Quark unpolarized transverse-momentum distribution functions of the pion Ydrefors, de Paula, TF, Salmè, e-Print: 2301.11599 [hep-ph]

T-even uTMD leading-twist from the quark-quark correlator Mulders \& Tangerman NPB461, 197 (1996)

$$
\begin{aligned}
& f_{1}^{q}(\gamma, \xi)=\frac{N_{c}}{4} \int d \phi_{\hat{\mathbf{k}}_{\perp}} \int_{-\infty}^{\infty} \frac{d y^{-} d \mathbf{y}_{\perp}}{2(2 \pi)^{3}} \\
& \times\left. e^{i\left[\xi P^{+} \frac{y^{-}}{2}-\mathbf{k}_{\perp} \cdot \mathbf{y}_{\perp}\right]}\langle P| \bar{\psi}_{q}\left(-\frac{y}{2}\right) \gamma^{+} \psi_{q}\left(\frac{y}{2}\right)|P\rangle\right|_{y^{+}=0}
\end{aligned} \gamma_{=\left|\mathbf{k}_{\perp}\right|^{2}}
$$



## Subleading-twist 3 uTMDs



$\xi e_{E o M}^{q}(\gamma, \xi)=\xi \tilde{e}^{q}(\gamma, \xi)+\frac{m}{M} f_{1 ; E o M}^{q}(\gamma, \xi)$
$\xi f_{E o M}^{q \perp}(\gamma, \xi)=\xi \tilde{f}^{q \perp}(\gamma, \xi)+f_{1 ; E o M}^{q}(\gamma, \xi), \quad$ Lorcé, Pasquini, Schweitzer, EPJ C 76, 415 (2016)

Gluon momentum in the pion

$$
|\pi\rangle=|q \bar{q}\rangle+|q \bar{q} g\rangle+|q \bar{q} 2 g\rangle+\cdots
$$

quark momentum distribution

$$
\begin{aligned}
& u^{q}(\xi)=\sum_{n=2}^{\infty}\left\{\prod_{i}^{n} \int \frac{d^{2} k_{i \perp}}{(2 \pi)^{2}} \int_{0}^{1} d \xi_{i}\right\} \\
& \times \delta\left(\xi-\xi_{1}\right) \delta\left(1-\sum_{i=1}^{n} \xi_{i}\right) \delta\left(\sum_{i=1}^{n} \mathbf{k}_{i \perp}\right) \\
& \times\left|\Psi_{n}\left(\xi_{1}, \mathbf{k}_{1 \perp}, \xi_{2}, \mathbf{k}_{2 \perp}, \ldots\right)\right|^{2}
\end{aligned}
$$

first-moment

$$
\begin{align*}
& \left\langle\xi_{q}\right\rangle=P_{v a l}\left\langle\xi_{q}\right\rangle_{v a l}+\sum_{n>2} P_{n}\left\langle\xi_{q}\right\rangle_{n} \\
& 0.471 \quad 0.5 \\
& =P_{\text {val }}\left\langle\xi_{q}\right\rangle_{v a l}+\left(1-P_{v a l}\right)\left\langle\xi_{q}\right\rangle_{H F S} \\
& \quad \mathrm{P}_{\text {val }}=0.3
\end{align*}
$$



$$
\left\langle\xi_{q}\right\rangle=\int_{0}^{1} d \xi \int_{0}^{\infty} d \gamma \xi f_{1}^{q}(\gamma, \xi)=0.471
$$

momentum sum-rule in the HFS

Gluons carry 6\% of the longitudinal momentum of the pion! @ the pion scale
Working now on the inclusion of quark self-energy in the BS equation in Minkowski...

