



Compact Photon Source for Hall D.

Design and simulation using FLUKA at $5 \mu\text{A}$ electron beam ($3.1 \times 10^{13} \text{ s}^{-1}$), FWHM=2.5 mm.

For KLF Collaboration

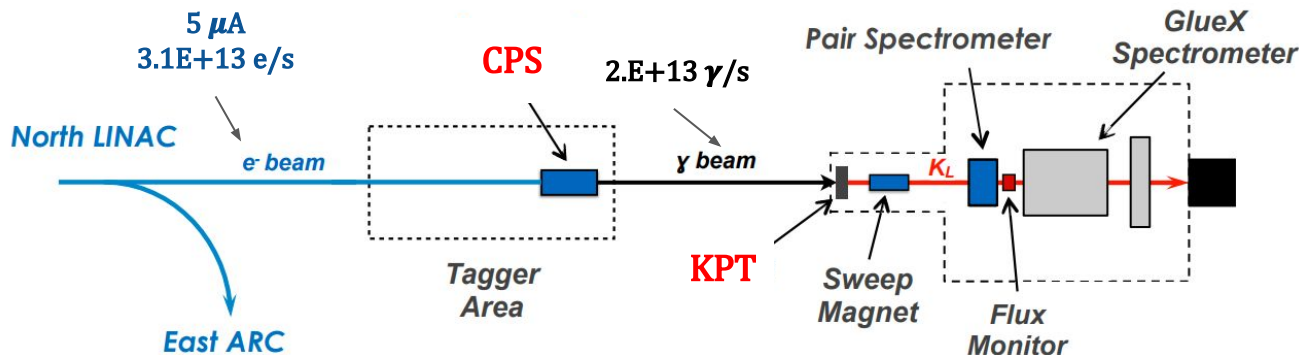
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02/03/2023.

Outline for the upcoming CPS Review

1. CPS in Experiment and FLUKA model. Location, Design, Performance, Alignment.
2. **Very High Radiation and Temperature inside CPS.**
3. Photon **Beam Quality.**
4. **Radiation** in CPS bending Magnet **and its Lifetime.**
5. Prompt **Dose and Activation** around CPS.
6. Tritium **Contamination** in Soil and Cooling Waters.
7. **Lifetime of various materials.**
8. Conclusion and Outlook.

CPS as a part of the Secondary K_L Beam in Hall D

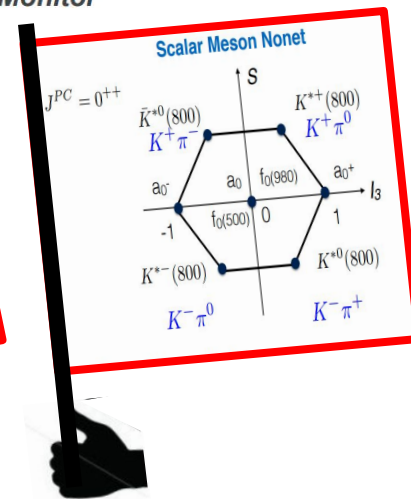
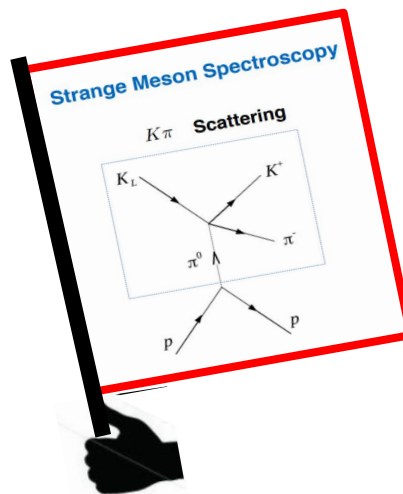


Strange Hadron Spectroscopy
with Secondary K_L beam in Hall D

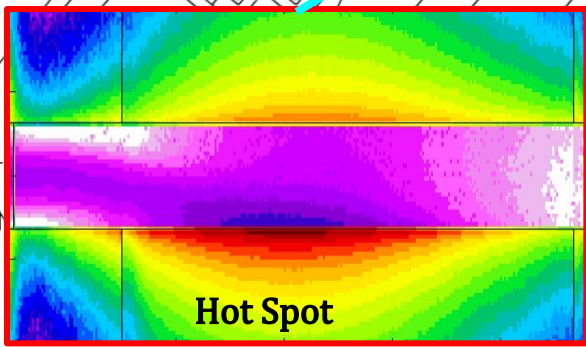
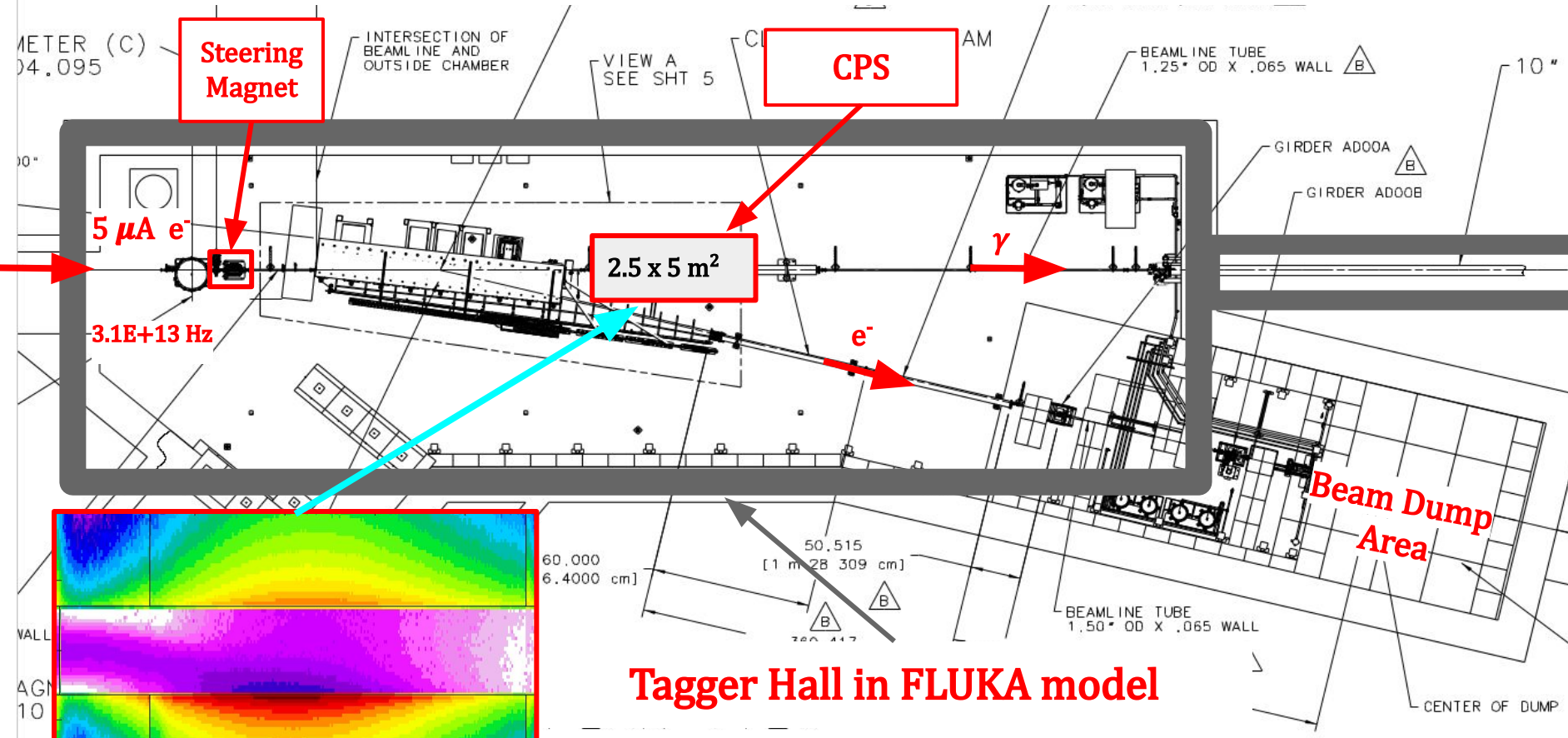


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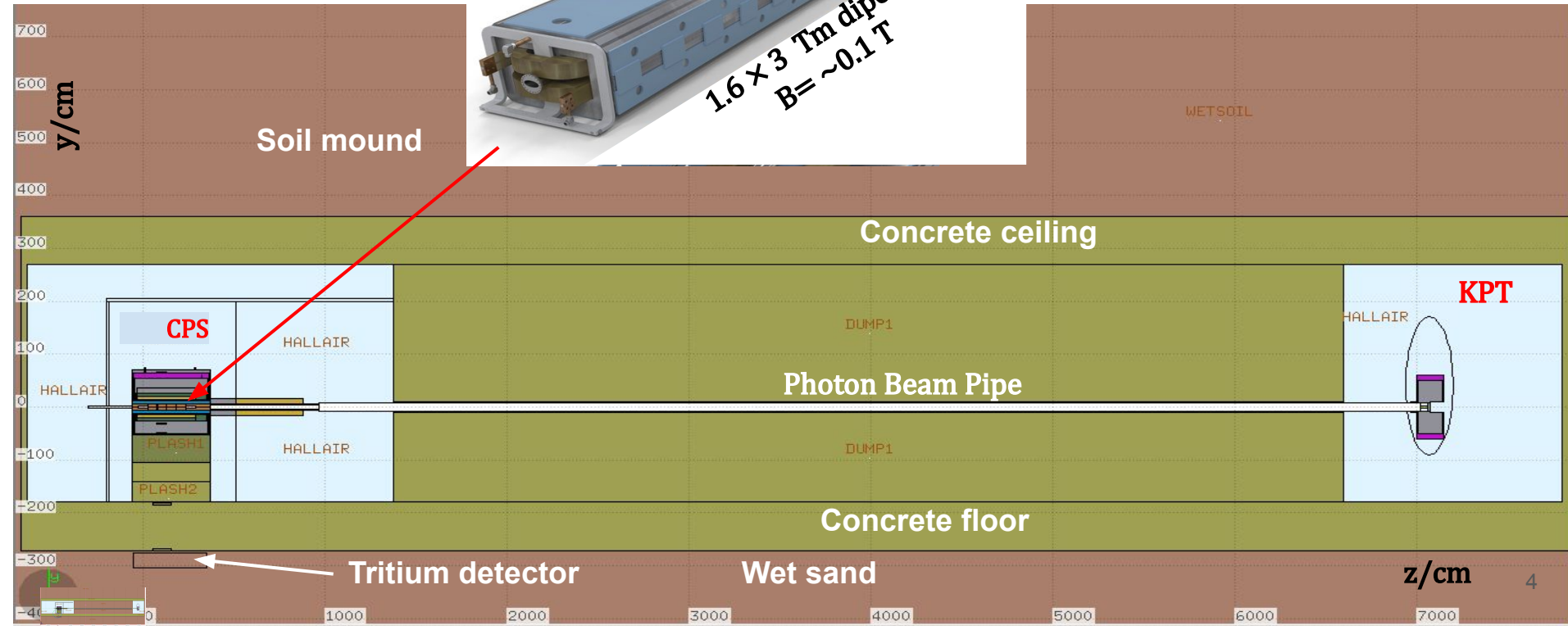
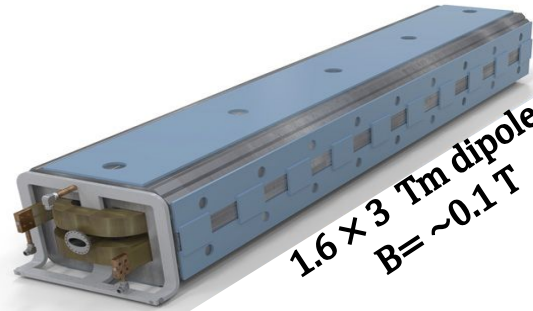


CPS location in Tagger Hall. Beam $5 \mu\text{A}$, Gaussian, FWHM=2.5 mm.

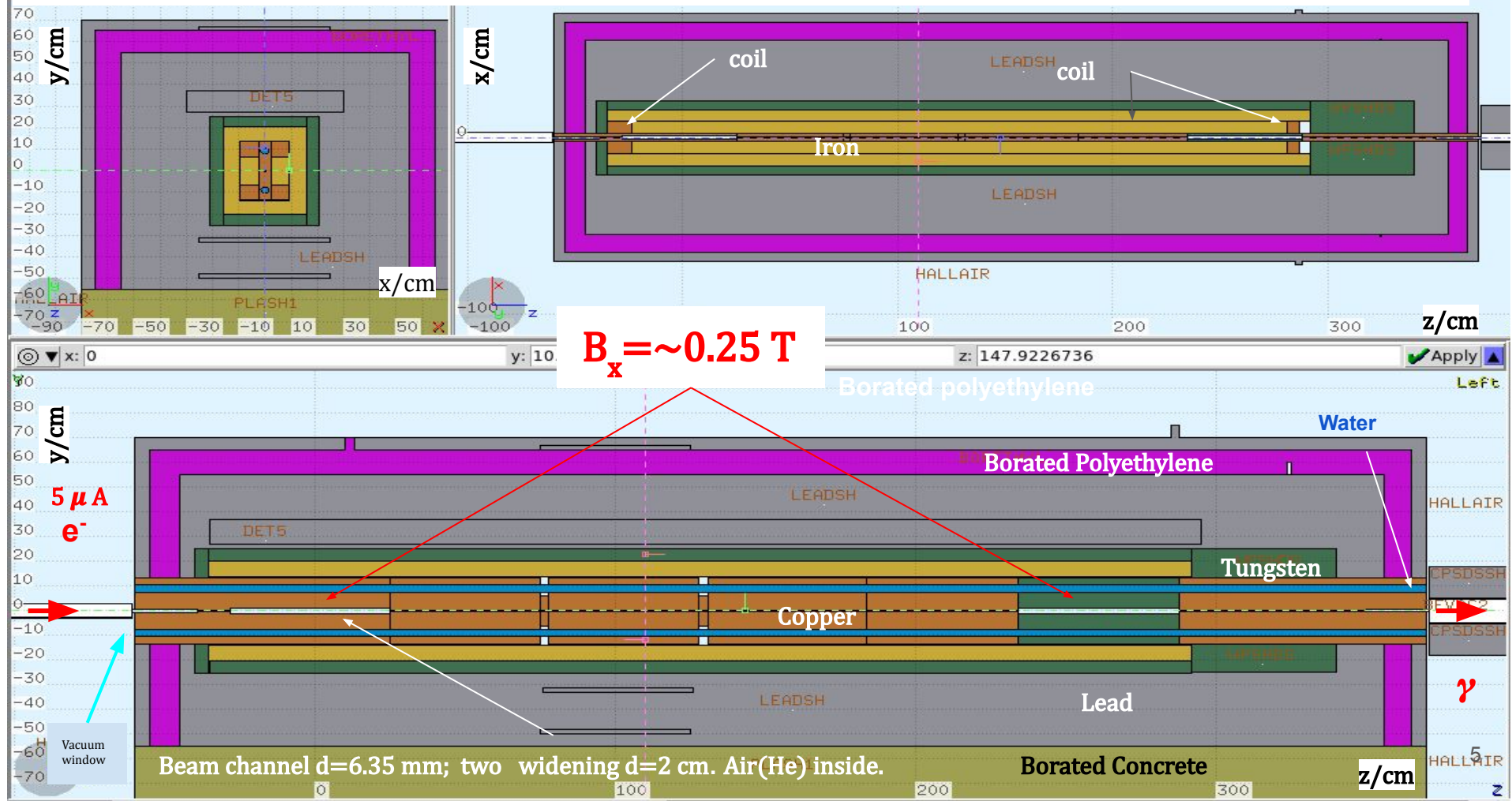


Tagger Hall in FLUKA model

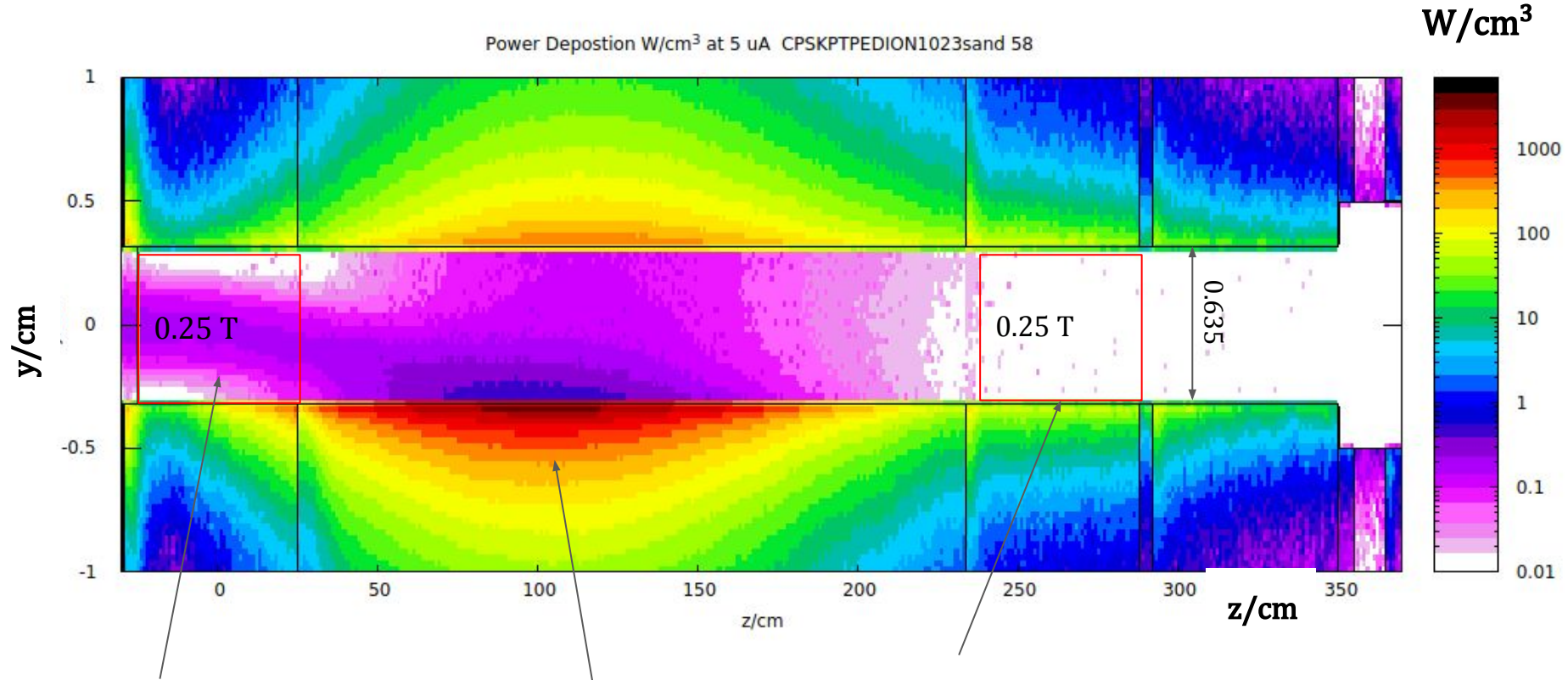
CPS, Tagger Hall, KPT and Magnet prototype in FLUKA model.



CPS in FLUKA: Magnet Yoke/platform, Two Coils, Cu Absorber, and 4 shield layers.

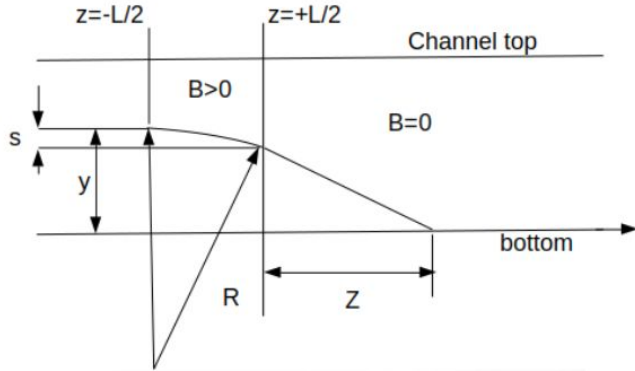


Source of radiation. Hot spot in the absorber. Power deposition



- Upstream magnet forms the Hot Spot; Downstream - cleans the photon beam.
- The **wider** is the Hot Spot - **the lower** is deposited power/temperature in the maximum.

Magnetic Field, Beam Channel, and Hot Spot Size.



z - counts from $L/2$ - coil area length, where $B > 0$.

z' - counts from $z = 0$.

L_M - length of **Beam Channel and Absorber**.

$\langle z' \rangle = L_M/2$ is constrained to be in the middle of Channel.

From two triangles on this figure we find:

$$\begin{aligned} (R - s)^2 + L^2 &= R^2, \quad \Rightarrow \quad s \approx \frac{L^2}{2R}, \\ \frac{L}{R - y} &= \frac{y - s}{z}, \\ z &\approx \frac{R}{L}(y - s) = \frac{R}{L}y - \frac{L}{2}, \\ \langle z' \rangle &\approx \langle y \rangle \frac{R}{L}, \\ \text{rms}(z') &\approx \text{rms}(y) \frac{R}{L} = \langle z' \rangle \frac{\text{rms}(y)}{\langle y \rangle}. \end{aligned}$$

$$\text{rms}(z') = 2 \langle z' \rangle \frac{\text{rms}(y)}{d} = \frac{L_M}{d} \text{rms}(y)$$

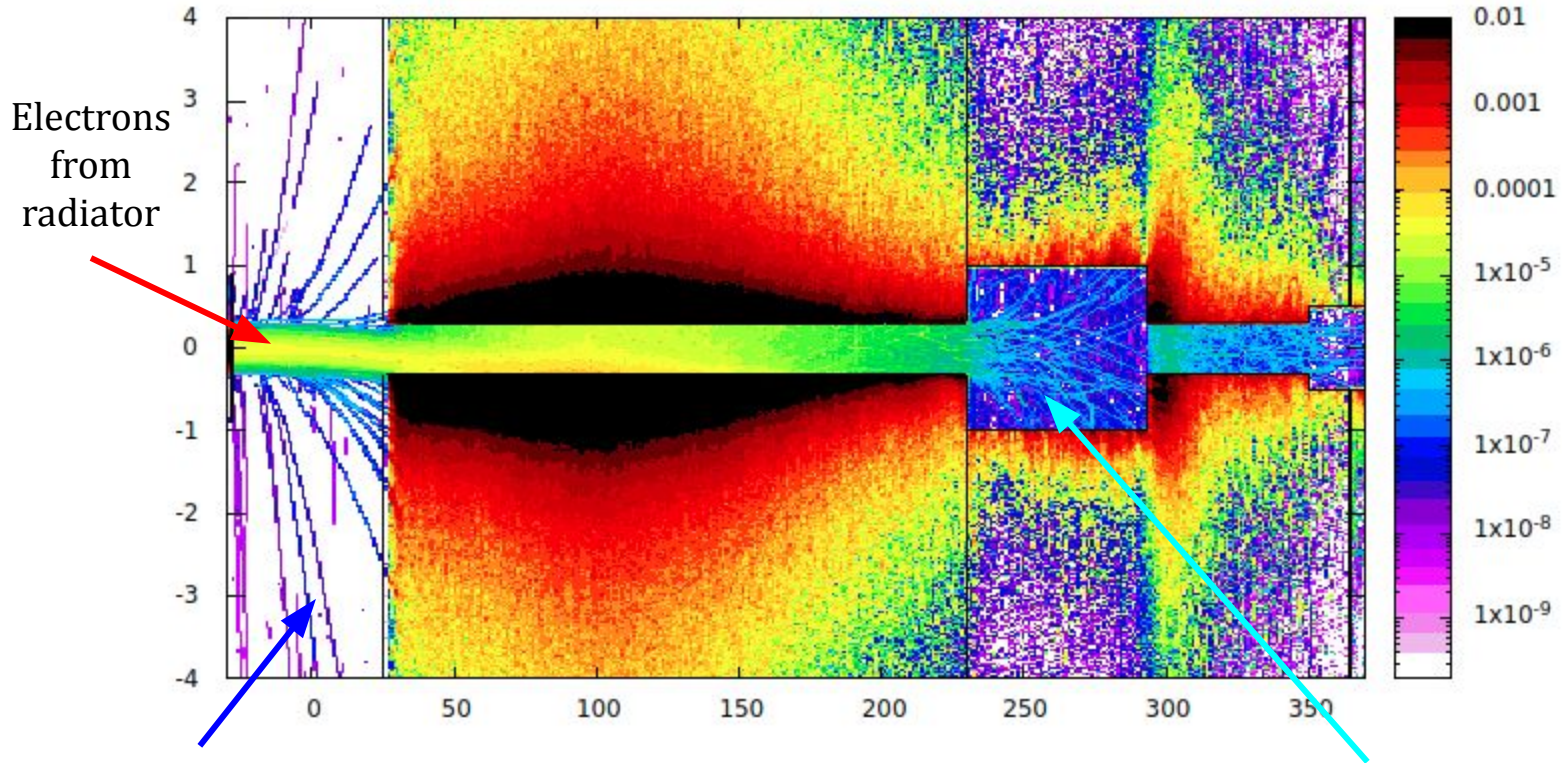
Constrain $\alpha \text{rms}(y) = d$, where $\alpha > 1$.

Then $\text{rms}(z') = \alpha^{-1} L_M$

- At given **beam rms(y)** for a **lower** specific power & temperature **do** :
- **Reduce** channel diameter, but keep $d > d_{\min} \approx 2 \text{rms}(y)$, otherwise beam tails hit Channel.
- **Increase** beam channel length L_M (\Rightarrow lower field B , simple magnet).

Magnet at CPS exit cleans photon beam.

USRBIN CPSKPTLEAD1712narrGUNvacTRP 58



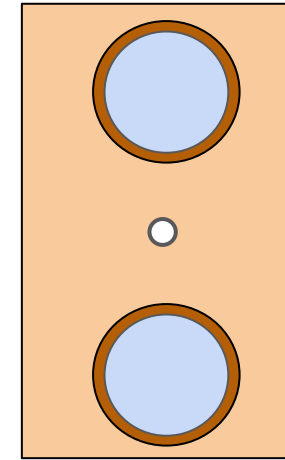
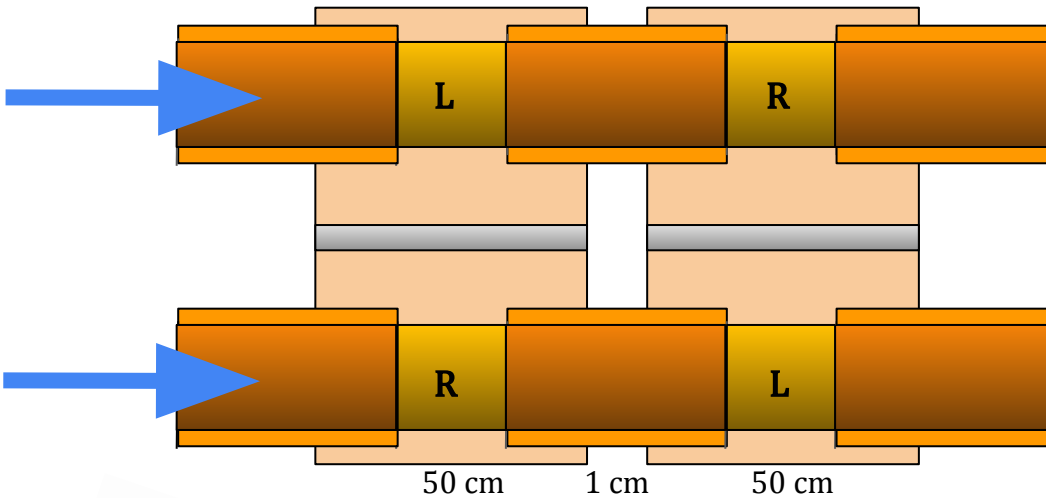
CPS Components. Weight and Cost.

CPS Component	Material	Density (g/cm ³)	Cost (\$/kg)	Weight (MetricT)	Total Cost (\$)
Absorb. In/Out	W	16.3	80.00	0.2	15,500
Lead skin	Pb	11.4	5.8	15.1	87,500
Plastic shield	Borated PE	1.2	20.5	0.5	10,100
Lead shield	Pb	11.4	5.8	36.5	211,400
Left shield	W	16.3	80.0	1.4	108,000
Top shield	W	16.3	80.0	0.8	67,000
Right shield	W	16.3	80.0	1.4	108,000
Bottom shield	W	16.3	80.0	0.8	67,000
Magnet	Fe	7.9	50.0	2.0	101,800
Absorber	Cu	9.0	122.6	0.2	27,400
Upstream shield	W/Cu	15.2	140.0	0.2	21,600
Downstream shield	W/Cu	15.2	140.0	1.2	171,400
CPS				60.9	894,100
Total tungsten				5.8	543,200

- CPS weight - 61,000 kg.
- CPS cost without magnet - \$793,000.
- Including Tungsten cost - \$543,000.

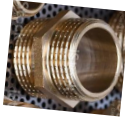
CPS Absorber and Alignment.

Segmented Copper Absorber - possible solution.



23 cm

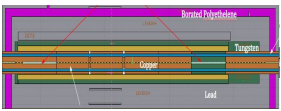
4.4 cm



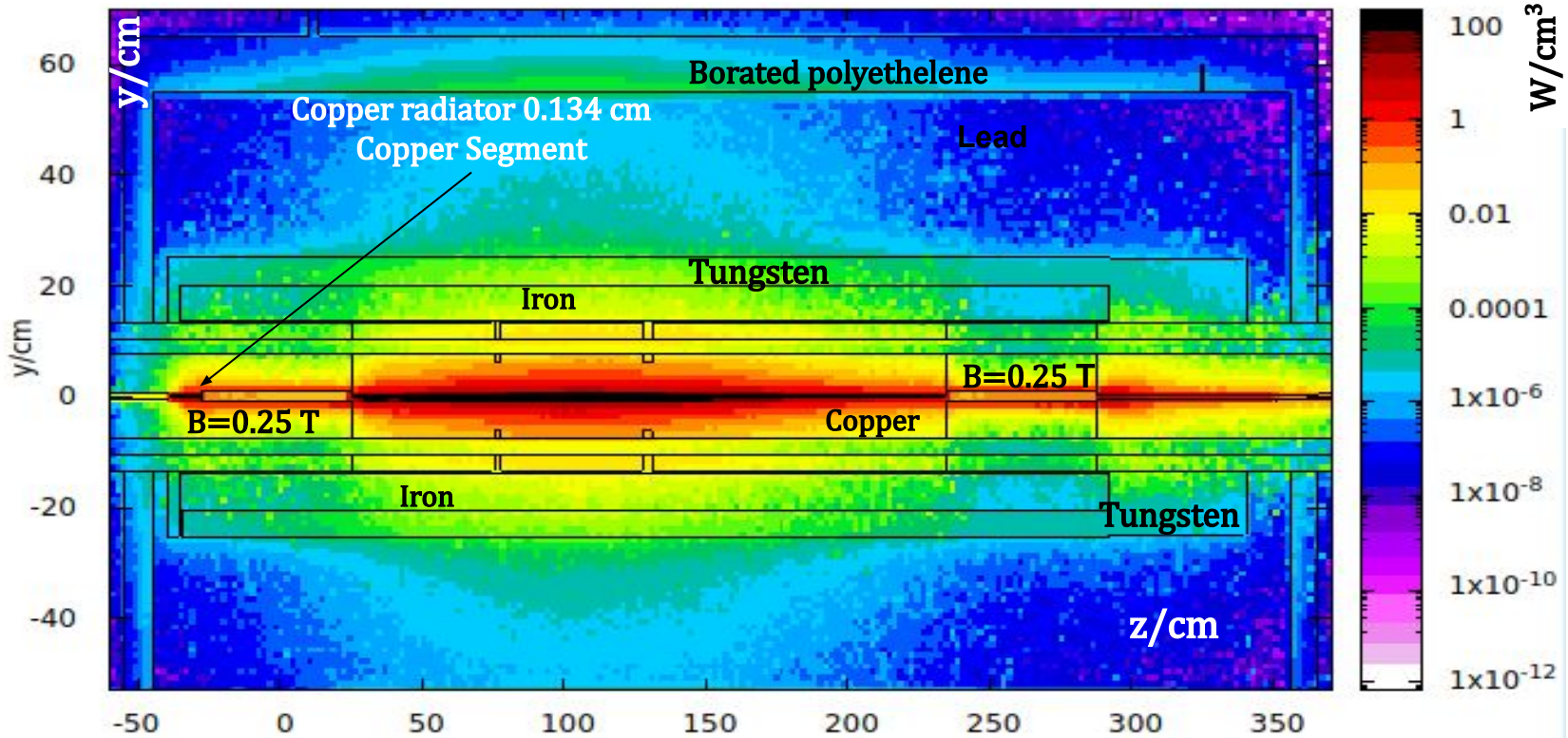
L R

- Segments $\sim 4.4 \times 20 \times 50 \text{ cm}^3$, **round beam hole:** \Rightarrow (1) no problem of thermal contact between 2 parts and (2) may be vacuumized.
- Segments are connected by fittings with **left/right-hand** threads; may be brazed.
- Provides direct **copper-water contact** inside segments: \Rightarrow no interface; better cooling.

Energy deposition
and
Temperature of CPS components.



Power Deposition in $-0.5 < x/cm < 0.5$ layer. Coarse mesh.



- Protruding **copper segment** around Radiator to mitigate lead overheating.
- T^0 -calculations **in progress**. Channel widening in coil area - to **reduce dose** rates.

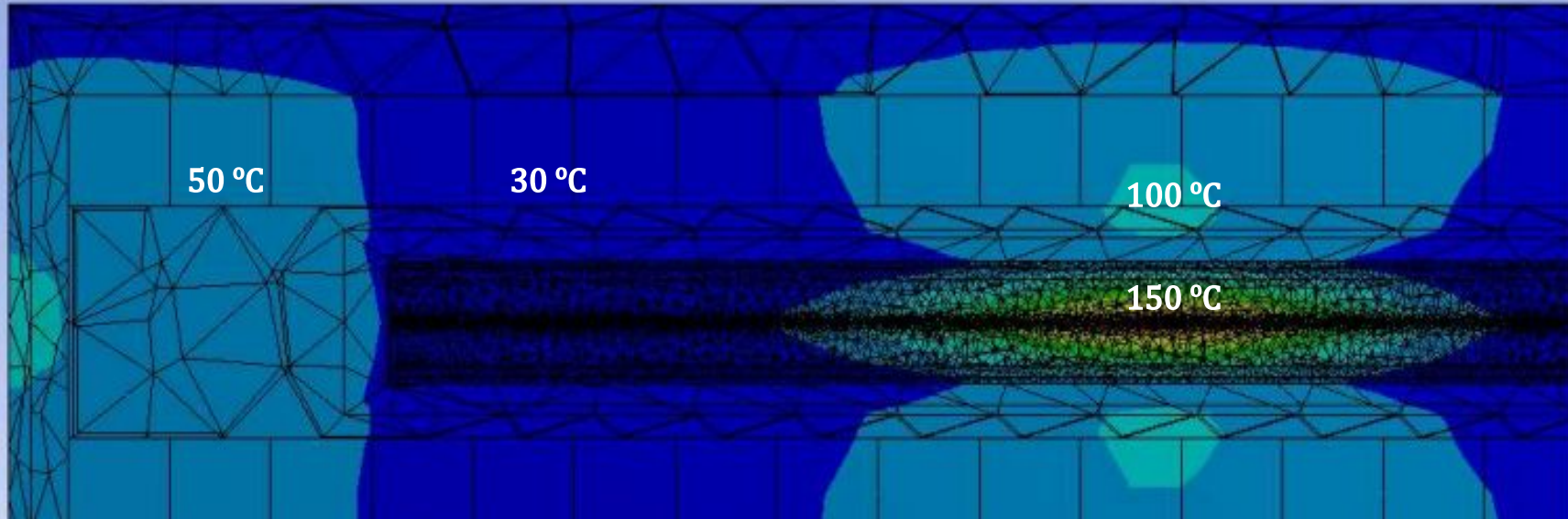
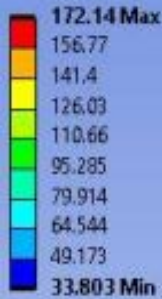
Power breakdown between CPS components .

CPS part	GeV/e	kW/5 μ A
DS Shield (W)	0.063	0.316
US Shield (W)	0.033	0.163
Side Shield (W)	0.013	0.064
Top Water Pipe	0.001	0.005
Bottom Pipe	0.001	0.006
Magnet Pole Right	0.322	1.610
Magnet Pole Left	0.321	1.619
Coils	0.058	0.289
Magnet Yoke	0.101	0.504
Lead Shield	0.006	0.032
Polyethylene (B)	0.002	0.011
Lead Skin	0.001	0.004
Converter (Cu)	0.002	0.010
Total	0.923	4.620

Segment	GeV/e	kW/5 μ A
1 W/Cu	0.230	1.151
2	2.013	10.077
3	4.743	23.744
4	2.034	10.183
5	0.385	1.929
6 W/Cu	0.164	0.822
Radiator	0.002	0.010
Total	9.571	47.916

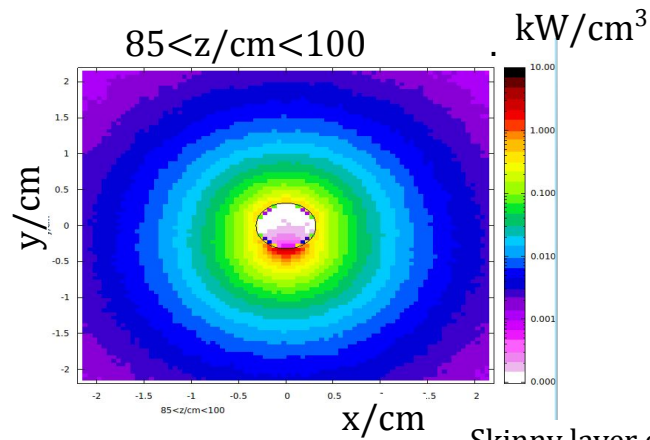
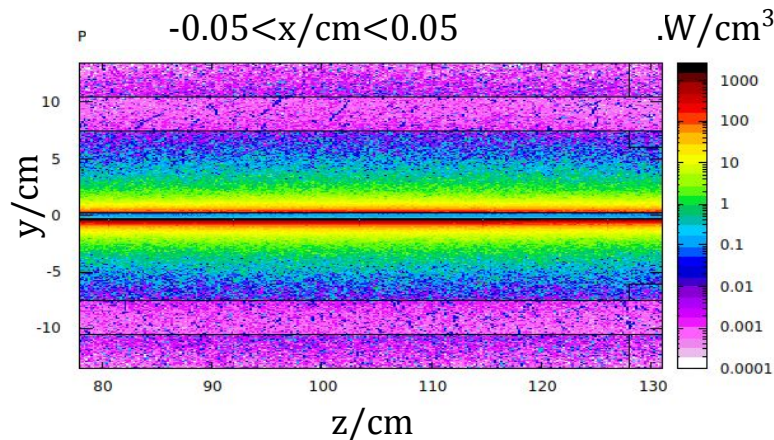
- **Total deposition 53 kW out of 60 kW of e-beam.**

Temperature field in the entire CPS at perfect thermal contact. For poor thermal contact - in progress.

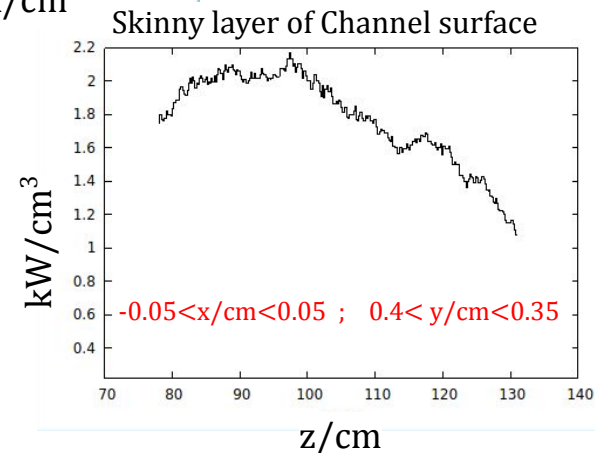


- Copper ($T_m=1084^\circ\text{C}$) in Absorber Channel **does not melt**: $T < 250^\circ\text{C}$.
- Lead ($T_m=327^\circ\text{C}$) and Iron ($T_m=1538^\circ\text{C}$) temperatures - below melting points: $T < 100^\circ\text{C}$? and 150°C .

Power Deposition in Hot Segment . Fine mesh 0.05 cm

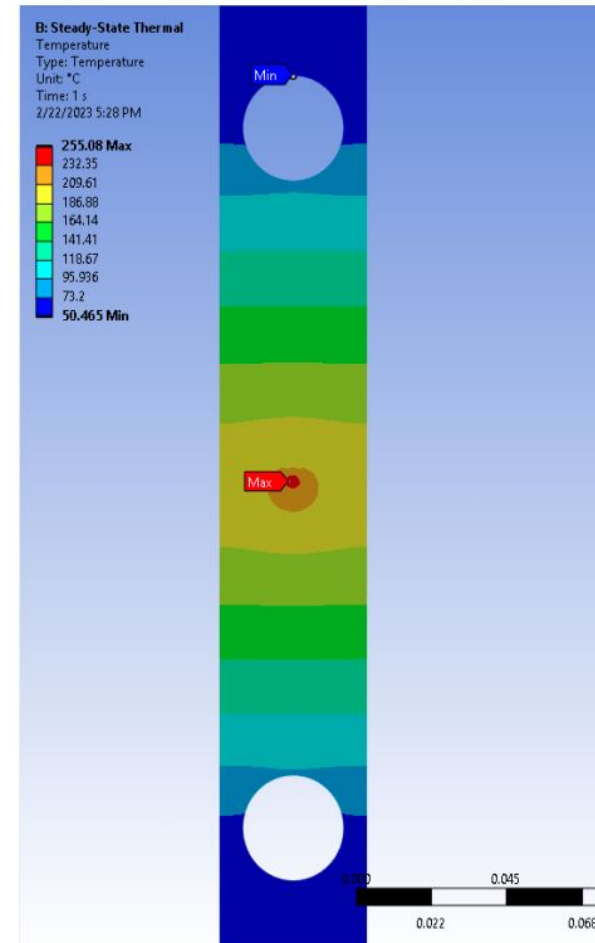
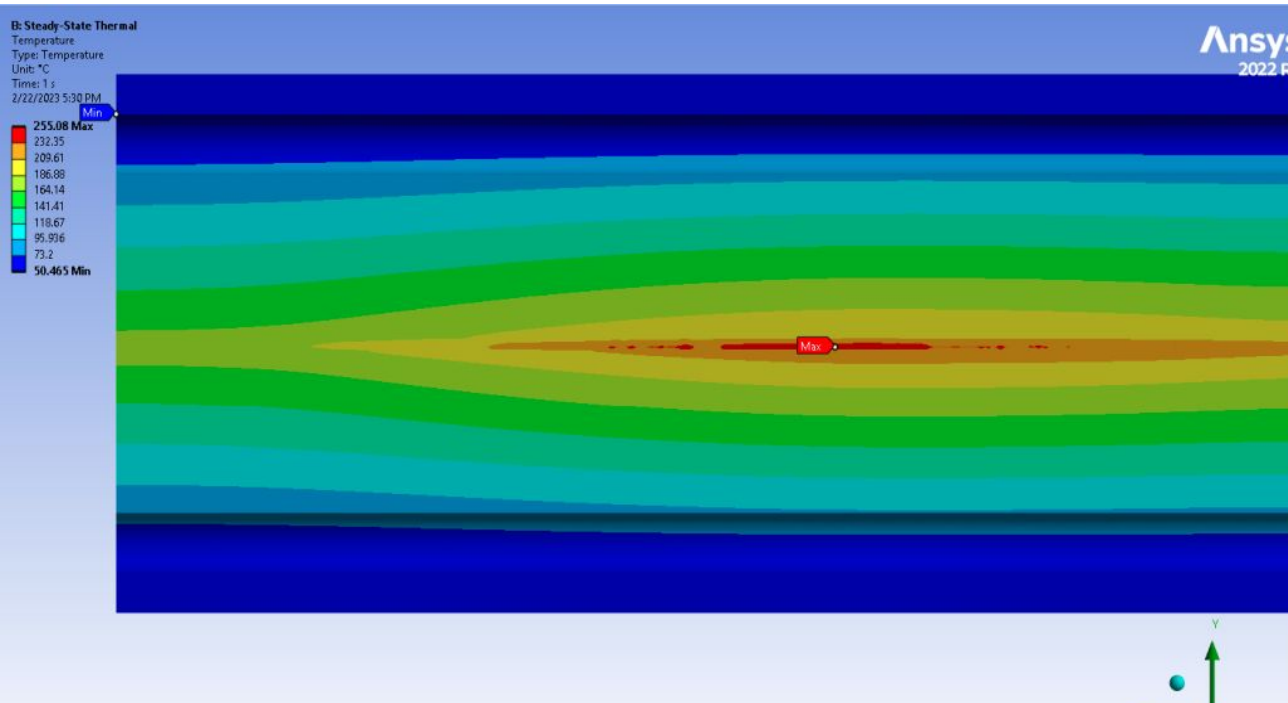


- Maximum $dP/dV = \sim 2 \text{ kW}/\text{cm}^3$
- **Temperature calculations** are done by Tim Whitlatch (JLab) using ANSYS and this Power Deposition Map.



Calculation by Tim Whitlatch

Temperature field in the Hot Segment at Heat Transfer Coefficient $9 \text{ kW/m}^2\text{C}$.

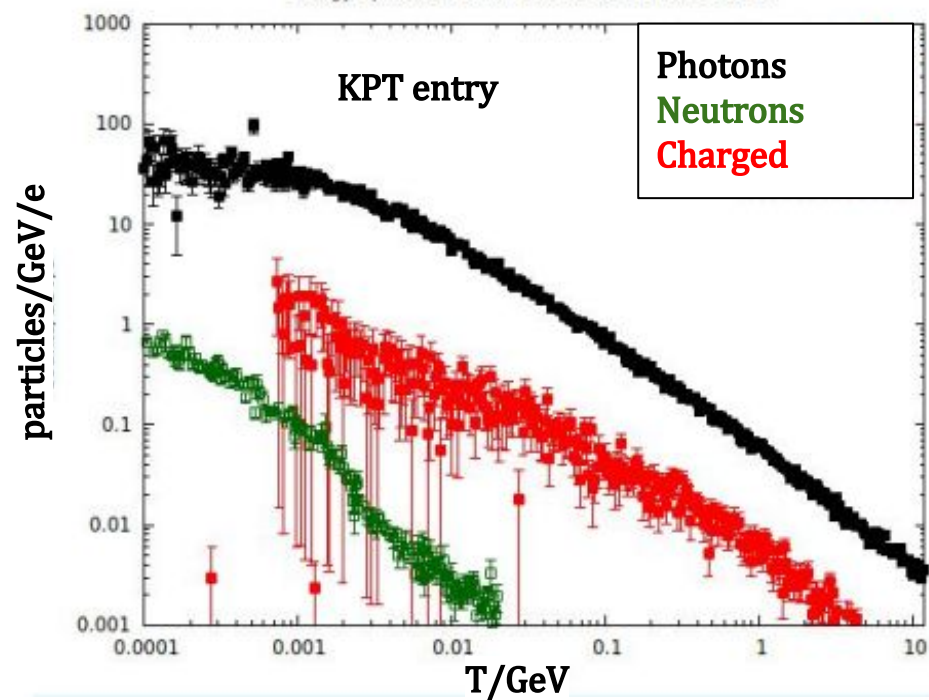
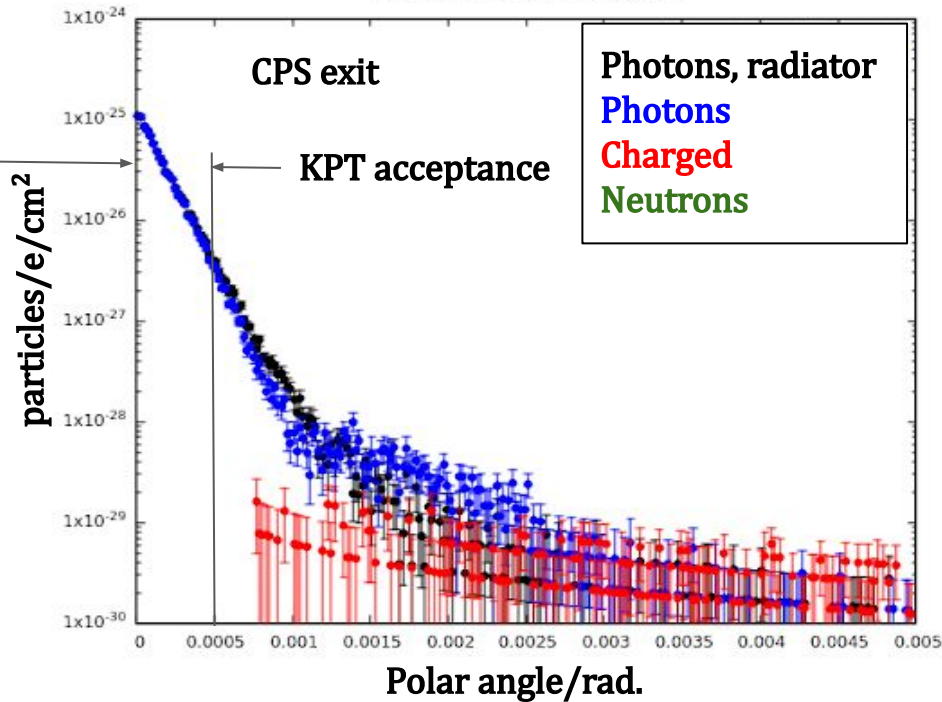


“Hot” Absorber (Cu), 53 cm long, 6.35mm Beam Hole with Air,
30 mm Water Channel ($9 \text{ kW/m}^2\text{C}$) evacuates 29 kW at $T_{\text{water}} \sim 40 \text{ }^\circ\text{C}$.

- Maximum Copper Temperature $255 \text{ }^\circ\text{C}$ (melts at $1,084 \text{ }^\circ\text{C}$).

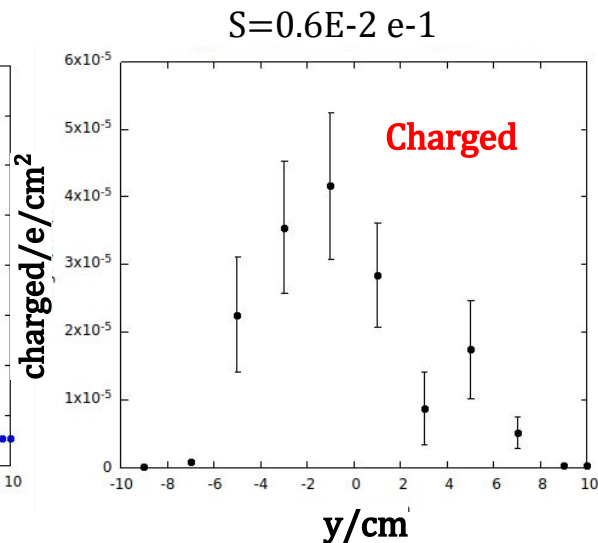
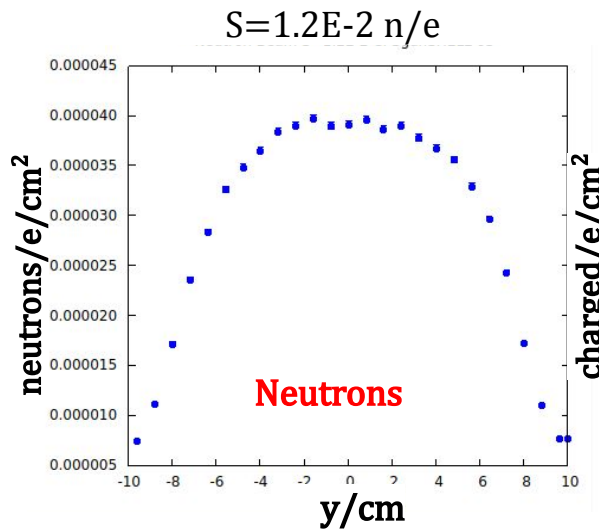
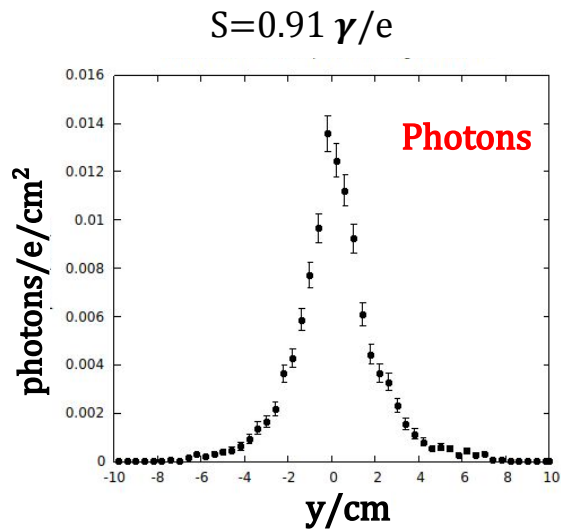
Photon Beam Quality

Particles exiting from the CPS . Angular profile.



- Photon beam at the CPS exit **looks very clean** ($< 1.E-3$). Left plot.
- What happens to the beam **after 67 m of beam line?** - Right plot.

Beam quality at KPT.



- After 67 m of beam line the total **background** of charged particles and neutrons is of **2. %**.
- Be target acceptance $r=2.5 \text{ cm}$; \Rightarrow **80%** of photon beam hits the Be target of KPT.
- Photon beam **intensity at KPT entry** $\sim 2.8 \text{ E}+13 \text{ photons/s}$.

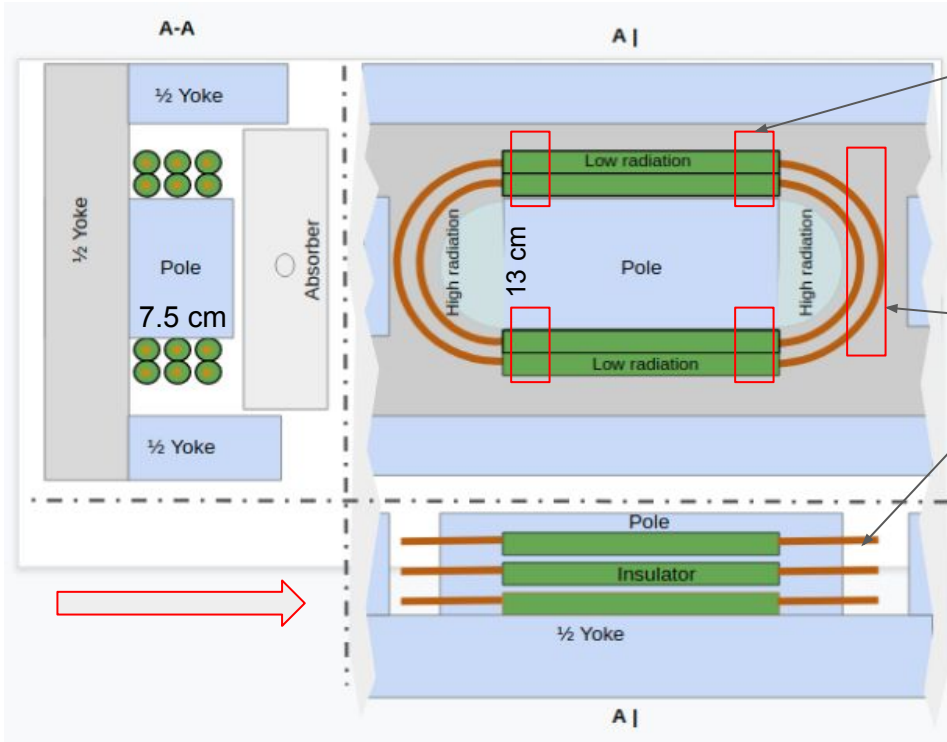
Radiation in CPS Magnet and Coil insulation lifetime.

For a closed shielding can : $S = 4/3 \mu t/D$ where μ - the permeability (relative) t : material thickness D : Shielding Diameter.

For a long hollow cylinder in a magnetic transverse field : $S = \mu t/D$.

For a cubic shielding box : $S = 4/5 \mu t/a$; a - box side length.

Coil Design and Insulation Exposure to Radiation.



Hot area for insulation.

Very hot area,
Air insulation,
Gap between
wires
~8 mm.

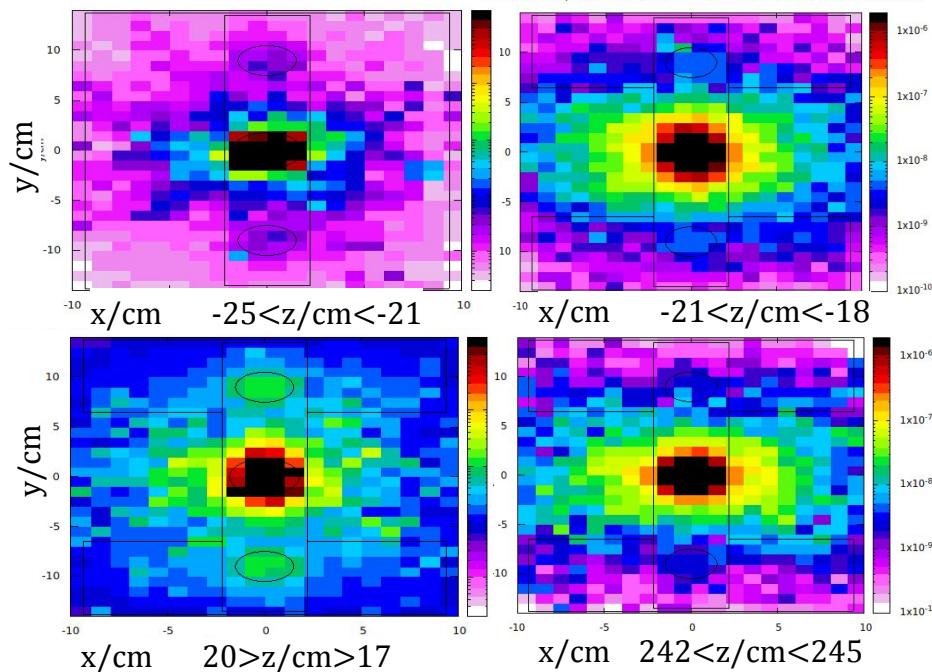
Ampere's force law:

$$dF/dl = (\mu_0 / 2\pi) (I^2/d) = \sim 25 \text{ N/m}$$

at $I=1800 \text{ A}$; $d=2.5 \text{ cm}$; $\mu_0=4\pi \times 10^{-7} \text{ N/A}^2$

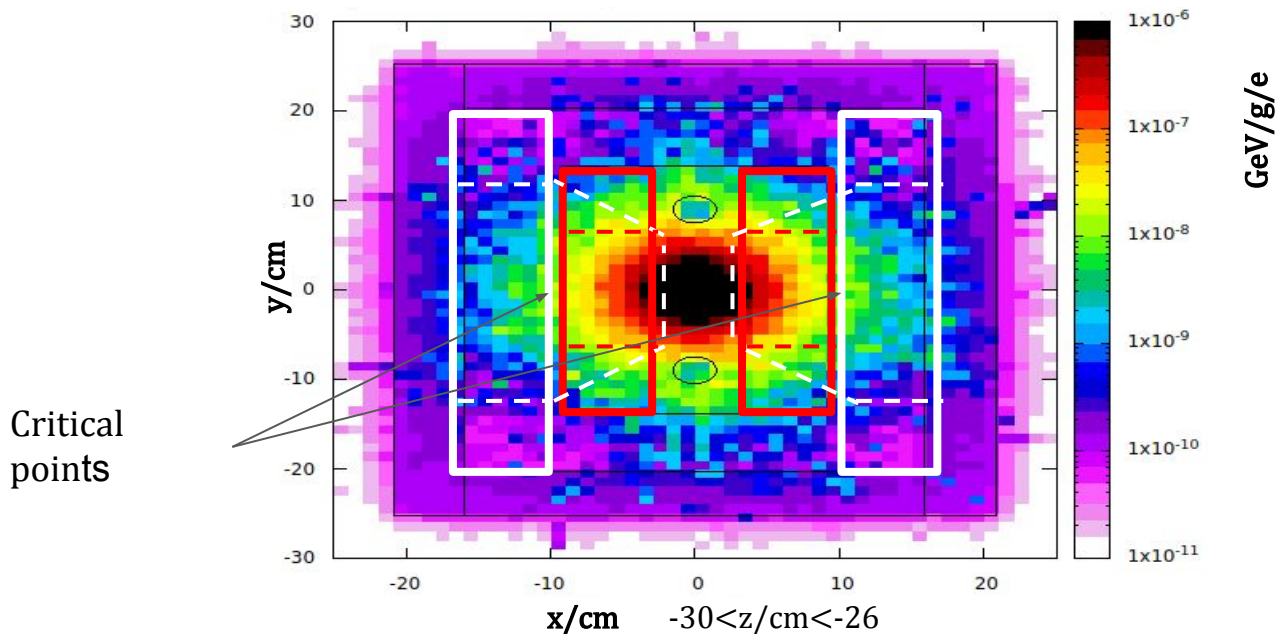
- Attractive force of bent parts $F = 25 \text{ N/m} \times 0.3 \text{ m} = 7.5 \text{ N}$.
- Copper 1.7 cm -wires (tubes) will not touch .

Prompt Dose in Coils and Insulation Lifetime (straight part).



- Reference Dose $2.E-8 \text{ GeV/g/e} \times 1.6E-10 \text{ J/GeV} = 3.2E-18 \text{ Jg}^{-1}\text{e}^{-1} = 3.2E-15 \text{ Gy/e}$;
- Translates to $3.2E-15 \text{ [Gy/e]} \times 3.E+13 \text{ [e/s]} \cong 0.1 \text{ [Gy/s]}$.
- Fiberglass cloth withstands **50 MGy** => **Lifetime** = $5.E+8 \text{ s} = 15 \text{ years}$.
- Bent part dose rate is ~ 10 times higher.

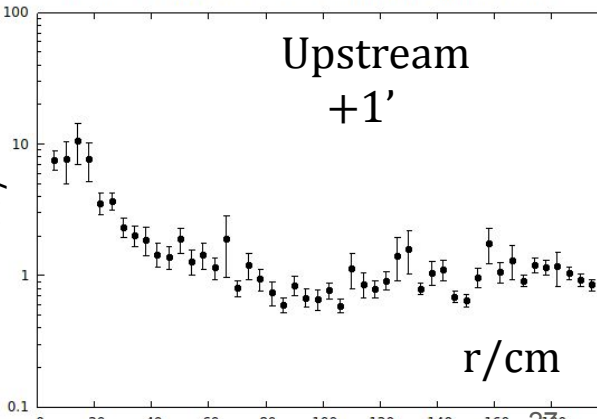
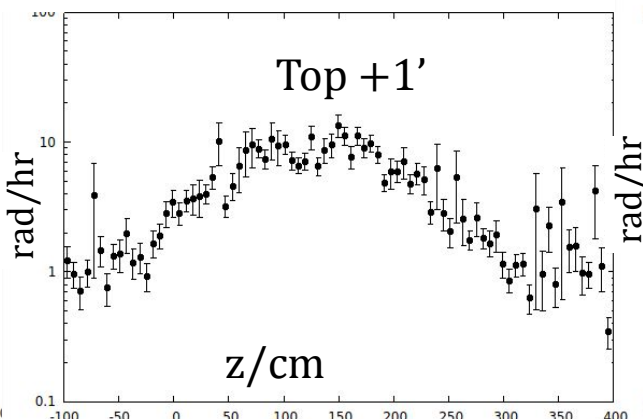
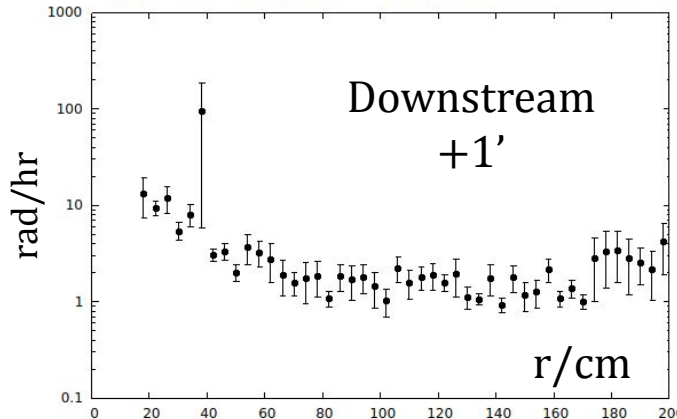
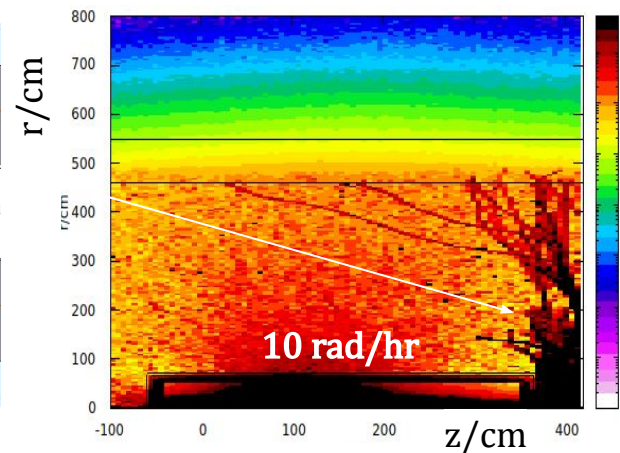
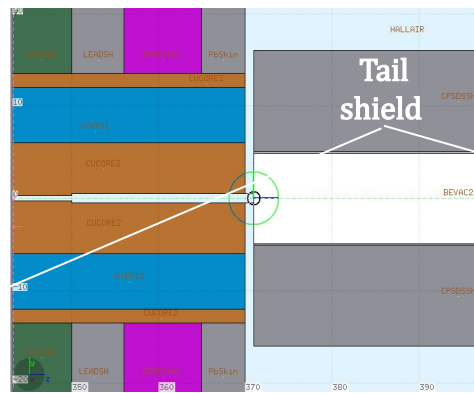
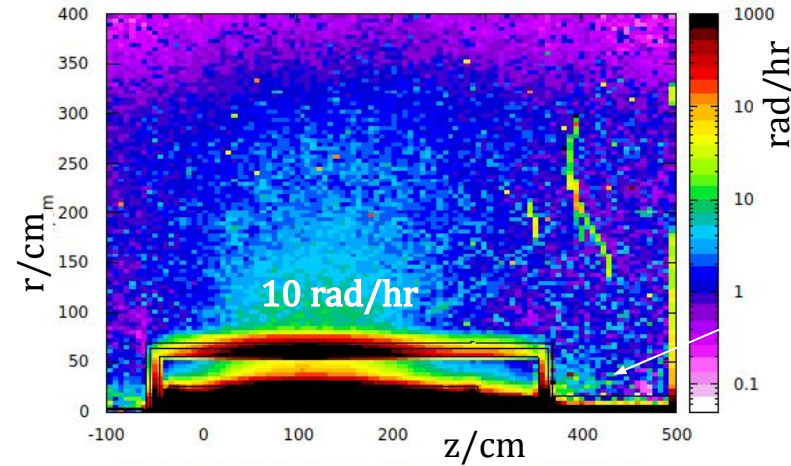
Benefit of wider magnet (+14 cm).



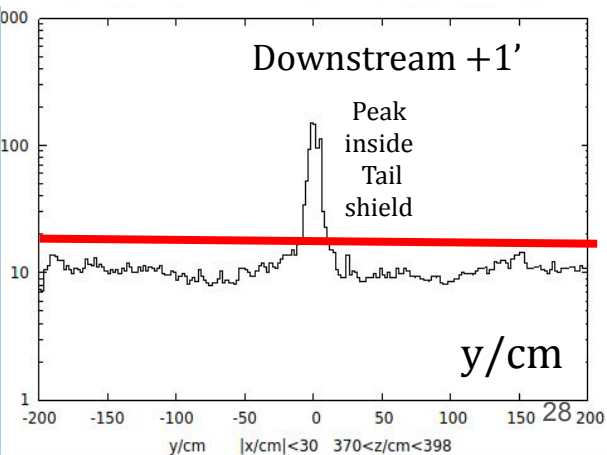
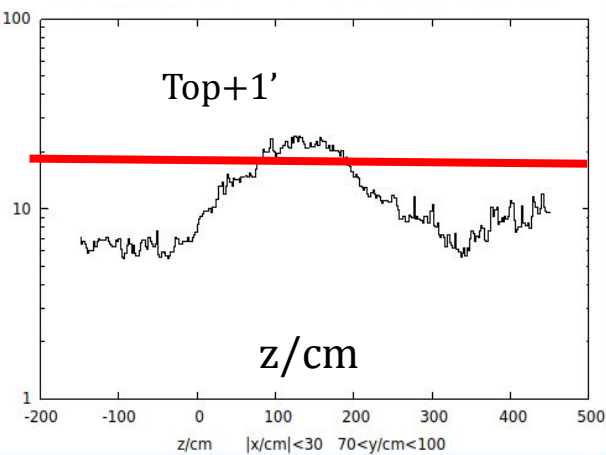
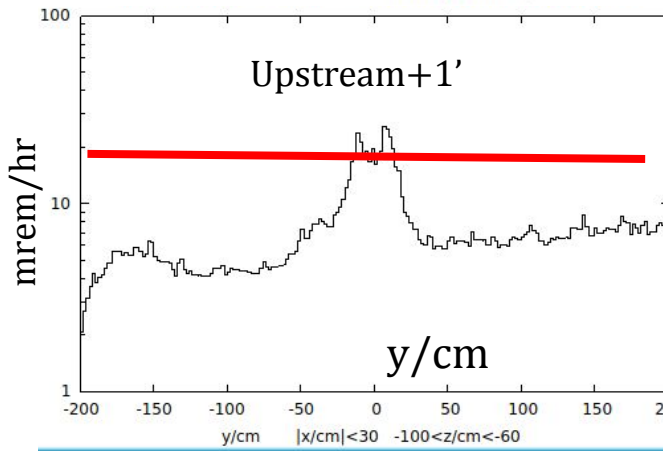
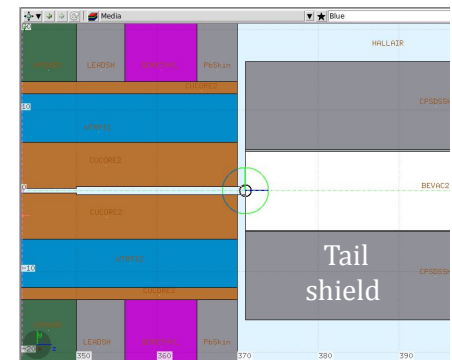
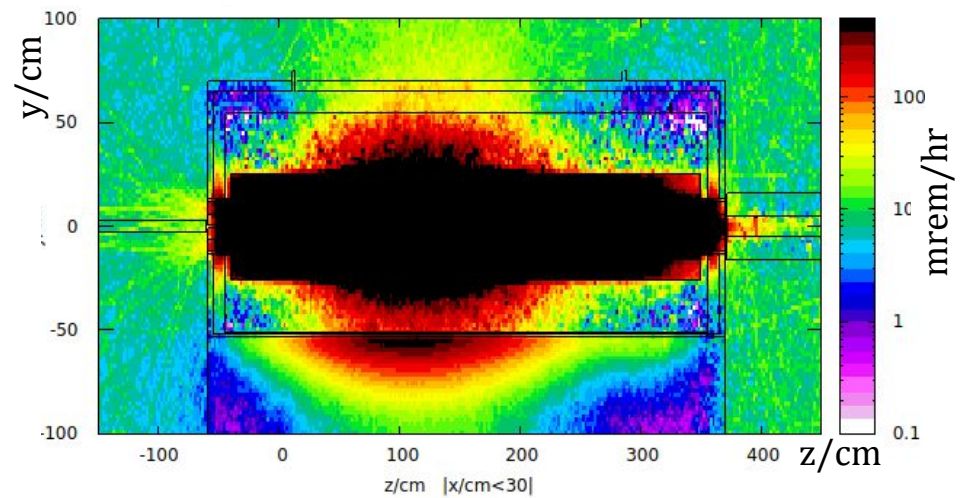
- Dose rate in critical points **0.1 Gy/s (2.E-8 GeV/g/e)**
- For 14 cm wider Magnet Insulation Lifetime in Coil return area is of **15 years.**

Prompt Dose (equipment)
and
Activation (human)
around CPS

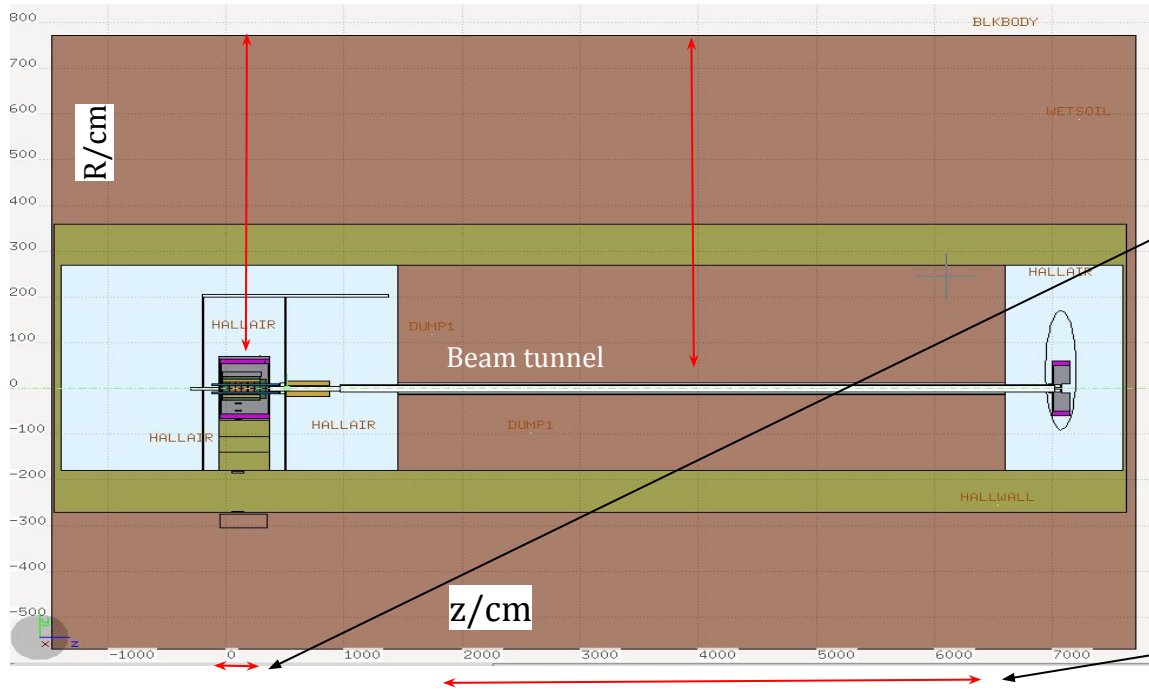
Prompt Dose Rate around CPS < 10 rad/hr . Effect of Tail shield .



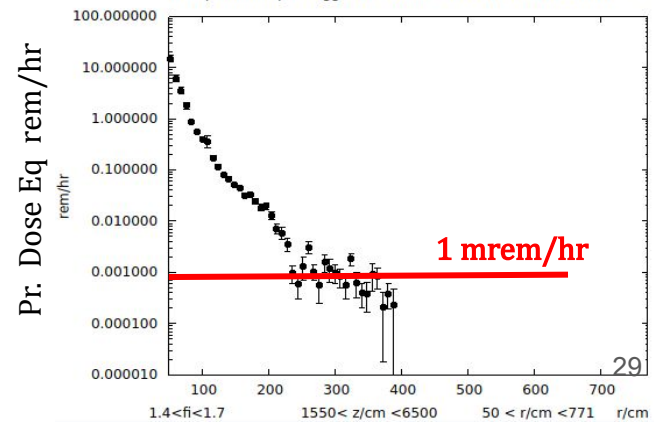
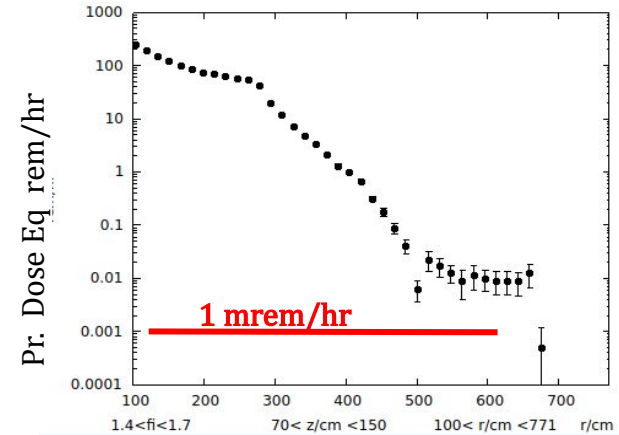
Activation After 1000+1 hr < 20 mrem/hr.



Prompt Dose Equivalent in Tagger hall and Beam Channel.

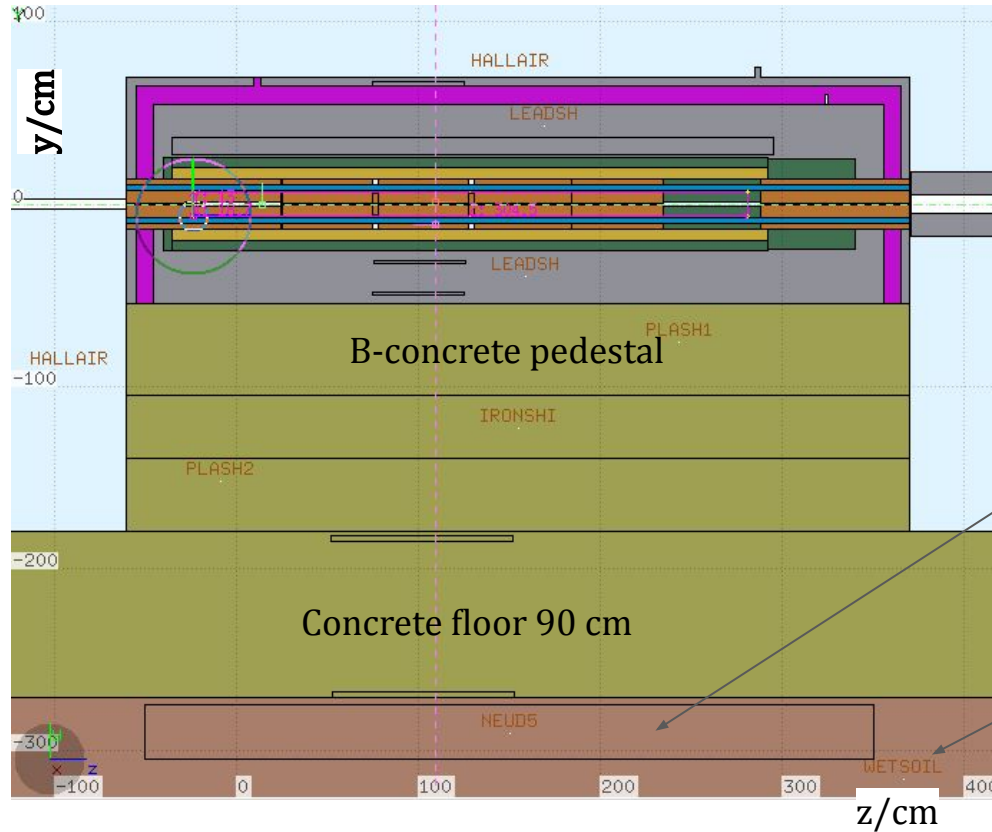


- Prompt DE is below **1 mrem/hr** at $R = \sim 2.5$ on top of Beam Tunnel.
- Prompt DE on top of hall mound $R=7.7$ m below **1 mrem/hr**.



Tritium activity in Soil and Cooling Water

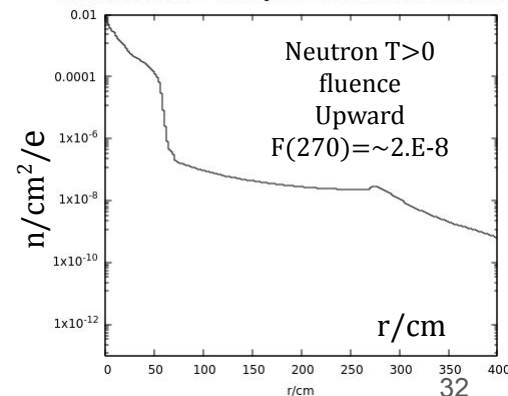
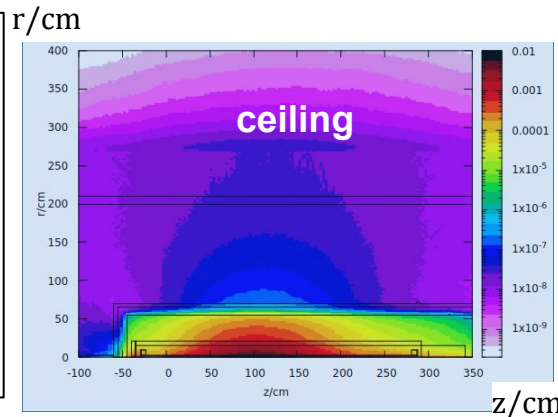
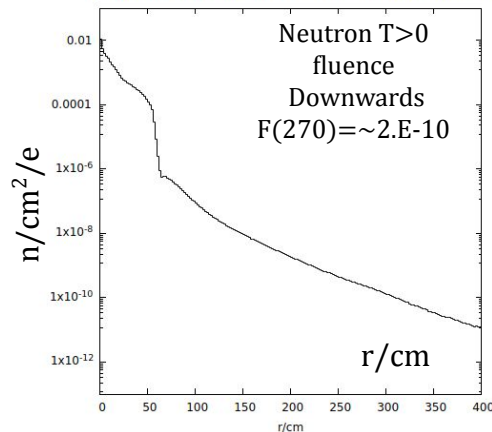
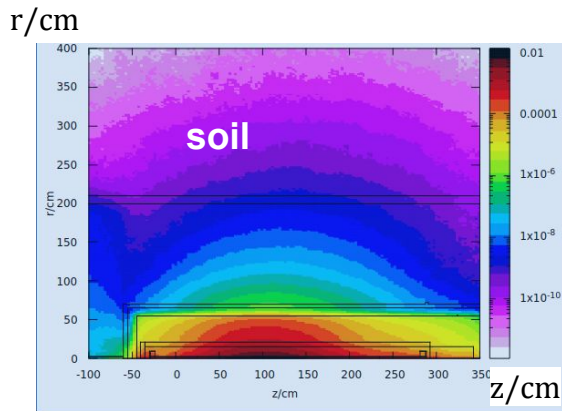
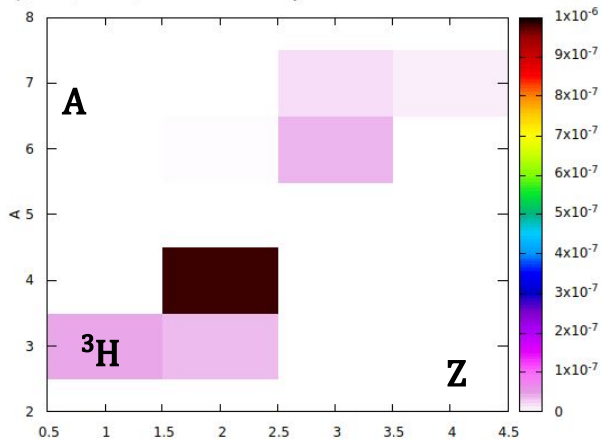
Tritium detector in FLUKA model



Tritium detector
 $V=2*0.3*4 \text{ m}^3=$
 2.4 m^3

Soil.
Wet sand with 20% of
water

Neutron fluence and Tritium in ground waters ($V=2.4 \text{ m}^3$).



^3H yield in $V=2.4\text{E}+6 \text{ cm}^3 = 1.\text{E}-7 \text{ [T/e]}$.

^3H yield per year $N=1.\text{E}-7 \text{ [T/e]} 3.\text{E}+13 \text{ [e/s]} 3.14\text{E}+7 \text{ [s]} = 1.\text{E}+14$.

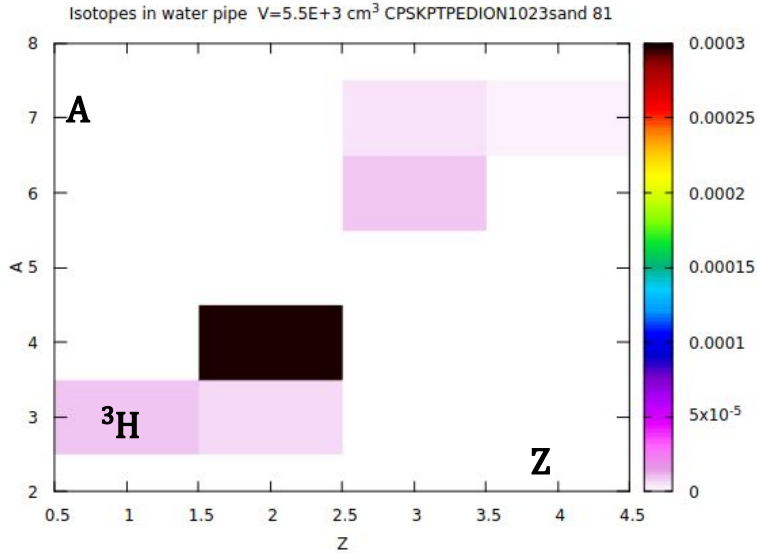
Activity of soil volume after one year :=

- $dN/dt = 1.\text{E}+14 / (12 * 3.14\text{E}+7 \text{ s}) = 2.6\text{E}+4 \text{ Bq}$

Or $\sim 200 \text{ Bq/L}$ in water ($\sim 20\%$ by volume in soil).

- Tritium activity in ground water is 3% of VA drink water limit 7000 Bq/L.

Tritium in water of cooling pipes.



We read the yield of ³H in the cooling water: **1.E-5 [T/e]**

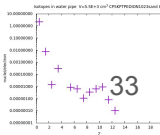
Number of T nuclei produced in one year: =

$$N_T = 1.E-5 \text{ [T/e]} \cdot 3.E+13 \text{ [e/s]} \cdot 3.14E+7 \text{ [s]} = 1.E+16 \text{ [T]}$$

Activity:

$$-dN_T/dt = 1.E+16 / (12 \cdot 3.14E+7 \text{ s}) = \mathbf{2.6 E+7 \text{ Bq}}$$

- This amount of Tritium may be accumulated by tritium absorbers.



Lifetime of various materials from
FLUKA simulations.

Material lifetime from FLUKA simulations

CPS Material	“Lethal” Dose (unit)	Max. Dose rate (unit)	Life time (unit)	Life time (year)	Comment
SuperNG [16]	4×10^7 (rad)	10 (rad/h)	4×10^6 (h)	≥ 400	Connectors
EVA [12]	2×10^7 (rad)	10 (rad/h)	2×10^6 (h)	≥ 200	Cable insulation
Low Den. Polyeth. [12]	1×10^7 (rad)	10 (rad/h)	1×10^6 (h)	≥ 100	Cable insulation
Low Den. Polyeth. [12]	1×10^7 (rad)	5×10^3 (rad/h)	2×10^3 (h)	> 0.2	Shield
Alumina ceramics [14]	10^{21} (n/cm ²)	5×10^9 (n/cm ² /s)	2×10^{11} (s)	$\geq 6,000$	Coil ins.
Alum./Silica glass [13]	10^7 (Gy)	0.1 (Gy/s)	1×10^8 (s)	≥ 3	Opt. Prop. study
Silica ceramics [14]	$> 0.3 \times 10^{21}$ (n/cm ²)	5×10^9 (n/cm ² /s)	6×10^{10} (s)	$> 2,000$	3 m Coil insul.
Silica ceramics [12]	$> 10^8$ (Gy)	0.1 (Gy/s)	10^9 (s)	> 30	Coil insul.
Kapton [7]	10^7 (Gy)	0.1 (Gy/s)	10^8 (s)	≥ 3	Coil insulation
Fiber Glass Cloth [7]	5×10^7 (Gy)	0.1 (Gy/s)	5×10^8 (s)	≥ 15	Coil insulation
Epoxy [12]	6×10^7 (Gy)	0.1 (Gy/s)	6×10^8 (s)	≥ 20	Coil insul.

- Blowing He through CPS may prevent oxidation and improve lifetime of some materials.

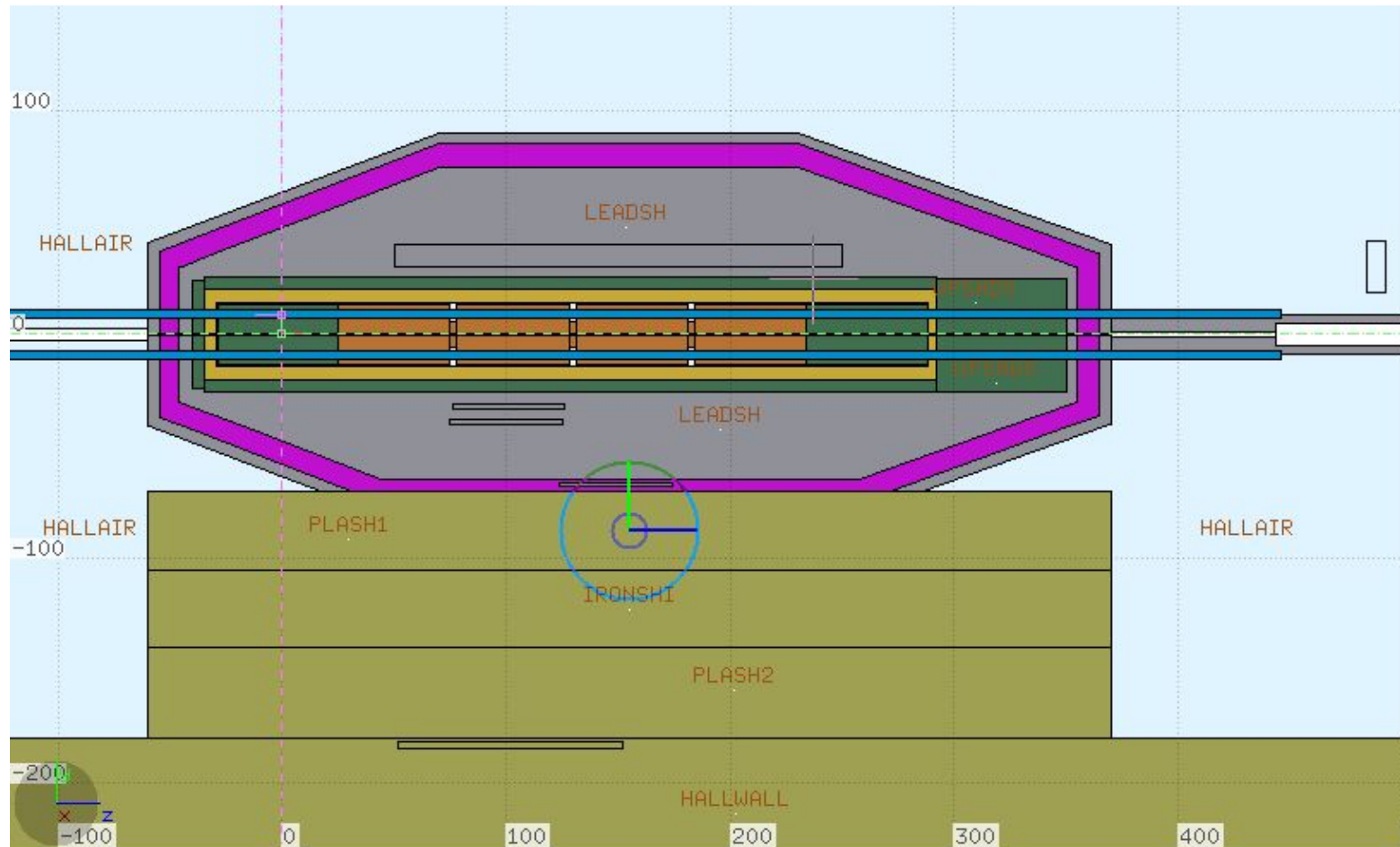
Conclusion

In our concept the **CPS is an Adjustable Unit** housing the entire Beam Channel. It is surrounded with several layers of shielding materials. CPS provides a 99% clear beam of $3.E+13$ photons/s on KPT.

This concept allows **to avoid risks** and provide:

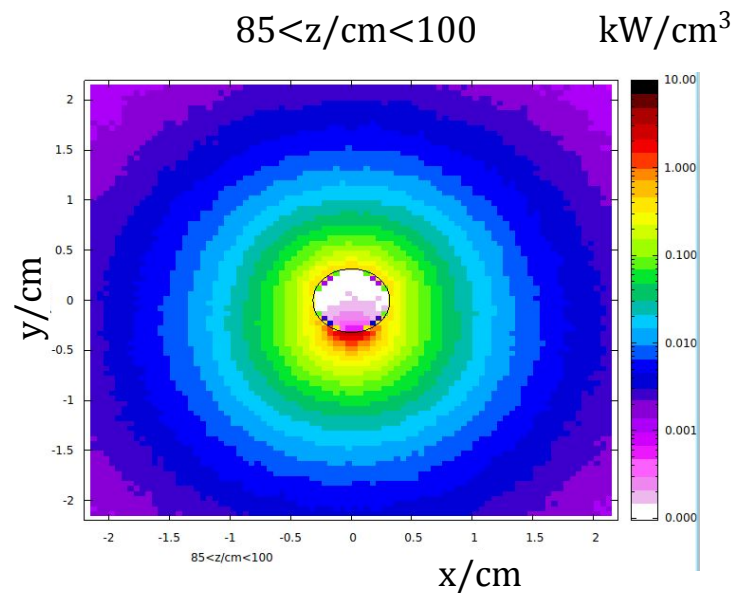
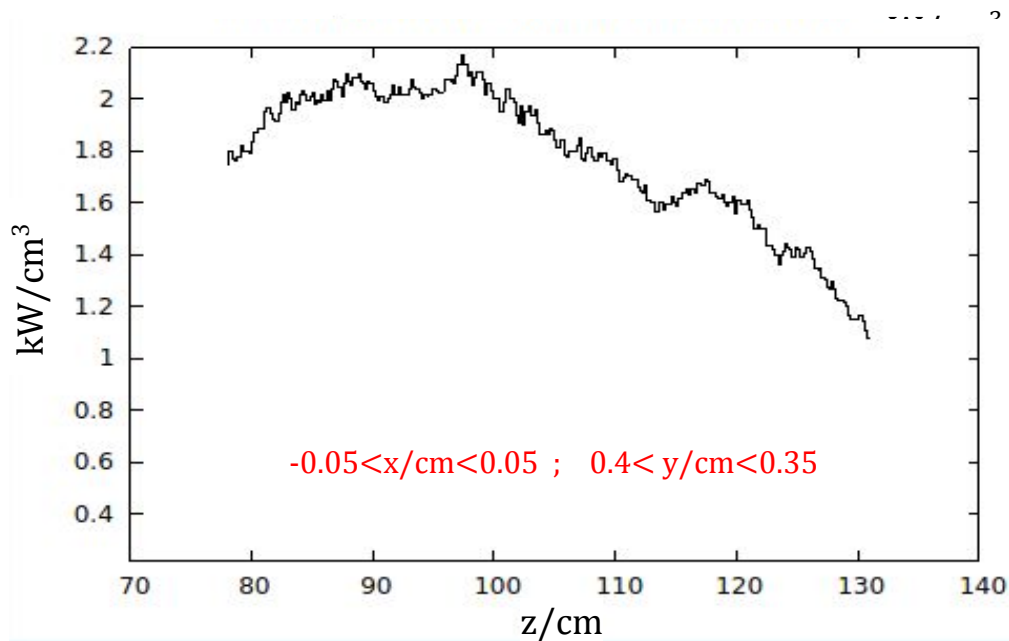
1. **No Overheating** of Copper Absorber ($T_{\max} = 200^{\circ} \text{C}$).
2. **No Short Circuit** in Magnet Coil for up to **15 years** with fiberglass based insulation.
3. **No Prompt Radiation** a $> 10 \text{ rad/hr}$ around CPS and $> 0.1 \text{ mrem/hr}$ on top of Tagger Hall.
4. **No Activation** $> 20 \text{ mrem/hr}$ around CPS after 1000+1 hrs of continuous operation .
5. **No Tritium Activity** $> 200 \text{ Bq/L}$ in ground and cooling waters. ($\sim 3\%$ of VA limit).

Optimized CPS with external layers of “elliptical” shape.



Thank you for your attention.

Power Deposition in Skinny Layer of Hot Segment . Fine map 0.05 cm.



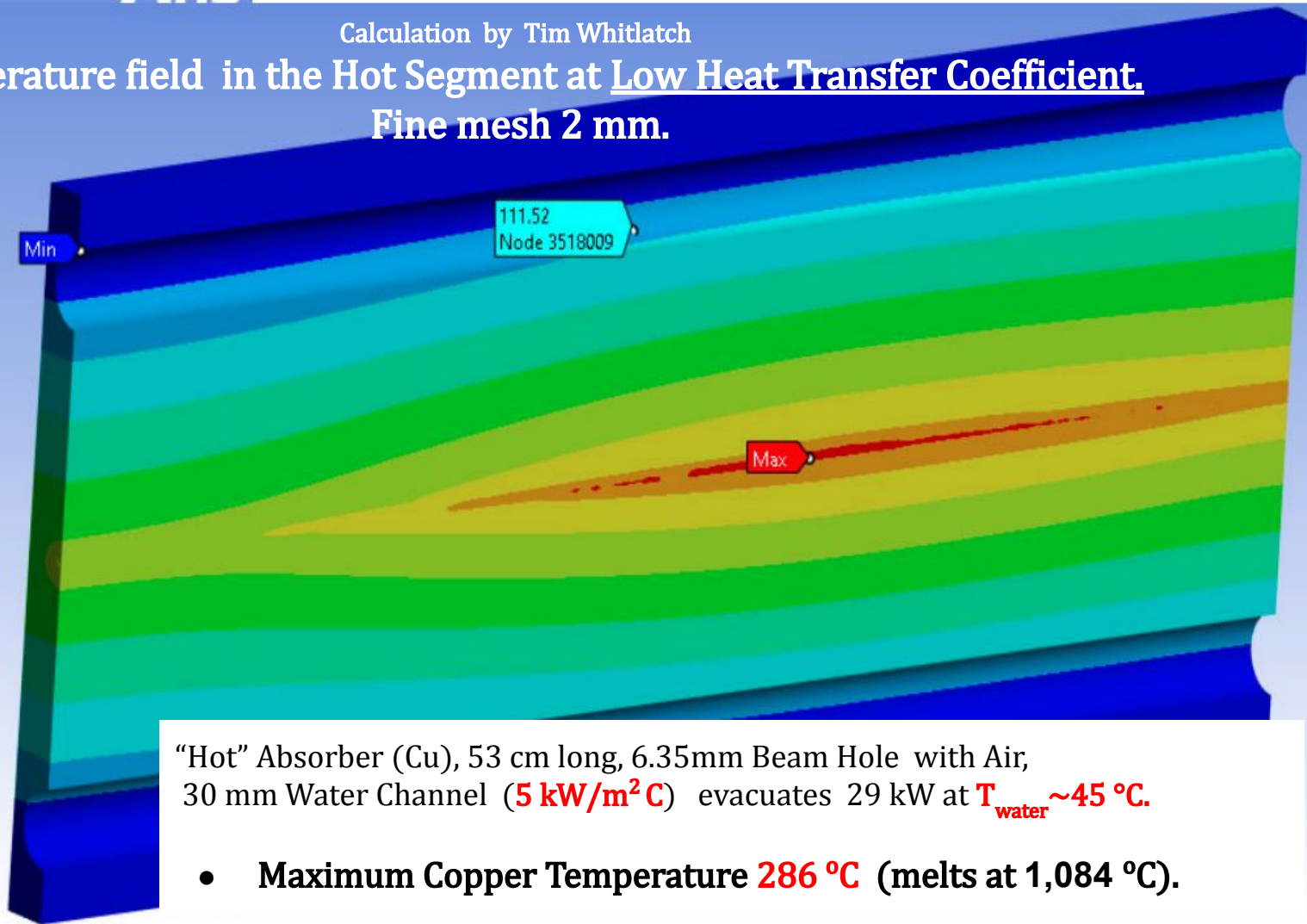
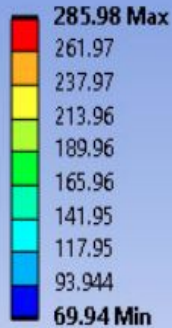
- Maximum $dP/dV = \sim 2$ kW/cm³
- **ANSYS calculations** are done by Tim Whitlatch (JLab) using this Map.

B: Steady-State Thermal

Temperature
Type: Temperature
Unit: °C
Time: 1 s
2/22/2023 2:28 PM

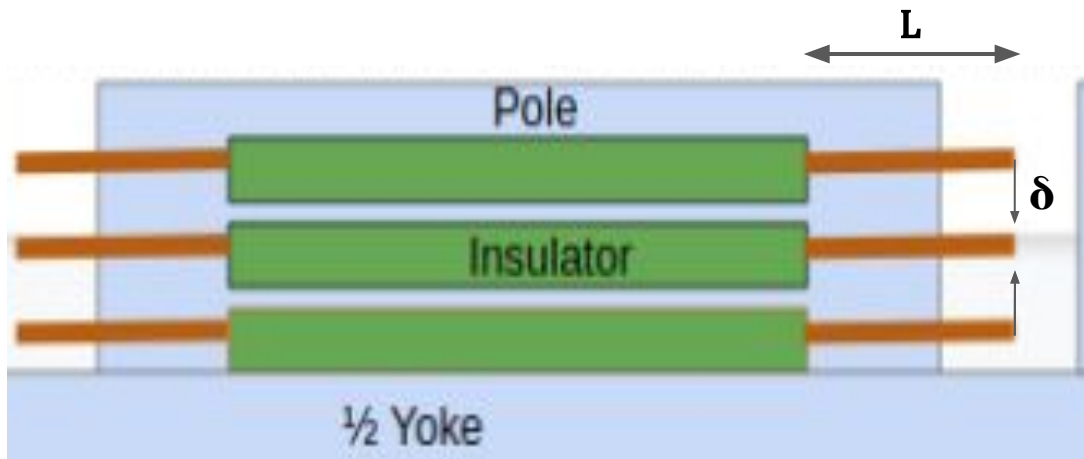
Calculation by Tim Whitlatch

Temperature field in the Hot Segment at Low Heat Transfer Coefficient, Fine mesh 2 mm.



“Hot” Absorber (Cu), 53 cm long, 6.35mm Beam Hole with Air,
30 mm Water Channel (**5 kW/m²C**) evacuates 29 kW at $T_{\text{water}} \sim 45 \text{ }^\circ\text{C}$.

- **Maximum Copper Temperature 286 °C** (melts at 1,084 °C).



Ampere's force law:

$$f' = dF/dl = (\mu_0 / 2\pi) (I^2/d)$$

$$= 25 \text{ N/m}$$

at

$I=1800 \text{ A}$ -current through wire

$d=2.5 \text{ cm}$ -distance between wires

$$\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$$

Consider a squared **Cu wire** $S=(1.7 \text{ cm})^2$, $L=20 \text{ cm}$ as a rod with fixed end

under load including gravitation $+25.5 \text{ N/m}$, total $f = f' + 25.5 = 50.5 \text{ N/m}$.

From **tabulated formula** the maximum sag at the end of the rod:

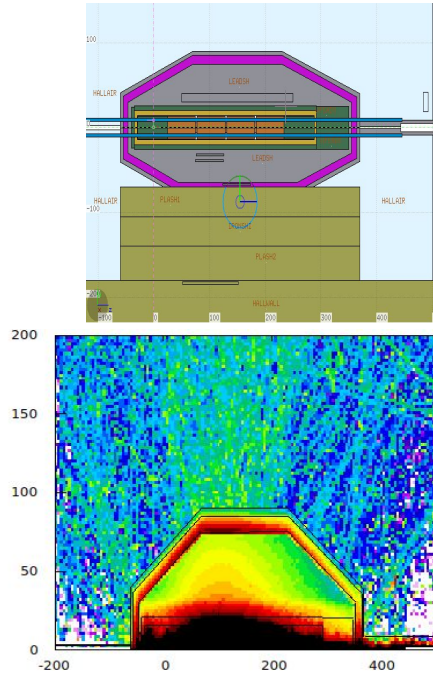
$$\delta = 3/2 f (L/W)^4 E^{-1}$$

$$= 1.5 * (50/1.2) * (20/1.7)^4 * 10^{-11} = 12 \text{ microns (compare with 8 mm gap)}$$

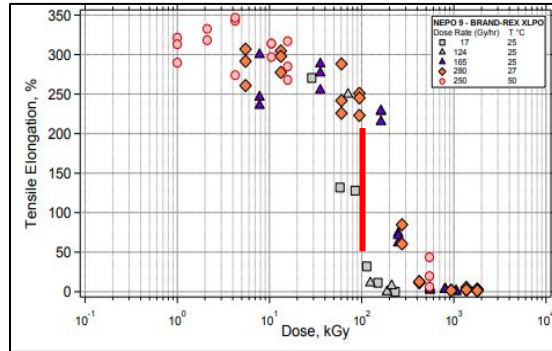
where $E=1.2 \times 10^{11} \text{ N/m}^2$ - Young's module **tabulated for copper**.

- No insulation required for coil return in high radiation area.

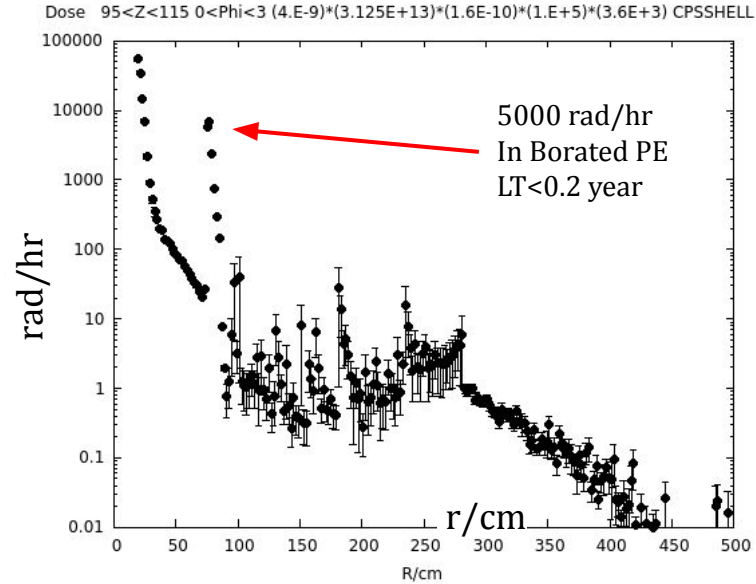
Prompt dose and Polyethylene lifetime.



PE Tensile Strength vs Dose/kGy
1Gy=100 rd



S.A. Waters, G.V. Wite, R. Tandon, L. Serna, M. Celina, R. Bernstine, "An Overview of Basic Radiation Effects on Polymers", Sandia National Laboratories, U.S. DOE, SAND2013-8003P, 2013.

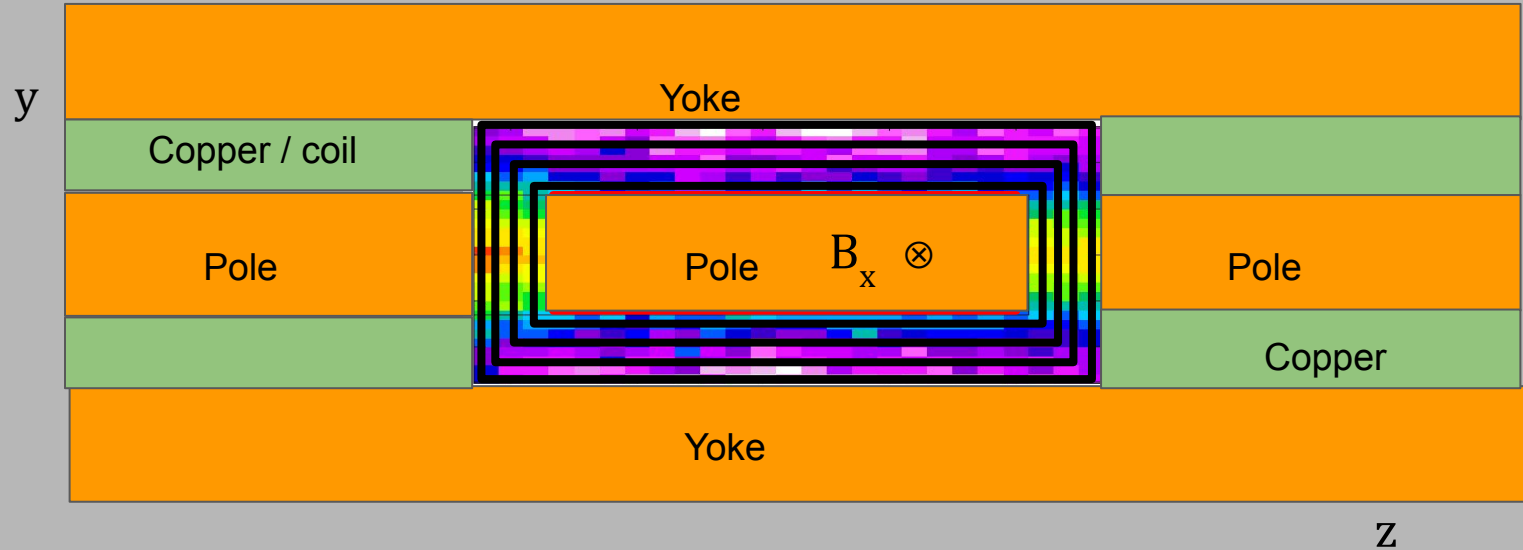


- BPE elastic properties degrade significantly after **1.E+7 rad** / 5000 rad/hr = **~0.2 year**.
- Borated polyethylene can **not** be used as **construction material**.
- Possible **solution**:- BPE granules in **metal tanks** or containers.

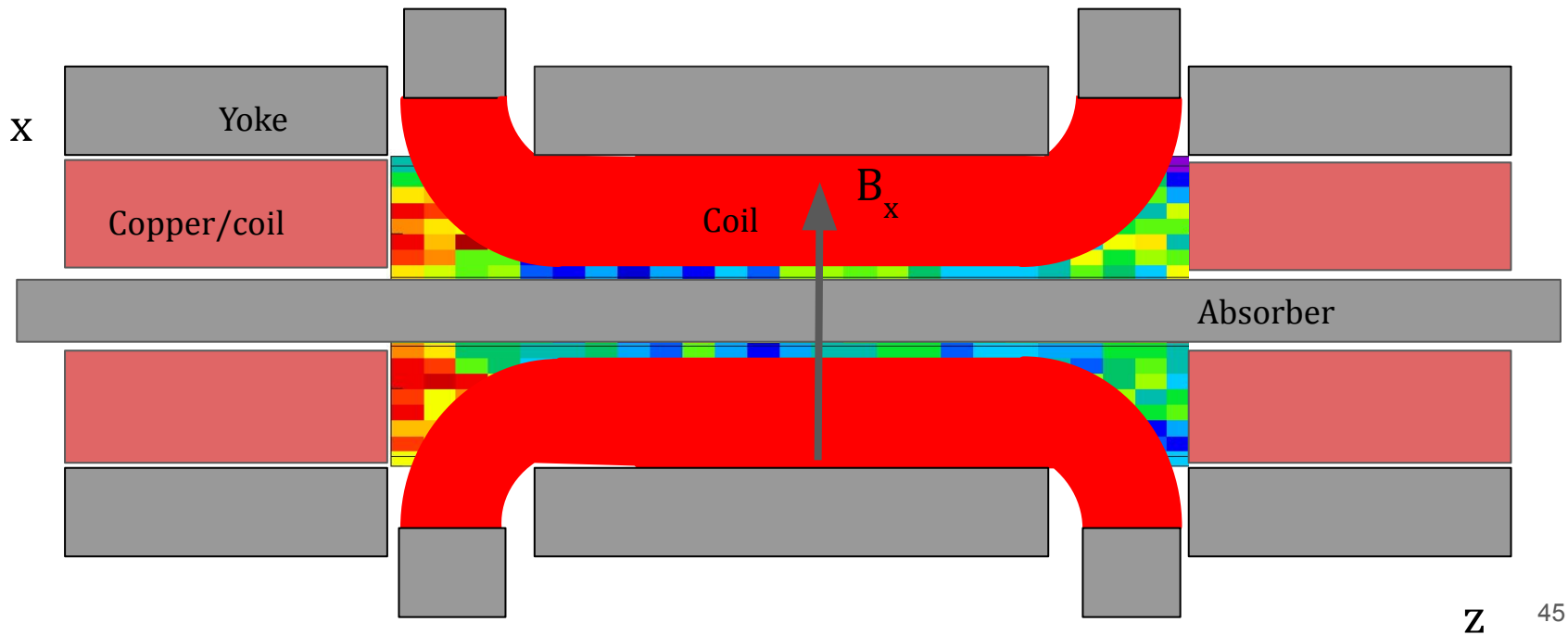
Hall D K-Long Facility E12-19-001. Experiment Readiness Review Phase I. Jefferson Lab , 2023 Charge.

- Is there any R&D needed to be done prior to start the construction of the KLong Facility? **No**
5 μ A electron beam on the CPS FWHM=**2.5 mm, 3.1E+13 e/s**, steering magnet.
- What is the status of the Compact Photon Source (CPS)? Specifically the :
 1. Conceptual design: Presented.
 2. Evaluation of the **produced radiation**: < **1 mrem/hr** on top of Tagger Hall and Tunnel Mounds.
 3. **Approximations** in the MC simulations and Code used: Simplified Tagger & KPT Halls. FLUKA2021.2.9.
 4. Energy deposition , **Absorber** and **Lead temperature**: **2 kW/cm³** , Cu Absorber < **200°C** , **Pb shield < 100°C**.
 5. Prompt **dose** and **activation** around the CPS (Tagger Hall): Dose < **10** rad/hr , <**20** mrem/hr. Maps available.
 6. **Magnet** and **insulation lifetime**: 0.25 \times 0.5 Tm, I \leq 1.8 kA, 4-6 turns, wire 2 \times 2 cm², T<**150°C**, LT=**15** years.
 7. **Cooling system** and **ground water contaminations**: Tritium Activity **2.6*10⁷ Bq** and **200 Bq/L** after 1 year.
- What will the photon **beam quality** be: **1%** of neutrons and \pm part . FWHM=4 cm, **3E+13 s⁻¹**
- What are the **cost and schedule estimates** for the construction of the CPS: **800 k\$** (no magnet).
- Will **civil constructions** be needed to contain the radiation in the Tagger Hall: **No**
- What is **Decommissioning Plan** for CPS and Activated Components: mounted on a platform, **move aside**.

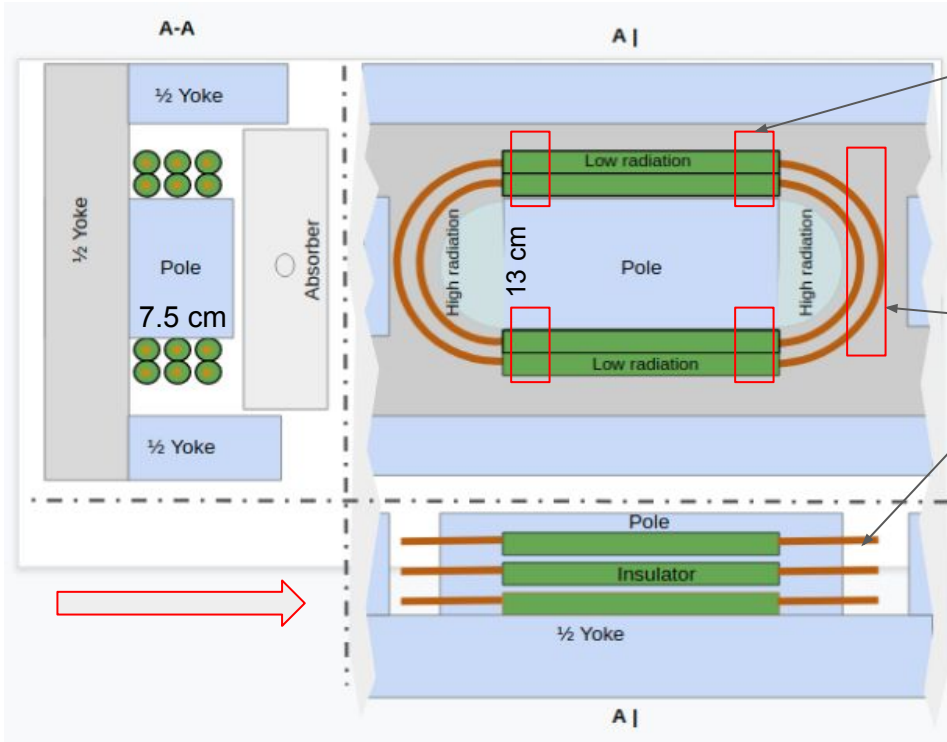
Problem of High radiation in return part of Coils.



Tim Whitlatch's solution.



Coil Design and Insulation Exposure to Radiation.



Hot area for insulation.

Very hot area,
Air insulation,
Gap between
wires
~8 mm.

Ampere's force law:

$$dF/dl = (\mu_0 / 2\pi) (I^2/d) = \sim 25 \text{ N/m}$$

at $I=1800 \text{ A}$; $d=2.5 \text{ cm}$; $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$

- Attractive force of bent parts $F = 25 \text{ N/m} \times 0.3 \text{ m} = 7.5 \text{ N}$.
- Copper 1.7 cm -wires (tubes) will not touch .

Leakage Current between wires.

Current through gas :

$$dI/ds \text{ [A/cm}^2\text{]} = n \text{ [e/cm}^3\text{]} \times v \text{ [cm/s]} \times e \text{ [C]}$$

1. What is concentration of electrons n ?
2. What is the drift velocity of electrons v ?

1. What is n and Ionisation in Magnet Coil.

$$dI/ds [A/cm^2] = n [e/cm^3] \times v [cm/s] \times e$$

Assume **maximum dose D in space between coil windings** is $D = 1.E-5 [GeV/g/e]$ ($\sim 10 \times$ of **FLUKA** estimate).

Assume **10 eV** is required to produce one electron-ion pair.

Dose D translate to ion **pair production** $\sim 1.E+3 [pair/g/e] = 1.E-5 [GeV/g/e] / 1.E-8 [GeV]$.

Ion pair production rate **per unit of mass** is at beam intensity $3.E+13 [e/s]$:

$$dN/dt = 3.E+16 [pair/g/s] = 1.E+3 [pairs/g/e] \times 3.E+13 [e/s].$$

Assume we have **1 cm of argon** between windings ($\rho_A = 1.7E-3 [g\ cm^{-3}] = \sim 2.E-3$).

Air - $1.3E-3$; He - $0.17E-3$

So we find the ion **production rate between coil wires** :

$$dn_p/dt = (dN/dt) \rho_A = 3.E+16 [pairs\ g^{-1}\ s^{-1}] \times 2.E-3 [g\ cm^{-3}] = 6.E+13 [pair\ cm^{-3}\ s^{-1}]$$

This rate is **balanced by recombination** of argon ions and electrons.

1. What is n. Ionisation in Magnet Coil and Leakage Current.

$$dI/ds \text{ [A/cm}^2\text{]} = n \text{ [e/cm}^3\text{]} \times v \text{ [cm/s]} \times e$$

$dn_p/dt = 6.E+13 \text{ [pairs cm}^{-3} \text{ s}^{-1}\text{]}$ is balanced by recombination of argon ions and electrons defined as:

$$dn_r/dt = \alpha n_+ n_- , \quad \text{where } \alpha = 2.E-10 \text{ [cm}^3 \text{ i}^{-1} \text{ s}^{-1}\text{]} \text{ recombination coeff. for Argon.}$$

$$(\alpha = \sim 1.E-8 \text{ [cm}^3 \text{ i}^{-1} \text{ s}^{-1}\text{]} \text{ for He, and } \alpha = 1.E-6 \text{ — } 1.e-7 \text{ for Air.)}$$

Assuming equal densities $n_+ = n_- = n$ for the equilibrium density of electrons n we write:

$$\alpha n^2 = dn_p/dt = 6.E+13 \text{ [pairs cm}^{-3} \text{ s}^{-1}\text{]} \text{ from the previous slide and}$$

$$n^2 = \alpha^{-1} dn_i/dt = 0.5E+10 \text{ [pairs s cm}^{-3}\text{]} \times 6.E+13 \text{ [pairs cm}^{-3} \text{ s}^{-1}\text{]} = 3.E+23 \text{ (pairs/cm}^3\text{)}^2.$$

- The equilibrium density of electrons yields $n = 6.E+11 \text{ (pairs/cm}^3\text{)}.$
- Density of electrons is proportional to the gas specific factor $(\alpha^{-1} q_A)^{1/2}.$

2. What is v and Electric Field between Wires at 2 kA current.

What is Voltage between windings?

Copper resistivity $\kappa=1.7E-6$ [Ohm·cm]; $L_w/S_w = 100 \text{ cm}/3 \text{ cm}^2 = 25 \text{ cm}^{-1}$

=> **Voltage between windings** ($V = I \times R_w$ where $R_w = \kappa \times L_w/S_w$)

$V = 2000 \text{ [A]} \times 1.7E-6 \text{ [Ohm·cm]} \times 25 \text{ [cm}^{-1}] = 2.E-6 \times 5.E+4 \text{ [Ohm·A]}$

$$V = 0.1 \text{ V.}$$

From **Top Plot** ⁽¹⁾ we see **drift velocity** as $v = v(E/P)$ where

E -electric field, P=gas pressure.

In our case $E=0.1 \text{ [V cm}^{-1}]$; $P \sim 1000 \text{ [mmHg]}$ =>

$$E/P = 1.E-4 \text{ [V cm}^{-1}/\text{mmHg]}$$

From Top Plot we read $v(0.1) = 2.E+6 \text{ [cm/s]}$ and linear interpolation yields:

$$v(1.E-4) = 2.E+3 \text{ [cm/s].}$$

From Bottom Plot for air we find $v(1.E-4) = 5.E+1 \text{ cm/s.}$

- (1) F. Sauli, "PRINCIPLES OF OPERATION OF MULTIWIRED PROPORTIONAL AND DRIFT CHAMBERS",

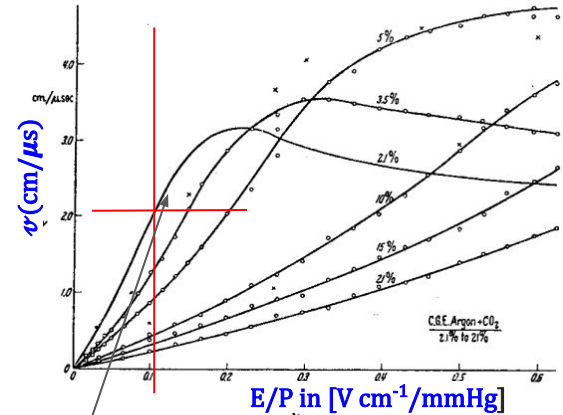


Fig. 29 Drift velocity of electrons in several argon-carbon dioxide mixtures⁽¹²⁾

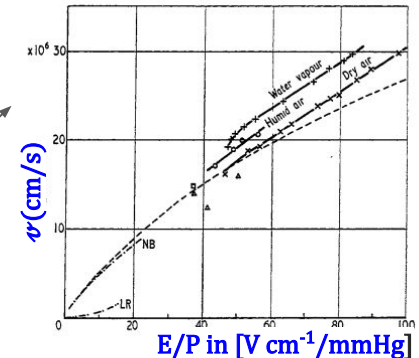


Figure 5. Electron drift velocity in dry air, humid air and water vapour as a function of reduced electrical field. Pressure readings reduced to temperature of 20 °C; humid air, $p_w/p = 16\%$. Broken line, Townsend and Tizard 1913; Δ , Raether; \square , Rieman 1944; \circ , Nielsen and Bradbury 1937; \times , Lowe and Rees 1963.

2. What is leakage current between wires .

Current density between windings:

$$dI/ds \text{ [A/cm}^2\text{]} = n \text{ [e/cm}^3\text{]} \times v \text{ [cm/s]} \times 1.6\text{E-19 [C/e]} \propto v (\alpha^{-1} \rho_A)^{1/2}$$

Where $n=6.\text{E}+11 \text{ [e/cm}^3\text{]}$.

$v=2.\text{E}+3 \text{ [cm/s]}$.

For the current density we find :

$$\begin{aligned} dI/ds \text{ [A/cm}^2\text{]} &= 6.\text{E}+11[\text{e/cm}^3] \times 2.\text{E}+3 \text{ [cm/s]} \times 1.6\text{E-19 [C/e]} = 12 \times 1.6 \text{ E}(+11+3-19) = \\ &= 20.\text{E-5 [A/cm}^2\text{]}. \end{aligned}$$

Wire area $S=2 \text{ cm} \times 100 \text{ cm} = 2.\text{E}+2 \text{ cm}^2$, and the maximum possible current yields:

$$I \text{ [A]} = 20.\text{E-5 [A/cm}^2\text{]} \times 2.\text{E}+2 \text{ [cm}^2\text{]} = 40.\text{E-3 [A]} = 40 \text{ [mA]}. \text{ Compare to 2 kA !}$$

- Leakage is of $2.\text{E-5}$ of the wire current. It does not affect the coil performance.
- For Helium the leakage is ~ 10 times lower - due to the gas specific factor $v (\alpha^{-1} \rho_{\text{He}})^{1/2}$.

(1)

