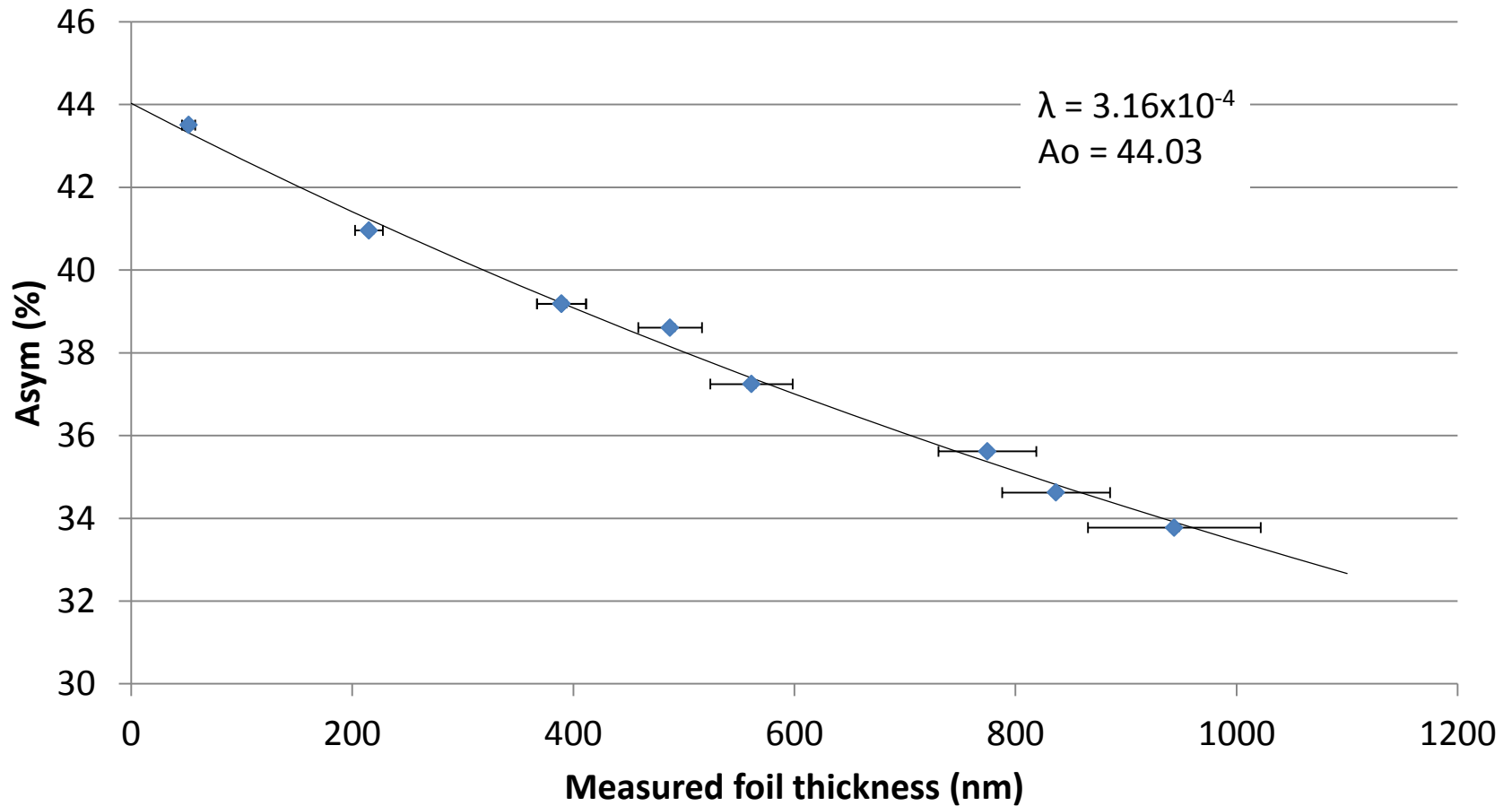
Target ladder position	foil	Meas (nm)	FESEM (all from section 1)	image anayl (all from section 2)	Lebow (from section 4: larger only)	Total uncertainty (nm)
15	5385	<b>943.7</b>	13.1	58.7	50.0	<b>78.2</b>
3	3057	<b>836.8</b>	12.3	18.3	43.5	<b>48.8</b>
4	5134	<b>774.6</b>	10.9	21.0	37.5	<b>44.3</b>
2	7028	<b>561.2</b>	7.7	18.7	31.3	<b>37.2</b>
5	5275	<b>487.6</b>	6.9	12.5	25.0	<b>28.8</b>
8, 14	5613	<b>389.4</b>	5.5	12.1	17.8	<b>22.2</b>
1	7029	<b>215.2</b>	3.2	4.6	11.3	<b>12.6</b>
13	6809	<b>52.0</b>	1.4	5.3	2.5	<b>6.0</b>



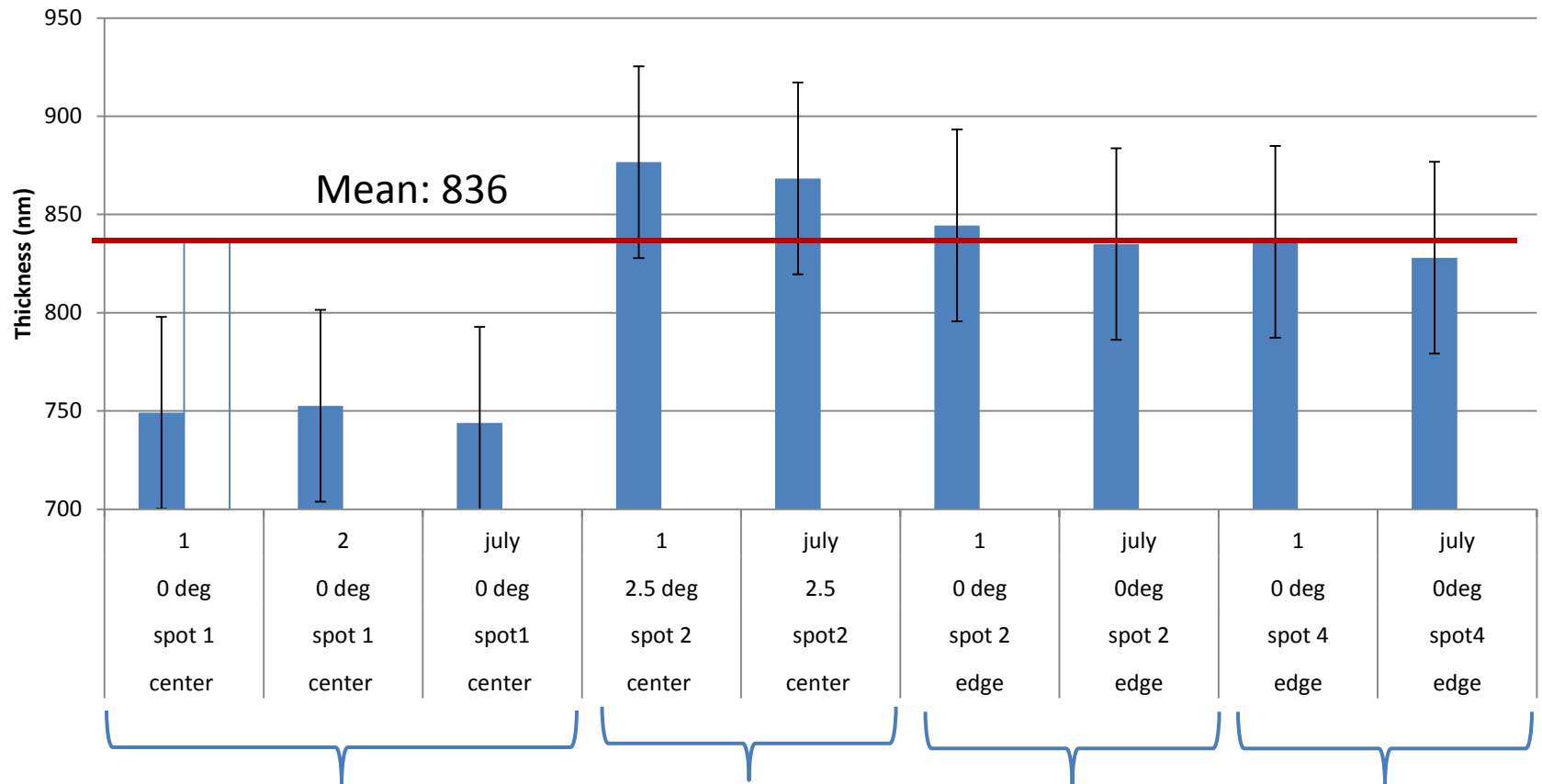
# Incorporating more sources of uncertainty



# Incorporating more sources of uncertainty



# Foil "870 nm" looked at again



Multiple analyses of the same image are grouped