Additional modeling comparing Hamamatsu and Broadcom SiPM for HEP PWO readout

Consider 15, 20, 25, 30% optical coupling efficiency between PWO and SiPM to estimate non-linearity

Modeling computation (energy linearity)

- Estimate the number of cells firing from incident particle
- Compute integral non-linearity at 15GeV
- Photon collection from crystal to SiPM? Use 100% and 20% (more realistic)

$$N_{fired}(M, V, \lambda) = M.\left\{1 - exp\left[-\frac{PDE(V, \lambda).N_{ph}}{M}\right]\right\}$$

 N_{fired} = number of activated cells

M = total number of cells

 $PDE(V, \lambda) =$ photodetection efficiency $V = bias \ voltage, \lambda = photon \ wavelength$

V_{ph}	=	number	of	incident	photons
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		Hamamatsu S14160-3010	Onsemi 60035	Hamamatsu S14160-3015	Broadcom AFBR- S4N44C013	Broadcom AFBR- S4N44P014M
	Total number of cells	89984	22292	39984	15060	8334
	Incoming Particle energy (eV)	1.50E+10	1.50E+1 0	1.50E+10	1.50E+10	1.50E+10
	Scintillator light yield (ph/eV)	1.50E-05	1.50E- 05	1.50E-05	1.50E-05	1.50E-05
	N photon / incoming particle	2.25E+05	2.25E+0 5	2.25E+05	2.25E+05	2.25E+05
5	Crystal surface area (mm2)	400	400	400	400	400
	Nflux (ph/mm2)	563	563	563	563	563
	Nb of SiPM	16	9	16	16/25	16
	SiPM active area (mm2)	9	37	9	13.84	13.47
	Nph for one SiPM	5063	20725	5063	7784.1	7575
	Include fill factor to Nph	1569	15544	2481	4687	5757
	Nb of activated sites/SiPM	907	6635	1588	3001	3633
	INL at 15GeV	<mark>0.18%</mark>	<mark>10.69%</mark>	<mark>1.26%</mark>	<mark>8.21%</mark>	<mark>24%</mark>
	Total activated cells	14506	59713	25402	48021	58131
	Resolution (bit)	14	16	15	16	16
	INL at 15GeV 20% coupling efficiency	<mark>0.04%</mark>	<mark>2.56%</mark>	0.26%	<mark>1.85%</mark>	<mark>6.59%</mark>
	Total activated cells	2913	13687	5163	10476	14428
	Resolution (bit)	12	14	13	14	14

Best compromises

Additional NL estimates vs. optical coupling

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INL at 15GeV 100% coupling efficiency	0.18%	<mark>10.69%</mark>	<mark>1.26%</mark>	<mark>8.21%</mark>	<mark>24%</mark>
Total activated cells	14506	59713	25402	48021	58131
Resolution (bit)	14	16	15	16	16
INL at 15GeV <mark>15%</mark> coupling efficiency	<mark>0.027%</mark>	<mark>1.94%</mark>	<mark>0.19%</mark>	<mark>1.40%</mark>	<mark>5.05%</mark>
Total activated cells	2185	10355	3876	7900	10975
Resolution (bit)	12	14	12	13	14
INL at 15GeV <mark>20%</mark> coupling efficiency	<mark>0.036%</mark>	<mark>2.56%</mark>	<mark>0.26%</mark>	<mark>1.85%</mark>	<mark>6.59%</mark>
Total activated cells	2913	13687	5163	10476	14428
Resolution (bit)	12	14	13	14	14
INL at 15GeV <mark>25%</mark> coupling efficiency	<mark>0.046%</mark>	<mark>3.16%</mark>	<mark>0.32%</mark>	<mark>2.30%</mark>	<mark>8.06%</mark>
Total activated cells	3640	16960	6447	13023	17785
Resolution (bit)	12	15	13	14	15
INL at 15GeV <mark>30%</mark> coupling efficiency	<mark>0.055%</mark>	<mark>3.75%</mark>	<mark>0.39%</mark>	<mark>2.74%</mark>	<mark>9.47%</mark>
Total activated cells	4367	20176	7729	15542	21047
Resolution (bit)	13	15	13	14	15

Incoming Particle energy	
(eV)	1.50E+10
Scintillator light yield	
(ph/eV)	1.50E-05
N photon / incoming	
particle	2.25E+05
Crystal surface area	
(mm2)	400
Nflux (ph/mm2)	563

$$N_{fired}(M, V, \lambda) = M \cdot \left\{ 1 - exp \left[-\frac{PDE(V, \lambda) \cdot N_{ph}}{M} \right] \right\}$$

$$INL = 1 - exp\left(-PDE.\frac{N_{fired}}{M}\right)$$

 N_{fired} = number of activated cells

M = total number of cells

 $PDE(V, \lambda) =$ photodetection efficiency $V = bias \ voltage, \lambda = photon \ wavelength$ $N_{ph} = number \ of \ incident \ photons$

Hamamatsu S14160-3015

- 3 mm x 3 mm active
- PDE <mark>32%</mark> (at 420 nm)
- 15 µm microcells
- Anode capacitance 530 pF
- Dark count rate 700 kcps (typ.)
- VOP variation within reel ±0.1V (± 8% gain)

- ≻16 pcs to fill 20 mm x 20 mm
- ➤Active fill: 36% of area
- Rough computation for # activated cells for 15GeV deposited in crystal: 5,160 (20% coupling eff.)
- Expected Integral Non-linearity at 15GeV: 0.26% (20% coupling eff.)

Measured fast timing (70ns FWHM)





Broadcom AFBR-S4N44C013

- 3.72 mm x 3.72 mm active
- PDE 43/55% (420 nm) (typ./perf.)
- 30 µm microcells
- Anode capacitance 990/760 pF (typ./perf.) slightly longer pulse
- Dark count rate 1660 kcps (typ.)



>16/25 pcs to fill 20 mm x 20 mm

Active fill: 55/86% of area

- Rough computation for # activated cells for 15GeV deposited in crystal: 10,476 (20% coupling eff.)
- Expected Integral Non-linearity at 15GeV: 1.85% (20% coupling eff.)

16 x S4N44C013

20 mm

5x5 matrix for area coverage is possible 86% active coverage (better than PMT)



Expected resolution with different SiPMs

- Use measured resolution from experiment as reference
- Compute relative signal level from change in PDE and active area
- Compute resolution change (1rst order scales with square root of signal)

	Hamamatsu 14160-3010	Hamamatsu 14160-3015	Hamamatsu 14160-6015	Hamamatsu 14160-6010	Broadcom AFBR S4N44C013	-Broadcom AFBR S4N44C013	-Broadcom AFBR- S4N44P014M	PMT Hamamatsu R4125 (19mm dia, 15mm cthode)			
configuration	4x4	4x4	2x2	2x2	4x4	5x5	4x4	1			
PDE (% 420nm)	17	30	30	17	43	43	63	27			
active fill (%)	36	36	36	36	55	86	54	71			
relative signal level (100%)	57	100	100	57	219	342	314	177	Predicted PMT resolution:		
expected resolution at 4.54 GeV (%)	2.86	2.15	2.15	2.86	1.45	1.16	1.21	1.62	1.59% at 4.7GeV Measurement: 1.5%		
expected resolution at 5.8 GeV (%)	2.27	1.71	1.71	2.27	1.16	0.92	0.96	1.28	3x3 PMT based detector measured at JLAB		
	Measured	at JLab w.	3x3 Crytur	prototype	2.0 pre	dicted					

Energy resolution: comparison with PMT



Summary table

	Hamamatsu 14160-3010	Hamamatsu 14160-3015	Hamamatsu 14160-6015	Hamamatsu 14160-6010	Broadcom AFBR- S4N44C013	Broadcom AFBR- S4N44C013	Broadcom AFBR- S4N44P014M	PMT Hamamatsu R4125 (19mm dia, 15mm cthode)
Cell pitch (µm)	10	15	15	10	30	30	40	15000
Capacitance (pF)	530	530	2500	2500	990/760	990/760	580	
PDE at 420nm (%)	17	30	30	30	43/55	43/55	63	27
configuration	4x4	4x4	2x2	2x2	4x4	5x5	4x4	1
PDE (% 420nm)	17	30	30	17	43	43	63	27
active fill (%)	36	36	36	36	55	86	54	71
relative signal level (100%)	57	100	100	57	219	342	314	177
expected resolution at 4.54 GeV (%)	<mark>2.86</mark>	<mark>2.15</mark>	<mark>2.15</mark>	<mark>2.86</mark>	1.45	<mark>1.16</mark>	<mark>1.21</mark>	<mark>1.62</mark>
expected resolution at 5.8 GeV (%)	<mark>2.27</mark>	<mark>1.71</mark>	<mark>1.71</mark>	<mark>2.27</mark>	<mark>1.16</mark>	0.92	<mark>0.96</mark>	<mark>1.28</mark>

PMT: 1.59% at 4.7GeV Measurement: 1.5%

Significant resolution improvement, slight pulse timing and NL tradeoff

Response linearity check, peak position vs beam energy

