PDFs in the EIC Era Challenges and Opportunities for QCD

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Thanks for substantial input from my friends & colleagues







EIC Users Group Meeting Washington DC July 30 – Aug 1, 2018

... an important step



2018 Workshop on Probing Quark-Gluon Matter with Jets

On July 23, the National Academies released a study report backing the scientific case for building a U.S.-based electron-ion collider (EIC).

FYI AIP.org

EIC: An Ideal QCD Laboratory



"QCD is our most perfect physical theory"

Frank Wilczek



QCD is our most perfect physical theory

What QCD Tells Us About Nature - and Why We Should Listen. Frank Wilczek

In many respects, our most complex asymptotic freedom strong color confinement ... associated manifestations

Lessons: The Nature of Nature

"... alien, simple, beautiful, weird, & comprehensible"



Ideally suited to " ... glean the fundamental insights into QCD"

A few thoughts:

Nucleon Structure:

protons, hadrons, nuclear tomography, ...

Hadron/Parton Transition:

Higher Twist, many body, duality, ...





The QCD Parton Model

$$d\sigma = f_a(x) \otimes \widehat{\sigma}$$

Parameterized in terms of a single variable x, the momentum fraction ... use DGLAP to determine μ dependence

 $f_a(x)$... working in the limit of a spherical horse ...



Nuclear Structure



Higher Twist, many body problem, duality, hi-x, mass corrections ...



EIC can push these boundaries

These are hard problems

 $\bullet \quad \bullet \quad \bullet$

we need good ideas

Some Inspiration



Dan Amidei (UM) & Chip Brock (MSU) FermiNews January 17, 2003

Case Study: The Strange PDF







Puzzle: What is the Nuclear Correction



High Energy Insight: *W*/*Z Production at LHC and the strange PDF* ¹³



2018 CTEQ School Tutorial

ATLAS: Eur. Phys. J. C 77 (2017) 367

Add LHC Heavy Ion:





A. Kusina, et al., Eur. Phys. J. C77 (2017) no.7, 488

What's the Solution???



"... for the time being it is still appears advantageous to retain nuclear target data in the global dataset for general-purpose PDF determination"



Nuclear PDFs are **ESSENTIAL** for proton PDFs

Nuclear

PDFS

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Nuclear PDF

The Players The Ingredients

... selected NLO Nuclear PDF Fits



Nuclear PDFs: DIS, DY, π Prod, (new) Di-Jet



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Data sets & cuts for nPDF fits



proton vs nuclear: fewer data and more DOF ... impose assumptions on nPDFs

1) Multiplicative nuclear correction factors (HKN, EPPS, DSSZ)

$$f_i^{\mathbf{p}/\mathbf{A}}(x_N, Q_0) = R_i(x_N, Q_0, \mathbf{A}) f_i^{\mathbf{free \ proton}}(x_N, Q_0)$$

... for example

HKN

$$R_i(x, Q_0, \mathbf{A}) = 1 + \left(1 - \frac{1}{A^{\alpha}}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1 - x)^{\beta_i}}$$



2) Generalized A-parameterization (nCTEQ)

$$f_{i}^{p/A}(x_{N}, \mu_{0}) = f_{i}(x_{N}, A, \mu_{0})$$

$$f \sim \dots x^{c_{1}(A)}(1 - x)^{c_{2}(A)}\dots$$

$$c_{k} \sim c_{k,0} + c_{k,1}\left(1 - A^{-c_{k,2}}\right)$$
Proton Nuclear



use proton as a Boundary Condition

Nuclear PDFs: Complementary efforts in general agreement



Nuclear PDFs are more complex more DOF than Proton case more "issues" to consider more work to do ...



Make predictions for heavy ion collisions at:

RHIC (Al, Au, Cu, U, ...)

LHC (pPb, PbPb)



Differentiate flavors of free-proton PDFs:



Di-Jets

EPPS16 pp & pPb

EPPS16: Di-Jet Production



Impact of CMS 5.02 TeV dijet measurements on gluon PDFs – a preliminary view Kari J. Eskola, Petja Paakkinen, Hannu Paukkunen. 1806.08208

HI-X

Higher twist mass effects limit $x \rightarrow 1$

CJ Project

Challenges at Hi-x

Partonic structure at high-x

- Partonic structure of nucleons/nuclei at high-x (x>0.5) poorly known:
 - >50% uncertainty on d(x) at x>0.6
 - >50% uncertainty on g(x) at x>0.2
 - very large uncertainties on quark sea
- Better understanding provides tests of models of hadron structure
 - ▶ $d/u \rightarrow 1/2$: SU(6) Spin-Flavor symmetry
 - ► $d/u \rightarrow 0$: Scalar diquark dominance
 - ► $d/u \rightarrow 1/5$: pQCD power counting
 - Local quark hadron duality:

 ${
m d/u}
ightarrow rac{4 \mu_{
m n}^2 / \mu_{
m p}^2 - 1}{4 - \mu_{
m n}^2 / \mu_{
m p}^2} \simeq 0.42$

 Better understanding important for BSM searches of new heavy states

> Ingo Schienbein 2018 Trento Workshop

CJ15 global fit, PRD93(2016)114017



Challenges at Hi-x

d/u at large x

Claire Gwenlan: DIS2018

dv/uv distribution at Q² = 10 GeV² 0.9 NNPDF3.0 MMHT2014 ABM12 0.8 CJ15 (T=10) CJ15 (T=1.645) 0.7 LHeC 0.6 0.5 0.4 0.3 0.2 0.1 LHeC O. 0.2 0.3 0.5 0.6 0.7 0.8 0.9 0.4 Х

d/u essentially unknown at large x

no predictive power from current pdfs; conflicting theory pictures; data inconclusive, large nuclear uncerts.

with precision ep (n) data to v. large x: no nuclear corrections; relax assumptions



resolve long-standing mystery of d/u ratio at large x



Intrinsic Charm (IC)

Probe IC via charm contributions to DIS σ , F_L^C , or angular distributions





Gluons and the quark sea at high energies: distributions, polarization, tomography, D.Boer, et al., arXiv:1108.1713.

T. Stavreva, I. Schienbein, F. Arleo, K. Kovarik, F. Olness, J.Y. Yu, J.F. Owens, JHEP 1101 (2011) 152

Lattice



Lattice QCD input & constraints to PDFs



Progress in Particle and Nuclear Physics Volume 100, May 2018, Pages 107-160



Review

Workshop March 2017

Parton distributions and lattice QCD calculations: A community white paper Huey-Wen Lin ^{1, 2}, Emanuele R. Nocera ^{3, 4}, Fred Olness ⁵, Kostas Orginos ^{6, 7}, Juan Rojo ((editors)) ^{8, 9} $\stackrel{\odot}{\sim}$ Alberto Accardi ^{7, 10}, Constantia Alexandrou ^{11, 12}, Alessandro Bacchetta ¹³, Giuseppe Bozzi ¹³, Jiunn-Wei Chen ¹⁴, Sara Collins ¹⁵, Amanda Cooper-Sarkar ¹⁶, Martha Constantinou ¹⁷, Luigi Del Debbio ⁴, Michael Engelhardt ¹⁸, Jeremy Green ¹⁹, Rajan Gupta ²⁰,

Lucian A. Harland-Lang ^{3, 21} ... James Zanotti ³²



First Monte Carlo Global Analysis of Nucleon Transversity with Lattice QCD Constraints Huey-Wen Lin, W. Melnitchouk, Alexei Prokudin, N. Sato, H. Shows, Phys.Rev.Lett. 120 (2018) no.15, 152502

xFitter

xFitter release xfitter-2.0.0

xFitter/xFitterTalks » xFitter/../xFitterDevel.. » xFitter/../Meeting2017-.. » xFitter » xFitter/DownloadPage





Sample data files: LHC: ATLAS, CMS, LHCb Tevatron: CDF, D0 HERA: H1, ZEUS, Combined Fixed Target: ... User Supplied: ...



Features & Recent Updates:

xFitter

Photon PDF & QED Pole & MS-bar masses Profiling and Re-Weighting Heavy Quark Variable Treshold Improvements in χ^2 and correlations TMD PDFs (uPDFs) ... and many other



xFitter 2.0.0 FrozenFrog

Versatility of xFitter



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New Tools

PDFSense & & ... borrowing from AI



See Talk By: Tim Hobbs (SMU) A new measure:

Sensitivity S_f

Extend concept of correlation (C) to include both pull and precision of experiment.

(Technically, weight by scaled residual.)

New insights on experimental impacts

Linked from: https://metapdf.hepforge.org/

Artificial Intelligence Tools: Projector tool of Google TensorFlow



Dynamical projections for the visualization of PDFSense data Dianne Cook, Ursula Laa, German Valencia arXiv:1806.09742

nCTEQ++

... the motivation for nCTEQ



nCTEQ++ ... a complete rewrite in C++

Top level C++, modular structure, output to YAML & Python scripts Use external programs: Minuit, HOPPET, MCFM, APPLgrid, ...



nCTEQ++ ... can now access all MCFM Processes

MCFM Processes Library (v6.8)

MCFM: Vector boson pair production at the LHC, J. M.Campbell, R. K.Ellis and C.Williams, JHEP 1107, 018 (2011)

The APPLGRID Project: Tancredi Carli, Dan Clements, Amanda Cooper-Sarkar, Claire Gwenlan, Gavin P. Salam, Frank Siegert, Pavel Starovoitov, Mark Sutton. Eur.Phys.J. C66 (2010) 503-524

nproc	$f(p_1) + f(p_2) \to d$			Order) $H(\gamma(p_3) + \gamma(p_4)) + f(p_5) + f(p_6) $ m heavy top limit] 1 $H(b(p_3) + \bar{b}(p_4)) + f(p_5) + f(p_6)[$ m heavy top limit] 2 $H(\tau^-(p_3) + \tau^+(p_4)) + f(p_5) + f(p_6)[$ in heavy top limit] 3 $H(\tau^-(p_3) + \tau^+(p_4)) + f(r_5) + f(r_6)[$) $h(p_6) + h(r_6) + h(r_6)[$	NLO NLO NLO	$\begin{array}{l} 540 H(b(p_3) + \bar{b}(p_4)) + t(p_5) + q(p_6) \\ 541 H(b(p_3) + \bar{b}(p_4)) + \bar{t}(p_5) + q(p_6) \\ \end{array}$	NLO NLO
1	$W^+(\rightarrow \nu(p_3) + e^-)$	$^{+}(p_{4}))$		NLO	$\begin{array}{c} 1 & H(\rightarrow w \ (v_{fg}), e \ (p_{4}))w \ (e \ (p_{5}), v(p_{6})) + f(p_{7}) + f(p_{8}) \\ 1 & H(\rightarrow Z(e^{-}(p_{3}), e^{+}(p_{4}))Z(\mu^{-}(p_{5}), \mu^{+}(p_{6}))) + f(p_{7}) + f(p_{8}) \\ 1 & H(b(p_{3}) + \bar{b}(p_{4})) + f(p_{5}) + f(p_{6}) + f(p_{7}) [\text{in heavy top limit]} \\ 1 & H(e^{-}(p_{7}) + e^{-}(p_{7})) + f(p_{7}) + f(p_{7}) [\text{in heavy top limit]} \end{array}$	NLO LO	$544 H(b(p_3) + b(p_4)) + t(\nu(p_5) + e^+(p_6) + b(p_7)) + q(p_9)$ $547 H(b(p_3) + \bar{b}(p_4)) + \bar{t}(e^-(p_5) + \bar{\nu}(p_6) + b(p_7)) + q(p_9)$ $550 H(e_1) + e^-(p_1) + e^-(p_1) + e^-(p_1)$	NLO
6	$W^{-}(\rightarrow e^{-}(p_3) + i$	$\overline{\nu}(p_A))$		NLO	$\begin{array}{c} H(-\sqrt{y_2}) + \gamma(p_4) + \gamma(y_5) + f(p_6) + f(p_7)[\text{in nearly cop}] \\ H(-\sqrt{y_1}) + \gamma(p_3), e^+(p_4))W^-(e^-(p_5), \bar{\nu}(p_6))) + f(p_7) + f(p_8) + f(p_6) \\ H(-\sqrt{z}(e^-(p_3), e^+(p_4))Z(\mu^-(p_5), \mu^+(p_6))) + f(p_7) + f(p_8) + f(p_6) \\ H(-\sqrt{z}(p_3), e^+(p_4))Z(\mu^-(p_5), \mu^+(p_6))) + f(p_7) + f(p_8) + f(p_6) \end{array}$	LO LO	$\begin{array}{l} 550 & H(\gamma(p_3) + \gamma(p_4)) + \eta(p_5) + \eta(p_6) \\ 551 & H(\gamma(p_3) + \gamma(p_4)) + f(p_5) + q(p_6) \\ 554 & H(\gamma(p_3) + \gamma(p_4)) + f(y_{(2)}) + e^{+}(p_1) + h(p_2)) + g(p_2) \end{array}$	NLO
11	\mathbf{W}^+	(I +))		NIO	$\begin{array}{c} & \gamma & $	LO	$ \begin{array}{c} 504 \\ 557 \end{array} H(\gamma(p_3) + \gamma(p_4)) + \bar{t}(v(p_3) + \bar{v}(p_6) + \delta(p_7)) + q(p_9) \\ 557 \end{array} \\ \end{array} $	NLO
	$VV (\rightarrow \nu(p_3) + e)$	$(p_4)) + f(p_5)$		NLO	$\begin{array}{c} f(p_1) + f(p_2) \rightarrow \gamma(p_3) + \varsigma(p_4) \\ f(p_1) + f(p_2) \rightarrow \gamma(p_3) + \varsigma(p_4) \\ i + f(p_1) + f(p_2) \rightarrow \gamma(p_3) + \gamma(p_4) \end{array}$	LO NLO+F	$\begin{vmatrix} 560 \\ 561 \\ 7(e_{-}(p_{3}) + e_{+}(p_{4})) + t(p_{5}) + q(p_{6}) \\ \hline 561 \\ 7(e_{-}(p_{3}) + e_{+}(p_{3})) + \bar{t}(p_{5}) + q(p_{6}) \end{vmatrix}$	NLO
12	$W^+(\rightarrow \nu(n_2) + e^-)$	$(n_{4}) + \bar{b}(n_{5})$		NLO	$\begin{array}{c} \vdots & f(p_1) + f(p_2) \rightarrow \gamma(p_3) + \gamma(p_4) + f(p_5) \\ \hline f(p_1) + f(p_2) \rightarrow \gamma(p_3) + \gamma(p_4) + \gamma(p_5) \end{array}$	NLO+F NLO+F	$562 Z(e - (p_3) + e + (p_4)) + t(p_5) + q(p_6) + f(p_7)$ $562 Z(e - (p_3) + e + (p_4)) + t(p_5) + q(p_6) + f(p_7)$	LO
10	$(-\nu(p_3)+c)$	(P4)) + o(P3)		NIC) $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + \gamma(p_5)$) $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + \gamma(p_5) + f(p_6)$	NLO+F LO	$\begin{array}{c c} 563 & Z(e - (p_3) + e + (p_4)) + \bar{t}(p_5) + q(p_6) + f(p_7) \\ 564 & Z(e - (n_2) + e + (n_2)) + t(-)y(n_2) + e^{+}(n_2) + b(n_2)) + q(n_2) \end{array}$	LO
13	$W^+ (\rightarrow \nu(p_3) + e^-)$	$(p_4)) + \bar{c}(p_5)$		NLO	5 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + \gamma(p_5)$ 7 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + \gamma(p_5) + f(p_6)$	NLO+F LO	$\begin{array}{c} 504 \\ 566 \\ Z(e - (p_3) + e + (p_4)) + t(\rightarrow \nu(p_5) + e^-(p_6) + \delta(p_7)) + q(p_8) \\ f(p_6) + f(p_6) + f(p_6) + f(p_7)) + q(p_8) + f(p_9) \end{array}$	LO
14	$W^+(\rightarrow \nu(p_3) + e^-)$	(p_4) + $\bar{c}(p_5)$ [massless]		LO) $Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + \gamma(p_{5})$) $Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + \gamma(p_{5}) + \gamma(p_{6})$) $Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + \gamma(p_{5}) + f(p_{6})$	NLO+F NLO +F NLO + F	$\begin{array}{l} 567 Z(e-(p_3)+e+(p_4))+\bar{t}(\rightarrow e^-(p_5)+\bar{\nu}(p_6)+b(p_7))+q(p_8)\\ 569 Z(e-(p_3)+e+(p_4))+\bar{t}(\rightarrow e^-(p_5)+\bar{\nu}(p_6)+\bar{b}(p_7))+q(p_8)+f(p_9) \end{array}$	NLO LO
16	$W^{-}(\rightarrow e^{-}(n_{c}) + i$	$\overline{u}(n_1) \perp f(n_2)$		NLO	$\begin{array}{c} 3 & Z^{*0} \mapsto e^{-}(p_{3}) + e^{+}(p_{4})) + \gamma(p_{5}) + \gamma(p_{6}) + f(p_{7}) \\ 1 & Z^{0} (\to e^{-}(p_{3}) + e^{+}(p_{4})) + \gamma(p_{5}) + f(p_{6}) + f(p_{7}) \\ 1 & Z^{0} (\to 2(\neg e^{-}) + \overline{\varphi(e^{-})}) + \gamma(p_{5}) + \gamma(p_{5}) + f(p_{6}) + f(p_{7}) \end{array}$	LO LO	$\begin{array}{c} 601 & H(b(p_3) + b(p_4)) + H(\tau^-(p_5) + \tau^+(p_6)) \\ 602 & H(b(p_3) + \bar{b}(p_4)) + H(\gamma(p_5) + \gamma(p_6)) \end{array}$	LO
10	$W (\rightarrow c (p_3) + I)$	$V(P_4)) + J(P_5)$		NLO	$\begin{array}{c} J \\ Z^{*}(\rightarrow 3(\nu(p_{3}) + \bar{\nu}(p_{4}))) + \gamma(p_{5}) \\ J \\ Z^{0}(\rightarrow 3(\nu(p_{3}) + \bar{\nu}(p_{4}))) + \gamma(p_{5}) + \gamma(p_{6}) \\ J \\ Z^{0}(\rightarrow 3(\nu(p_{3}) + \bar{\nu}(p_{4}))) + \gamma(p_{5}) + f(p_{5}) \end{array}$	NLO + F	$\begin{bmatrix} 640 \\ t(p_3) + \bar{t}(p_4) + H(p_5) \\ 0 \end{bmatrix} = \bar{t}(p_3) + \bar{t}(p_3) + \bar{t}(p_3) = \bar{t}(p_3) + \bar{t}(p_3) + \bar{t}(p_3) = \bar{t}(p_3) + \bar{t}(p_3$	LO
17	$W^{-}(\rightarrow e^{-}(p_3) + i$	$\bar{\nu}(p_4)) + b(p_5)$		NLO	$\begin{array}{c} Z^{-}(\rightarrow)(\nu(p_{3}) + \bar{\nu}(p_{4})) + \gamma(p_{5}) + f(p_{6}) \\ Z^{0}(\rightarrow)(\nu(p_{3}) + \bar{\nu}(p_{4}))) + \gamma(p_{5}) + \gamma(p_{6}) + f(p_{7}) \\ \end{array}$	LO LO	$\begin{array}{c} b41 & t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + t(\rightarrow \nu(p_7) + e^-(p_8) + b(p_6)) + H(b(p_9) + b(2)) \\ 644 & t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_7)) + \overline{t}(\rightarrow \overline{q}(p_7) + q(p_8) + \overline{b}(p_6)) + H(b(p_9) + \overline{b}(p_7)) \\ \end{array}$	$p_{10})$ LO p_{10} LO
10	(10)	$(I \downarrow)$ $(I \downarrow)$		NIO	$\frac{1}{2} \frac{Z^{-}(\rightarrow (\nu(p_3) + \nu(p_3))) + \gamma(p_5) + f(p_6) + f(p_7)}{f(p_1) + b(p_2) - W^{+}(\rightarrow \nu(p_3) + e^+(p_4)) + b(p_5) + f(p_6)}$	LO	647 $t(\rightarrow q(p_3) + \bar{q}(p_4) + b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7) + e^-(p_8) + \bar{b}(p_5)) + H(b(p_9) + \bar{b}(p_7) + e^-(p_8) + \bar{b}(p_5)) + H(b(p_9) + \bar{b}(p_8) + \bar{b}(p_8)) + H(b(p_8) + \bar{b}(p_8) + \bar{b}(p_8) + \bar{b}(p_8)) + H(b(p_8) + \bar{b}(p_8) + \bar{b}(p_8$	η ₀)) LO
18	$W (\rightarrow e (p_3) + i)$	$\nu(p_4)) + c(p_5)$		NLO	$\frac{1}{1} \frac{f(p_1) + b(p_2) \to W}{f(p_1) + c(p_2) \to W'(\to e^-(p_3) + e^+(p_4)) + c(p_5) + f(p_6)}{\frac{1}{1} \frac{f(p_1) + c(p_2) \to W'(\to \psi(p_3) + e^+(p_4)) + c(p_5) + f(p_6)}{W'(\to \psi(p_3) + e^+(p_4)) + c(p_5) + f(p_6)}$	LO	$\begin{array}{c} 651 \\ 651 \\ t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7) + e^-(p_8) + b(p_6)) + H(\gamma(p_9) + \gamma(p_8) + b(p_8)) + H(\gamma(p_8) + \rho(p_8)) + H(\gamma(p_8) + h(p_8)) + H(\gamma(p_8) + h$	(p ₁₀)) LO
19	$W^{-}(\rightarrow e^{-}(n_{0}) + i$	$\overline{u}(n_{1}) + c(n_{2})$ [massless]		LO	$\frac{1}{2} \int f(p_1) + c(p_2) \rightarrow W (\rightarrow e(p_3) + \nu(p_4)) + c(p_5) + f(p_6)$ $\frac{1}{2} W^+(\rightarrow \nu(p_3) + e^+(p_4)) + c(p_5) + f(p_6)[\text{c-s interaction}]$ $W^-() = () + (-$	LO	$ \begin{array}{c} 657 \\ 657 \end{array} t (\rightarrow v (p_3) + \bar{v} (p_4) + b(p_5)) + \bar{t} (\rightarrow \bar{v} (p_7) + q_4 p_8) + \phi_4 p_6)) + H(\gamma (p_8) + \gamma (p_6)) \\ 657 \\ t (\rightarrow q (p_3) + \bar{q} (p_4) + b(p_5)) + \bar{t} (\rightarrow \bar{v} (p_7) + e^- (p_8) + \bar{b} (p_6)) + H(\gamma (p_9) + \gamma (p_8) + \phi_6)) \\ \end{array} $	$p_{10}))$ LO
$12 W^{+}(\rightarrow \nu(p_1))$	$e^{\tau(p_4) + \theta(p_5)}$ (, C (P3) 1	$ (p_4)) (c_{(a)} + c_{(a)} + c_{$	$ \cdot \cdot \cdot \cdot \cdot \cdot $ 129 $H(\rightarrow Z''(e^-(p3) + e^+(p4)) + Z''(\mu^-(p5) + \mu^+(p6))$ on	IV H, gg→ZZ IntL LO	$\frac{b}{ $	NLO	$\begin{array}{c c} 661 & t(\rightarrow \nu(p_3)e^+(p_4)b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_9, p_{10})W^-(p_{11}, p_{12})) \\ \hline \\ 661 & t(\rightarrow \nu(p_3)e^+(p_4)b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_9, p_{10})W^-(p_{11}, p_{12})) \\ \hline \\ 661 & t(\rightarrow \nu(p_3)e^+(p_4)b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_9, p_{10})W^-(p_{11}, p_{12})) \\ \hline \\ 661 & t(\rightarrow \nu(p_3)e^+(p_4)b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_9, p_{10})W^-(p_{11}, p_{12})) \\ \hline \\ \\ 661 & t(\rightarrow \nu(p_3)e^+(p_4)b(p_5)) + \bar{t}(\rightarrow \bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_9, p_{10})W^-(p_{11}, p_{12})) \\ \hline \\ \\ \\ \\ \\ \end{array}$	p ₁₂)) LO
13 $W^+(\rightarrow \nu(p_3) + W^+(\rightarrow \nu(p_3) + W^+(\rightarrow \nu(p_3) + W^+))$	$+e^+(p_4)) + \bar{c}(p_5)$ NLO $+e^+(p_4)) + \bar{c}(p_5)$ [massless] I.O	$ \begin{array}{c c} 107 & Z^0(\rightarrow 3 \times (\nu(p_3) + \bar{\nu}(p_4))) + H(\rightarrow W^+(\nu(p_5), e^+(p_6))W^-(e^-(p_7), \bar{\nu}(p_8))) \\ 108 & Z^0(\rightarrow b(p_3) + \bar{b}(p_4)) + H(\rightarrow W^+(\nu(p_5), e^+(p_6))W^-(e^-(p_7), \bar{\nu}(p_8))) \end{array} $	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	² and H,gg→ZZ intf.] LO (H + gg→ZZ) squared] LO	$\begin{array}{c} 342 f(p_1) + b(p_2) \rightarrow Z^{*}(\rightarrow e^{-}(p_3) + e^{+}(p_4)) + b(p_5) + f(p_6) + b(p_7) \\ 346 f(p_1) + b(p_2) \rightarrow Z^{0}(\rightarrow e^{-}(p_3) + e^{+}(p_4)) + b(p_5) + f(p_6) + f(p_7) \\ a = \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) + $	(REAL) LO	$\begin{array}{c} 667 \\ t(\rightarrow \nu(p_3)e^-(p_4)b(p_5)) + t(\rightarrow q(p_7)q(p_8)b(p_6)) + H(W^+(p_9,p_{10})W^-(p_{11},p_{12})) \\ t(\rightarrow q(p_4)\bar{q}(p_4)b(p_5)) + \bar{t} \rightarrow (\bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) + H(W^+(p_8,p_{10})W^-(p_{11},p_{12})) \\ t(\rightarrow q(p_4)\bar{q}(p_4)b(p_5)) + \bar{t} \rightarrow (\bar{\nu}(p_7)e^-(p_8)\bar{b}(p_6)) \\ t(\rightarrow q(p_4)\bar{q}(p_4)b(p_5)) \\ t(\rightarrow q(p_4)\bar{q}(p_4)b(p_5)b(p_5)) \\ t(\rightarrow q(p_4)\bar{q}(p_4)b(p_5)b$	(2)) LO (2)) LO
16 $W^{-}(\rightarrow e^{-}(p_{3}))$ $W^{-}(\rightarrow e^{-}(p_{3}))$	$+ \bar{\nu}(p_4) + f(p_5)$ NLO $+ \bar{\nu}(p_4) + f(p_5)$ NLO	$\frac{109}{111} \frac{Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + H(\rightarrow Z(e^{-}(p_{5}), e^{+}(p_{6})) + Z(\mu^{-}(p_{7}), \mu^{+}(p_{8})))}{111} \frac{111}{H(\rightarrow b(p_{3}) + b(p_{4}))}$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$) squared LO ps, exact LO	$\frac{347}{51} \frac{f(p_1) + o(p_2) \to Z^{\circ}(\to e^-(p_3)) + \delta^{4}e^+(p_4)) + o(p_5) + f(p_6) + o(p_7)}{251} \frac{f(p_1) + o(p_1) \to Z^{0}(\to e^-(p_1) + o^+(p_1)) + o(p_2) + f(p_1) + f(p_2)}{251}$			
18 $W^-(\rightarrow e^-(p_3))$ 19 $W^-(\rightarrow e^-(p_3))$	$+ \bar{\nu}(p_4)) + c(p_5)$ $+ \bar{\nu}(p_4)) + c(p_5)$ $+ \bar{\nu}(p_4)) + c(p_5)$ I.O	112 $H(\rightarrow \tau^{-}(p_{3}) + \tau^{+}(p_{4}))$ 113 $H(\rightarrow W^{+}(\nu(p_{3}) + e^{+}(p_{4})) + W^{-}(e^{-}(p_{5}) + \bar{\nu}(p_{6})))$	NLO $1311 = e^{-(p3)} + e^{+(p4)} + \nu_e(p5) + \nu_e(p6)$ [gg only, (h + gg - $1321 = e^{-(p3)} + e^{+(p4)} + \nu_e(p5) + \bar{\nu}_e(p6)$ [gg $\rightarrow ZZ$ squared $1282 = H(\rightarrow e^{-(p3)} + e^{+(p4)} + \nu_e(p5) + \bar{\nu}_e(p6)$ [m bottom [d]	LO LO LO	$\begin{array}{c} 351 & f(p_1) + c(p_2) \rightarrow Z & (-e^-(p_3) + e^-(p_4)) + c(p_3) + f(p_6) + f(p_7) \\ 352 & f(p_1) + c(p_2) \rightarrow Z^0 (-e^-(p_3) + e^+(p_4)) + c(p_3) + f(p_6) [+\bar{e}(p_7)] \\ \end{array}$	(REAL)	800 $V \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5)$ [Vector Mediator] 801 $A \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5)$ [Axial Vector Mediator]	NLO NLO
$\frac{13}{20}$ $W^+(\rightarrow \nu(p_3) + \frac{13}{21})$ $W^+(\rightarrow \nu(p_3) + \frac{13}{21})$	$+ e^+(p_4)) + e(p_5)$ [massive] NLO $+ e^+(p_4)) + b(p_5) + b(p_6)$ [massive] NLO	114 $H \rightarrow W^+(\nu(p_3) + e^+(p_4)) + W^-(q(p_5) + \bar{q}(p_6)))$ 115 $H \rightarrow W^+(\nu(p_3) + e^+(p_4)) + W^-(q(p_5) + \bar{q}(p_6)))$ [rad in.dk]	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	[Z) squared] LO LO	$\begin{array}{c} 356 f(p_1) + c(p_2) \rightarrow Z''(\rightarrow e^-(p_3) + e^-(p_4)) + c(p_5) + f(p_6) + f(p_7) \\ 357 f(p_1) + c(p_2) \rightarrow Z^0(\rightarrow e^-(p_3) + e^+(p_4)) + c(p_5) + f(p_6) + \bar{c}(p_7) \end{array}$	LO	802 $S \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5)$ [Scalar Mediator]	NLO
21 $W^+(\rightarrow \nu(p_3) +$ $W^+(\rightarrow \nu(p_3) +$	$+ e^+(p_4)) + \delta(p_5) + \delta(p_6)$ NLO + $e^+(p_4)) + f(p_5) + f(p_6)$ NLO	116 $H (\rightarrow Z^0(e^-(p_3) + e^+(p_4)) + Z^0(\mu^-(p_5) + \mu^+(p_6))$ 117 $H (\rightarrow Z^0(3 \times (\nu(p_3) + \bar{\nu}(p_4))) + Z^0(\mu^-(p_5) + \mu^+(p_6))$	NLO NLO NLO 133 $H(\rightarrow Z^0(e^-(p_3) + e^+(p_4)) + Z^0(\mu^-(p_5) + \mu^+(p_6) + f_1)$ 136 $H(\rightarrow b(p_3) + b(p_4)) + b(p_5)(+g(p_6))$	(p7)) [intf,no p ₇ cut] LO NLO	$\begin{vmatrix} 361 \\ c(p_1) + \bar{s}(p_2) \rightarrow W^+(\rightarrow \nu(p_3) + e^+(p_4)) mc=0 \text{ in NLO} \end{vmatrix}$ $\begin{vmatrix} 362 \\ c(p_1) + \bar{s}(p_3) \rightarrow W^+(\rightarrow \nu(p_3) + e^+(p_4)) massless corrections only \end{vmatrix}$	NLO	803 $PS \rightarrow (\chi(p_3) + \chi(p_4)) + f(p_5)$ [Pseudo Scalar Mediator] 804 $GG \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5)$ [Gluonic DM operator]	NLO
23 24 $W^+(\rightarrow \nu(p_3) + W^+(\rightarrow \nu(p_3) + W^+(\rightarrow \nu(p_3) + W^+))$	$+e^+(p_4)) + f(p_5) + \bar{f}(p_6) + f(p_7)$ $+e^+(p_4)) + b(p_5) + \bar{b}(p_6) + f(p_7)$ LO	118 $H (\rightarrow Z^o(\mu^-(p_3) + \mu^+(p_4)) + Z^o(b(p_5) + b(p_6))$ 119 $H (\rightarrow \gamma(p_3) + \gamma(p_4))$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	(REAL) (REAL)	$c(p_1) + \bar{s}(p_2) \rightarrow W^+(\rightarrow \nu(p_3) + e^+(p_4))$ [massive charm in real]	NLO	805 $S(\chi(p_3) + \bar{\chi}(p_4)) + f(p_5)$ [Scalar Mediator, mt loops]	NLO
25 $W^-(\rightarrow e^-(p_3))$ 26 $W^-(\rightarrow e^-(p_3))$	$+ \bar{\nu}(p_4)) + b(p_5) + b(p_6)$ [massive] NLO $+ \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6)$ NLO	$\begin{array}{ccc} 120 & H (\rightarrow Z^{\circ}(\mu^{-}(p_{3}) + \mu^{+}(p_{4})) + \gamma(p_{5})) \\ 121 & H (\rightarrow Z^{0}(3 \times (\nu(p_{3}) + \bar{\nu}(p_{4})))) + \gamma(p_{5})) \end{array}$	NLO NLO 141 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b (p_6) + e^-(p_7))$	$+ \bar{\nu}(p_8))$ NLO	$\begin{array}{cccc} 370 & W^*(\rightarrow b(p_3) + e^*(p_4)) + \gamma(p_5) + \gamma(p_6) \\ 371 & W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + \gamma(p_5) + \gamma(p_6) \end{array}$	LO	820 $V \rightarrow (\chi(p_3) + \chi(p_4)) + \gamma(p_5)$ [Vector Mediator] 821 $A \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5)$ [Axial Vector Mediator]	NLO + F NLO + F
27 $W^-(\rightarrow e^-(p_3))$ 28 $W^-(\rightarrow e^-(p_3))$	$+ \bar{\nu}(p_4)) + f(p_5) + f(p_6)$ $+ \bar{\nu}(p_4)) + f(p_5) + f(p_6) + f(p_7)$ NLO LO	56 $Z^0(\rightarrow e^-(p_3) + e^+(p_4)) + c(p_5) + \bar{c}(p_6)$	NLO $142 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + 143 t(\rightarrow \nu(p_6) + e^+(p_6) + e^+(p_6) + b(p_6) + e^+(p_6) + e^+(p_6$	$+ \overline{\nu}(p_8))$ [rad.in.dk] NLO $+ \overline{\nu}(p_8)) + f(p_9)$ LO	$\begin{array}{l} 401 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + b(p_5) & [1,2 \text{ or } 3 \text{ jets}, 4\text{FNS}] \\ 402 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + (b + \overline{b})(p_5) & [1 \text{ or } 2 \text{ jets}, 4\text{FNS}] \end{array}$	NLO	822 $S \rightarrow (\chi(p_3) + \overline{\chi}(p_4)) + \gamma(p_5)$ [Scalar Mediator]	NLO + F
29 $W^-(\rightarrow e^-(p_3))$ 31 $Z^0(\rightarrow e^-(p_3))$	$+ \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6) + f(p_7)$ LO	$\begin{array}{c} 61 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + W^-(\rightarrow e^-(p_5) + \bar{\nu}(p_6)) \\ 62 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + W^-(\rightarrow q(p_5) + \bar{q}(p_6)) \end{array}$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$+ \bar{\nu}(p_8)$) (uncorr) NLO $+ \bar{\nu}(p_8)$) [rad.in.dk],uncorr NLO	403 $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + b(p_5) + \bar{b}(p_6)$ [2 or 3 jets, 4FNS]	NLO	823 $PS \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5)$ Pseudo Scalar Mediator] 840 $V \rightarrow (\chi(p_5) + \bar{\chi}(p_5)) + f(p_5) + f(p_5)$ [Vector Mediator]	NLO + F
32 $Z^0(\rightarrow 3 \times (\nu))$	$(p_4)(p_4)(p_4)))$ NLO	63 $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + W^-(\rightarrow q(p_5) + \bar{q}(p_6))$ [rad.in.dk] 64 $W^-(\rightarrow e^-(p_3) + \bar{e}(p_3)) W^+(\rightarrow q(p_5) + \bar{q}(p_6))$]	NLO 146 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b(p_6) + q(p_7) + 147)$ $t(\rightarrow \nu(p_4) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b(p_6) + q(p_7) + 147)$	$\bar{q}(p_8)$) NLO $\bar{q}(p_8)$) [rad.in.top.dk] NLO	$\begin{array}{l} 406 & W^{-}(\rightarrow e^{-}(p_{3}) + \bar{\nu}(p_{4})) + b(p_{5}) & [1, 2 \text{ or } 3 \text{ jets}, 4\text{FNS}] \\ 407 & W^{-}(\rightarrow e^{-}(p_{3}) + \bar{\nu}(p_{4})) + (b + \bar{b})(p_{5}) & [1 \text{ or } 2 \text{ jets}, 4\text{FNS}] \end{array}$	NLO	841 $A \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5) + f(p_6)$ [Axial Vector Mediator]	LO
$\begin{array}{ccc} 33 \\ 34 \end{array} & \begin{array}{c} Z^0(\rightarrow b(p_3) + \\ Z^0(\rightarrow 3 \times (d) \mu) \end{array}$	$b(p_4))$ NLO $p_5) + \bar{d}(p_6)))$ NLO	$\begin{array}{cccc} 64 & W & (\rightarrow e^-(p_3) + \bar{\nu}(p_4))W & (\rightarrow q(p_5) + \bar{q}(p_6)) \\ 65 & W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4))W^+(\rightarrow q(p_5) + \bar{q}(p_6))[\text{rad.in.dk}] \end{array}$	NLO 148 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b(p_6) + q(p_7) + 149 t(\rightarrow q(p_3) + \bar{q}(p_1) + b(p_3)) + \bar{t}(\rightarrow b(p_3) + e^-(p_2) + e^-(p_3) + e^-(p_3$	$\bar{q}(p_8)$ [rad.in.W.dk] NLO $\bar{v}(p_e)$ NLO	408 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + \bar{b}(p_6)$ [2 or 3 jets, 4FNS]	NLO	842 $S \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5) + f(p_6)$ [Scalar Mediator]	LO
35 $Z^0(\rightarrow 2 \times (u))$ $Z \rightarrow t(\rightarrow u)$	p_5 + $\bar{u}(p_6)$)) + $e^+(p_1) + b(p_2)$ + $\bar{t}(\rightarrow \bar{b}(p_2) + e^-(p_2) + \bar{\nu}(p_2))$ I.O	$\begin{array}{c} 66 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + W^-(\rightarrow e^-(p_5) + \bar{\nu}(p_6)) + f(p_7) \\ 69 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + W^-(\rightarrow e^-(p_5) + \bar{\nu}(p_6)) [\text{no pol}] \end{array}$	LO LO LO 150 $t(\rightarrow q(p_3) + \bar{q}(p_4) + b(p_5)) + \bar{t}(\rightarrow b(p_6) + e^-(p_7) + \bar{t}(\rightarrow b(p_6) + \bar{t}(\rightarrow b(p_6) + e^-(p_7) + \bar{t}(\rightarrow b(p_6) + \bar{t}(\rightarrow b(p_6) + e^-(p_7) + \bar{t}(\rightarrow b(p_6) + \bar{t}(\rightarrow b(p_6$	$\bar{\nu}(p_8)$ [rad.in.top.dk] NLO $\bar{\nu}(p_8)$ [rad.in W db] NLO	411 $f(p_1) + b(p_2) \rightarrow W^-(\rightarrow \nu(p_3) + e^-(p_4)) + b(p_5) + f(p_6)$ [5FNS] 416 $f(p_1) + b(p_2) \rightarrow W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + f(p_6)$ [5FNS]	NLO	843 $PS \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5) + f(p_6)$ [Pseudo Scalar Mediator] 844 $GG \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + f(p_5) + f(p_6)$ [Gluonic DM operator]	LO
41 $Z^0(\rightarrow e^-(p_3) +$	$+e^+(p_4)) + f(p_5)) + e^{(-p_6)} + e^{(-p_1)} + p_{(p_8)})$ NLO	71 $W^+(\rightarrow \nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow e^-(p_5) + e^+(p_6))$ 72 $W^+(\rightarrow \nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 3 \times (\nu_e(p_5) + \bar{\nu}_e(p_6)))$	NLO NLO NLO 157 $t\bar{t}[for total Xsect]$ NLO	v(pg)) [rannin w.uk] NLO	$\begin{array}{c} 421 & W^+(\rightarrow \nu(p_3) + e^+(p_4)) + b(p_3) & [1,2 \text{ or } 3 \text{ jets}, 4\text{FNS}+5\text{FNS}] \\ 426 & W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_3)) + b(p_3) & [1,2 \text{ or } 2 \text{ jets}, 4\text{FNS}+5\text{FNS}] \end{array}$	NLO	845 $V \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5) + f(p_6)$ [Vector Mediator]	LO
42 $Z_0 (\rightarrow 3 \times (\nu))$ 43 $Z^0 (\rightarrow b(p_3) + $	$\bar{b}(p_4)) + f(p_5)$ NLO $\bar{b}(p_4)) + f(p_5)$ NLO	73 $W^+(\rightarrow \nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow b(p_5) + \bar{b}(p_6))$ 74 $W^+(\rightarrow \nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 3 \times (d(p_1) + \bar{d}(p_1)))$	NLO 159 cc[for total Xsect]	NLO	$\frac{420}{431} \frac{W^+(\rightarrow \nu(p_3) + \nu(p_4)) + b(p_5)}{W^+(\rightarrow \nu(p_3) + e^+(p_4)) + b(p_5) + b(p_6) + f(p_7)} $ [massive]	LO	846 $A \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5) + f(p_6)$ [Axial Vector Mediator] 847 $S \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5) + f(p_6)$ [Scalar Mediator]	LO
44 $Z^0(\rightarrow e^-(p_3) + Z^0(\rightarrow e^-(p_3) + Z$	$+e^+(p_4)) + f(p_5) + f(p_6)$ NLO $+e^+(p_4)) + f(p_5) + f(p_6) + f(p_7)$ LO	$\begin{array}{c} 75 \\ 75 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 75 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 75 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 75 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 75 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 80 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 80 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ 80 \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_3) + \mu^+(p_4) + \mu^+(p_4)) + Z^0(\rightarrow 2 \times (u(p_5) + \bar{u}(p_6))) \\ W^+(\rightarrow\nu(p_4) + \mu^+(p_4) + \mu^+(p_4) + \mu^+(p_4)) \\ W^+(\rightarrow\nu(p_4) + \mu^+(p_4) + \mu^+(p_4)) + Z^0(\rightarrow\nu(p_4) + \mu^+(p_4)) \\ W^+(\rightarrow\nu(p_4) + \mu^+(p_4) + \mu^+(p_4)) + Z^0(\rightarrow\nu(p_4) + \mu^+(p_4)) \\ W^+(\rightarrow\nu(p_4) + \mu^+(p_4) + \mu^+(p_4)) \\ W^+(\rightarrow\nu(p_4) + \mu^+(p_4) + \mu^+(p$	NLO 100 $tt + g[tor total Asect]$ NLO 161 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + q(p_6)[t-channel]$	NLO	$\frac{436}{500} \frac{W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + b(p_5) + b(p_6) + f(p_7) \text{ [massive]}}{W^+(\rightarrow \nu(p_3) + e^+(p_4)) + t(p_5) + \bar{t}(p_6) \text{ [massive]}}$	LO	848 $PS \rightarrow (\chi(p_3) + \bar{\chi}(p_4)) + \gamma(p_5) + f(p_6)$ [Pseudo Scalar Mediator]	LO
46 $Z^0(\rightarrow 3 \times (\nu))$ 47 $Z^0(\rightarrow 3 \times (\nu))$	$p_3) + \bar{\nu}(p_4)) + f(p_5) + f(p_6)$ NLO $p_4) + \bar{\nu}(p_4)) + f(p_7) + f(p_7) + f(p_7)$ LO	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	NLO 162 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + q(p_6)[decay]$ NLO 163 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + q(p_6)[t-channel]mb >$	0 NLO	$ 501 t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{t}(\rightarrow b(p_6) + e^-(p_7) + \bar{\nu}(p_8)) + W^+(\nu(p_9), \mu^+(p_7)) + \bar{t}(\rightarrow b(p_7) + \bar{t}(\rightarrow b(p_7)) + $	p ₁₀)) NLO	902 Check of Volume of 2 particle phase space	
$50 Z^0(\rightarrow e^-(p_3) + 2)$	$+e^+(p_4)) + b(p_5) + b(p_6)$ [massive] LO	78 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + Z^0(\rightarrow b(p_5) + b(p_6))$ 79 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + Z^0(\rightarrow 3 \times (d(p_5) + \tilde{d}(p_6)))$	NLO 166 $t(\rightarrow e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + q(p_6)[t-\text{channel}]$ NLO 167 $\bar{t}(\rightarrow e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + q(p_6)[\text{rad.in.dk}]$	NLO NLO	502 (same as process 501 but with radiation in decay) 503 $t(→ ν(p_3) + e^+(p_4) + b(p_3)) + \bar{t}(→ b (p_6) + q(p_7) + q (p_8)) + W^+(ν(p_9), µ^+(p_7))$	10)) NLO	903 Check of Volume of 3 particle phase space 904 Check of Volume of 4 particle phase space	
51 $Z^0(\rightarrow e^-(p_3) + Z_0(\rightarrow 3 \times (\nu p_3))$	$+e^+(p_4)) + b(p_5) + b(p_6)$ NLO $b_3) + \bar{\nu}(p_4))) + b(p_5) + \bar{b}(p_6)$ NLO	$\frac{80}{81} \frac{W^{-}(\rightarrow e^{-}(p_{3}) + \bar{\nu}(p_{4})) + Z^{0}(\rightarrow 2 \times (u(p_{5}) + \bar{u}(p_{6})))}{W^{-}(\alpha + e^{+}(p_{3})) + Z^{0}(\rightarrow \mu^{-}(p_{5}) + \mu^{+}(p_{5}))}$	NLO 168 $\bar{t}(\rightarrow e^-(p_3) + \bar{\nu}(p_4) + b(p_5)) + q(p_6)[t-channel]mb >$ 171 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + b(p_6))[s-channel]$	0 NLO NLO	$\frac{506}{t(\rightarrow q(p_3) + q(p_4) + b(p_5))} + \bar{t}(\rightarrow b(p_6) + e^-(p_7) + \bar{\nu}(p_8)) + W^+(\nu(p_9), \mu^+(p_{12})) + \bar{t}(p_{12}) + $	10)) NLO	905 Check of Volume of 5 particle phase space	
53 $Z^0(\rightarrow b(p_3) + Z^0(\rightarrow e^-(p_2) + Z^0(\rightarrow e^-(p_2)))$	$\bar{b}(p_4)) + b(p_5) + \bar{b}(p_6)$ NLO + $e^+(p_4)) + b(p_6) + \bar{b}(p_6) + f(p_7)$ LO	$\begin{array}{c} 81 \\ 82 \\ \hline \\ 82 \\ \hline \\ 82 \\ \hline \\ 82 \\ \hline \\ 80 \\ \hline \\ 90 \\ \hline 90$	NLO NLO 172 $t(\rightarrow \nu(p_3) + e^+(p_4) + b(p_5)) + \bar{b}(p_6))[\text{decay}]$ 176 $\bar{t}(\rightarrow e^-(p_1) + \bar{\nu}(p_3) + \bar{b}(p_5)) + b(p_6))[\text{s-channel}]$	NLO NLO	$ \begin{array}{c} 510 & W & (\rightarrow e^{-}(p_3) + \nu(p_4)) + v(p_5) + i(\phi_6) (\text{massave}) \\ 511 & t(\rightarrow \nu(p_3) + e^{+}(p_4) + b(p_5)) + \bar{t}(\rightarrow b^{-}(p_5) + e^{-}(p_7) + \bar{\nu}(p_8)) + W^{-}(\mu^{-}(p_9), \bar{\nu}(p_6)) \\ \end{array} $	p ₁₀)) NLO	906 Check of Volume of 6 particle phase space 008 Check of Volume of 8 particle phase space	
	70	$\begin{array}{l} 83 Z^{\circ}(\rightarrow e^{-}(p_{3})+e^{+}(p_{4}))+Z^{\circ}(\rightarrow b(p_{5})+b(p_{6}))\\ 84 Z^{0}(\rightarrow b(p_{3})+\bar{b}(p_{4}))+Z^{0}(\rightarrow 3\times (\nu(p_{5})+\bar{\nu}(p_{6})))\\ \end{array}$	NLO NLO 1777 $\bar{t}(\rightarrow e^-(p_3) + \bar{\nu}(p_4) + \bar{b}(p_5)) + b(p_6))$ [rad.in.dk] 180 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + t(q_7)$	NLO	512 (same as process 511 but with radiation in decay) 513 $t(\rightarrow \nu(p_0) + e^+(p_0) + h(p_1)) + \bar{t}(\rightarrow h(p_0) + a(p_0) + a(p_0)) + W^-(\mu^-(p_0))\bar{\nu}(p_0)$	NLO NLO	909 Check of Volume of 8 particle masse space 909 Check of Volume of 4 particle massive phase space	
		85 $Z^{0}(\rightarrow e^{-}(p_{3}) + e^{+}(p_{4})) + Z^{0}(\rightarrow 3 \times (\nu(p_{5}) + \bar{\nu}(p_{6}))) + f(p_{7})$ 86 $Z^{0}(\rightarrow \mu^{-}(p_{3}) + \mu^{+}(p_{4})) + Z^{0}(\rightarrow e^{-}(p_{5}) + e^{+}(p_{6}))[\text{no gamma}^{*}]$	LO NLO $V^{-}(-e^{-}(p_3) + \bar{\nu}(p_4)) + t(\nu(p_5) + e^+(p_6) + b(p_7))$ $V^{-}(-e^{-}(p_3) + \bar{\nu}(p_4)) + t(\nu(p_5) + e^+(p_6) + b(p_7))$	NLO NLO	$516 t(\rightarrow q(p_3) + q \ (p_4) + b(p_5)) + \bar{t}(\rightarrow b \ (p_6) + e^-(p_7) + \bar{\nu}(p_8)) + W^-(\mu^-(p_9), \bar{\nu}(p_8)) + W^-(\mu^-(p_9), \bar{\nu}(p_8)) + W^-(\mu^-(p_8), \bar{\mu}(p_8)) + W^-(\mu^-(p_8)) + W^-(\mu^-(p_8)) + W^-(\mu^-(p_8$	10)) NLO	910 Check of Volume of 3 particle (2 massive) phase space	
		$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	NLO 183 $W^-(\rightarrow e^-(p_3) + \bar{v}(p_4)) + t(v(p_3) + e^-(p_6) + b(p_7))$ NLO 183 $W^-(\rightarrow e^-(p_3) + \bar{v}(p_4)) + t(v(p_3) + e^+(p_6) + b(p_7))$ NLO 184 $W^-(\rightarrow e^-(p_3) + \bar{v}(p_4)) + t(v(p_3) + e^+(p_6) + b(p_7))$	$+b(p_8)$ LO	$\begin{vmatrix} 529 \\ 530 \end{vmatrix} \mathcal{L}^{-}(\rightarrow e^{-}(p_{3}) + e^{-}(p_{4})) + t(p_{3}) + t(p_{6}) \\ 530 \end{vmatrix} t(\rightarrow \nu(p_{3}) + e^{+}(p_{4}) + b(p_{5})) + \overline{t}(\rightarrow e^{-}(p_{7}) + \overline{\nu}(p_{8}) + b(p_{6})) + Z(e^{-}(p_{8}), e^{+}(p_{1})) + \overline{t}(p_{1}) + \overline{t}(p_{2}) + \overline{t}(p_{2}) + \overline{t}(p_{3}) + \overline{t}$	(0)) LO	911 Uneck of Volume of 5 particle W+t (with decay) massive phase space 912 Check of Volume of 5 particle W+t (no decay) massive phase space	
		$\begin{array}{c} 89 \\ 89 \\ 00 \\ 70 \\ 70 \\ 70 \\ 70 \\ 70 \\ 70 \\ 7$	NLO NLO 185 $W^+(\rightarrow \nu(p_3) + \nu(p_4)) + \bar{\iota}(p_5) + b(p_6)$ [massive b] 185 $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + \bar{\iota}(p_5)$	NLO	$\begin{bmatrix} 531 \\ t(\rightarrow \nu(p_3) + e^+(\bar{p}_4) + b(\bar{p}_5)) + \bar{t}(\rightarrow e^-(\bar{p}_7) + \bar{\nu}(\bar{p}_8) + b(\bar{p}_6)) + Z(b(\bar{p}_9), b(\bar{p}_{10}) \\ t(\rightarrow \nu(p_3) + e^+(\bar{p}_3) + b(\bar{p}_3)) + \bar{t}(\rightarrow e^-(\bar{p}_7) + \bar{\nu}(\bar{p}_8) + b(\bar{p}_8)) + Z(e^-(\bar{p}_7) + e^+(\bar{p}_8) + b(\bar{p}_8)) + Z(e^-(\bar{p}_7) + e^+(\bar{p}_8) + e^+(p$) LO	913 Check of Volume of 5 particle W+t+g (in decay) massive phase space	
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\frac{1810}{\text{NLO}} = \frac{180}{187} \frac{W^+(\rightarrow \nu(p_3) + e^+(p_4)) + t(e^-(p_5) + \bar{\nu}(p_6) + b(p_7))}{W^+(\rightarrow \nu(p_3) + e^+(p_4)) + \bar{t}(e^-(p_5) + \bar{\nu}(p_6) + \bar{b}(p_7))}$	rad.in.dk] NLO	$\begin{bmatrix} 0 \\ 5 \\ 5 \\ 5 \\ 5 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0$)) LO	914 Check of Volume of 5 particle W+t+g (in production) massive phase space	.e
		$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	NLO NLO					
		94 $W^+(\rightarrow \nu(p_3) + e^+(p_4)) + H(\rightarrow \gamma(p_5) + \gamma(p_6)$ 96 $W^-(\rightarrow e^-(p_3) + \bar{\nu}(p_4)) + H(\rightarrow b(p_5) + \bar{b}(p_6))$	NLO NLO					
		97 $W^{-}(\rightarrow e^{-}(p_{3}) + \bar{\nu}(p_{4})) + H(\rightarrow W^{+}(\nu(p_{3}), e^{+}(p_{6}))W^{-}(e^{-}(p_{7}), \bar{\nu}(p_{8})))$ 98 $W^{-}(\rightarrow e^{-}(p_{3}) + \bar{\nu}(p_{3})) + H(\rightarrow Z(e^{-}(p_{3}), e^{+}(p_{3})) + Z(e^{-}(p_{3}), e^{+}(p_{3})))$	NLO					
		$\begin{array}{c} 0 \\ 99 \end{array} \begin{array}{l} W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + H (\to 2(e^-(p_5), e^-(p_6)) + Z(\mu^-(p_7), \mu^-(p_8))) \\ W^-(\to e^-(p_3) + \bar{\nu}(p_4)) + H (\to \gamma(p_5) + \gamma(p_6)) \end{array}$	NLO					

Conclusion

EIC an ideal QCD Laboratory

"QCD is our most perfect physical theory" Frank Wilczek

"EIC would unlock scientific mysteries" NAP Report

Ideally suited to " ... glean the fundamental insights into QCD"

