

***K*_{Long} beam experiment in JLAB and
search for pentaquark states in the
meson photoproduction reactions**

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Physics
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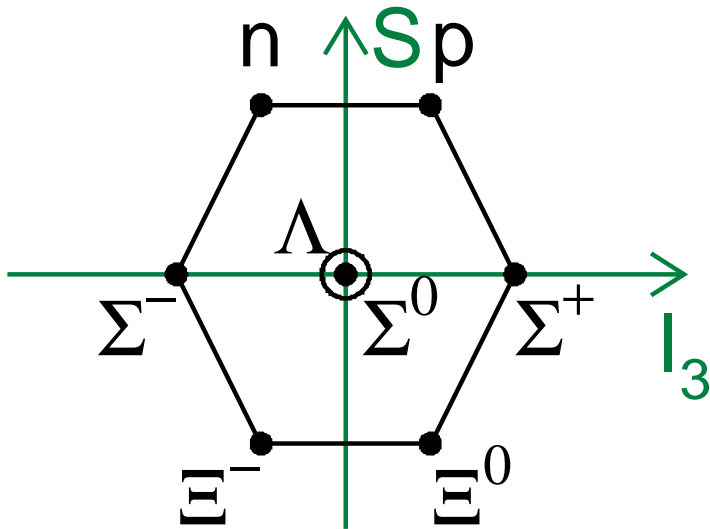
RNC "Kurchatov Institute" PNPI (Russia)

K_{Long} beam motivation

1. Search for the missing Σ -hyperons
2. Search for the pentaquark states predicted by the chiral soliton model (Dyakonov, Petrov, Polyakov).

$$3 \otimes 3 \otimes 3 = 10_S \oplus 8_M \oplus 8_M \oplus 1_A$$

Octet



Decuplet

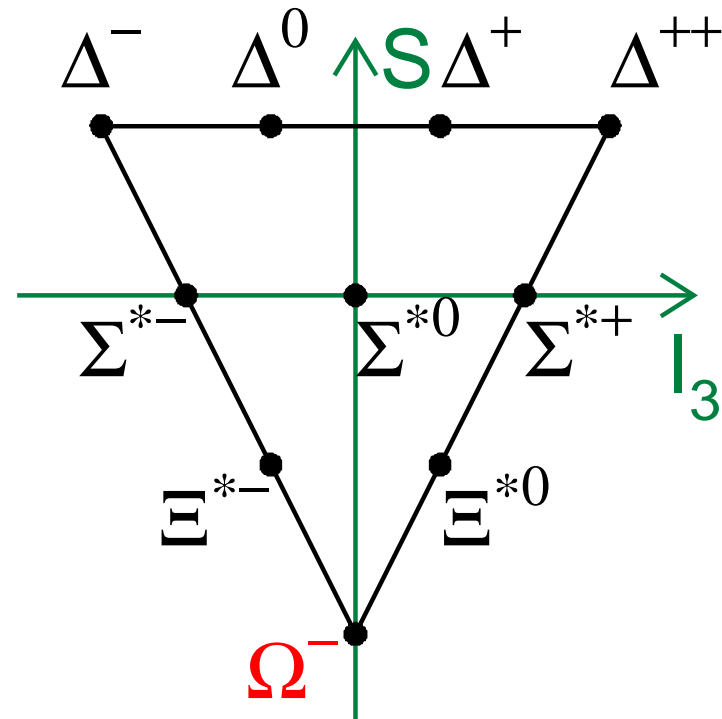


Table 1: Λ -hyperons used in the first fit of the data.

		J^P	Status	Mass	Width
singlet	$\Lambda(1405)$	$1/2^-$	****	$1405_{-1.0}^{+1.3}$	50.5 ± 2.0
$N(1535)$	$\Lambda(1670)$	$1/2^-$	****	$1660 - 1680$	$25 - 50$
$N(1650)$	$\Lambda(1800)$	$1/2^-$	***	$1720 - 1850$	$200 - 400$
singlet	$\Lambda(1520)$	$3/2^-$	****	1519.5 ± 1.0	15.6 ± 1.0
$N(1520)$	$\Lambda(1690)$	$3/2^-$	****	$1685 - 1695$	$50 - 70$
$N(1675)$	$\Lambda(1830)$	$5/2^-$	****	$1810 - 1830$	$60 - 110$
$N(2190)$	$\Lambda(2100)$	$7/2^-$	****	$2090 - 2110$	$100 - 250$
$N(1440)$	$\Lambda(1600)$	$1/2^+$	***	$1560 - 1700$	$50 - 250$
$N(1710)$	$\Lambda(1810)$	$1/2^+$	***	$1750 - 1850$	$50 - 250$
$N(1700)$	$\Lambda(1890)$	$3/2^+$	****	$1850 - 1910$	$60 - 200$
$N(1680)$	$\Lambda(1820)$	$5/2^+$	****	$1815 - 1825$	$70 - 90$
$N(2060)$	$\Lambda(2110)$	$5/2^+$	***	$2090 - 2140$	$150 - 250$

Table 2: Σ -Hyperons used in the first fit of the data.

		J^P	Status	Mass	Width
$N(1440)$	$\Sigma(1660)$	$1/2^+$	***	1630 – 1690	40 – 200
$\Delta(1230)$	$\Sigma(1385)$	$3/2^+$	****	1382.80 ± 0.35	36.0 ± 0.7
$N(1680), \Delta(1905)$	$\Sigma(1915)$	$5/2^+$	****	1900 – 1935	80 – 160
$N(1990), \Delta(1950)$	$\Sigma(2030)$	$7/2^+$	****	2025 – 2040	150 – 200
$N(1520)$	$\Sigma(1670)$	$3/2^-$	****	1665 – 1685	40 – 80
$N(1535), \Delta(1620), N(1650)$	$\Sigma(1750)$	$1/2^-$	***	1730 – 1800	60 – 160
$N(1675)$	$\Sigma(1775)$	$5/2^-$	****	1770 – 1780	105 – 135
$N(1700), \Delta(1700)$	$\Sigma(1940)$	$3/2^-$	***	1900 – 1950	150 – 300

Many Σ states are missing.

The πN (KN) interaction. Three measurements are needed to fix quantum numbers

$$A_{\pi N} = \omega^* [G(s, t) + H(s, t)i(\vec{\sigma}\vec{n})] \omega' \quad \vec{n}_j = \varepsilon_{\mu\nu j} \frac{q_\mu k_\nu}{|\vec{k}||\vec{q}|} .$$

$$G(s, t) = \sum_L [(L+1)F_L^+(s) + LF_L^-(s)] P_L(z) ,$$

$$H(s, t) = \sum_L [F_L^+(s) - F_L^-(s)] P'_L(z) .$$

Differential cross section in c.m.s. of the reaction

$$|A|^2 = \frac{1}{2} \text{Tr} [A_{\pi N}^* A_{\pi N}] = |G(s, t)|^2 + |H(s, t)|^2 (1 - z^2)$$

the recoil asymmetry:

$$P = \frac{\text{Tr} [A_{\pi N}^* \sigma_2 A_{\pi N}]}{2|A|^2 \cos \phi} = \sin \Theta \frac{2 \text{Im} (H^*(s, t) G(s, t))}{|A|^2} .$$

and the rotation parameter.

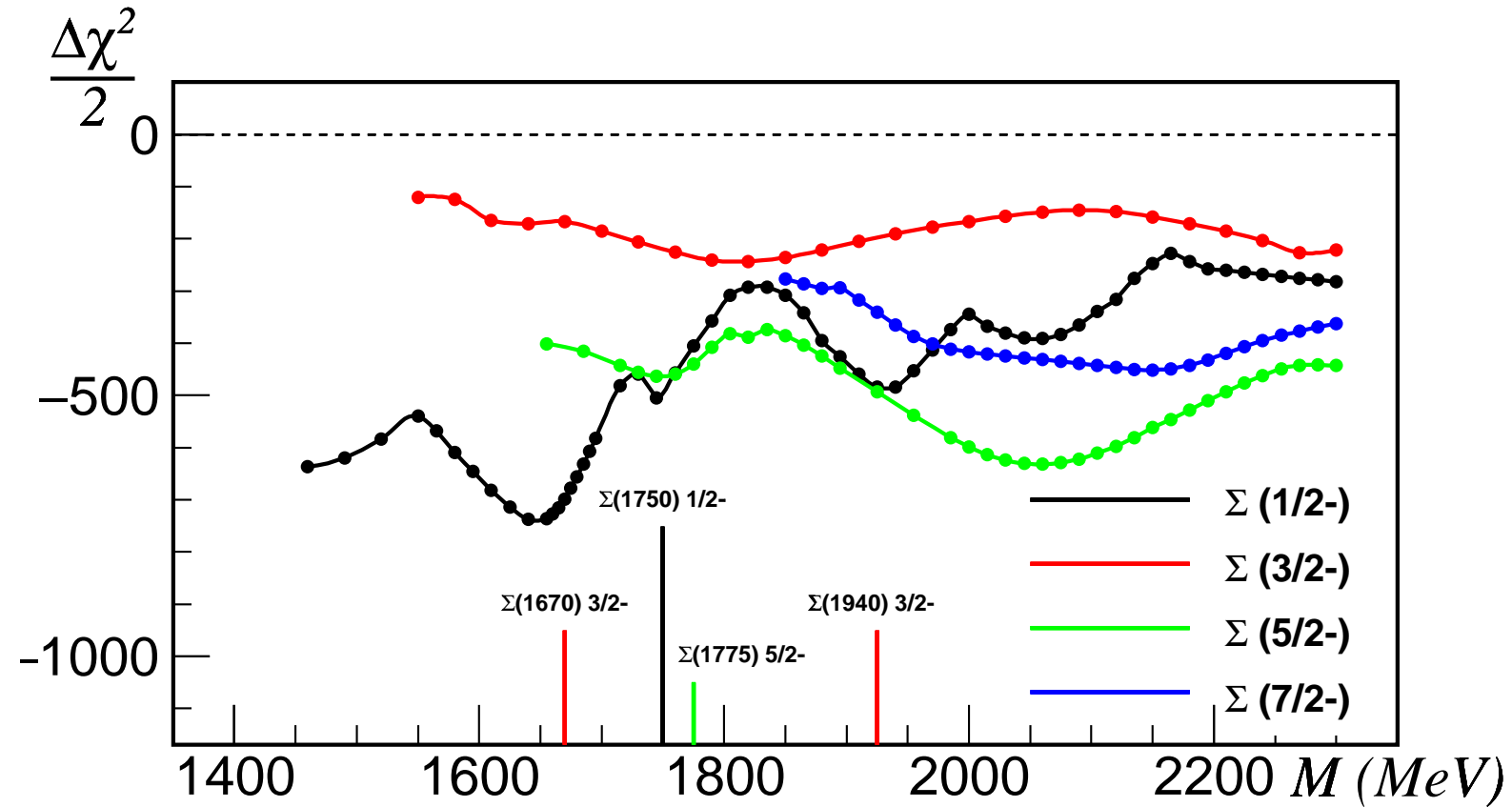
Kaon beam motivation

There is a hope to observe the baryon multiplets and therefore to confirm the states observed in the Nucleon and Delta sector.

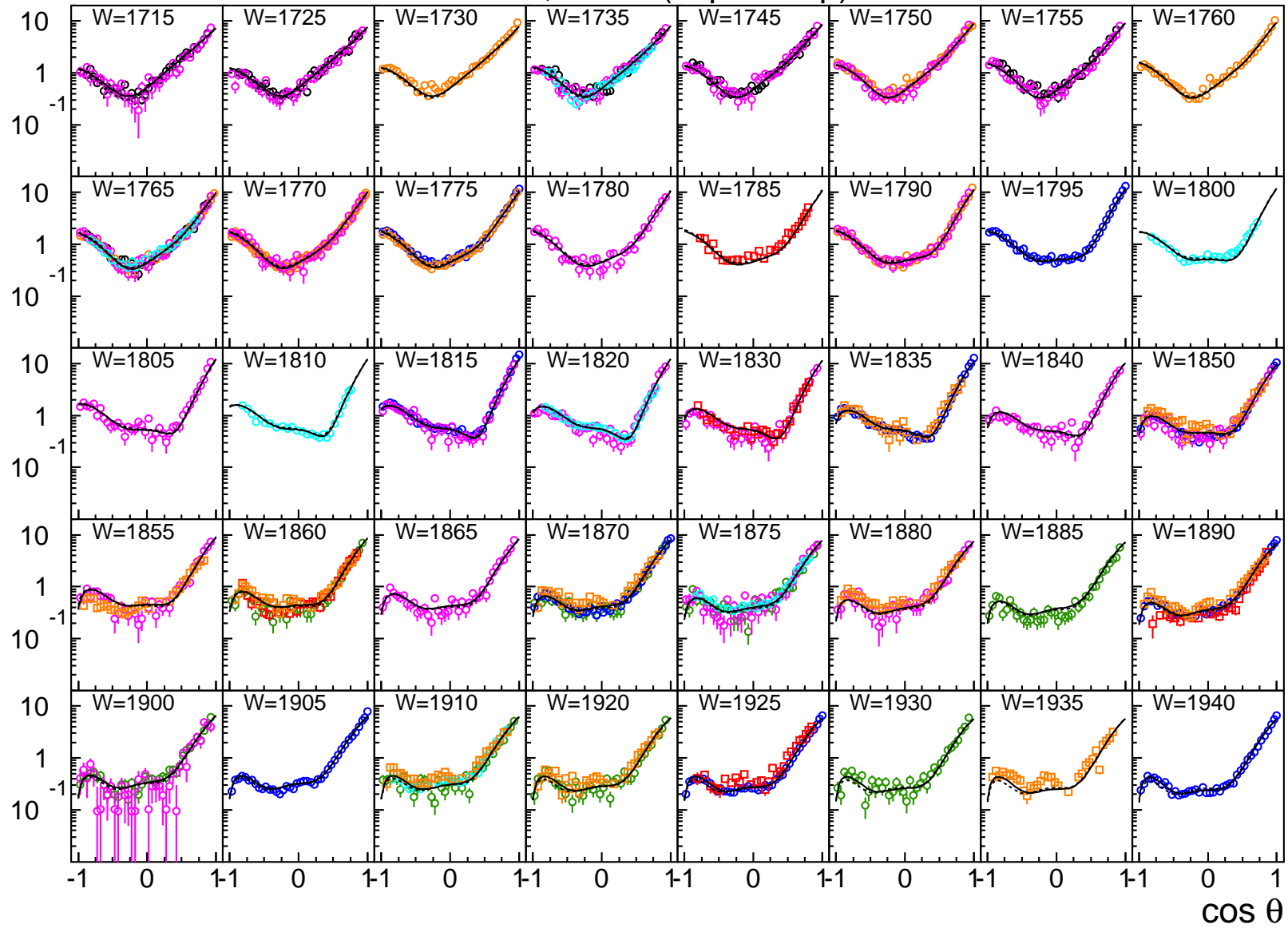
Table 3: List of reactions used in the partial wave analysis.

$K^- p \rightarrow K^0 n$	$K^- p \rightarrow K^- p$	$K^- p \rightarrow \omega \Lambda$
$K^- p \rightarrow \pi^0 \Lambda$	$K^- p \rightarrow \eta \Lambda$	$K^- p \rightarrow \pi^+ \Sigma^-$
$K^- p \rightarrow \pi^0 \Sigma^0$	$K^- p \rightarrow \pi^- \Sigma^+$	$K^- p \rightarrow \pi^0 \pi^0 \Lambda$
$K^- p \rightarrow K^+ \Xi^-$	$K^- p \rightarrow K^0 \Xi^0$	$K^- p \rightarrow \pi^0 \pi^0 \Sigma^0$

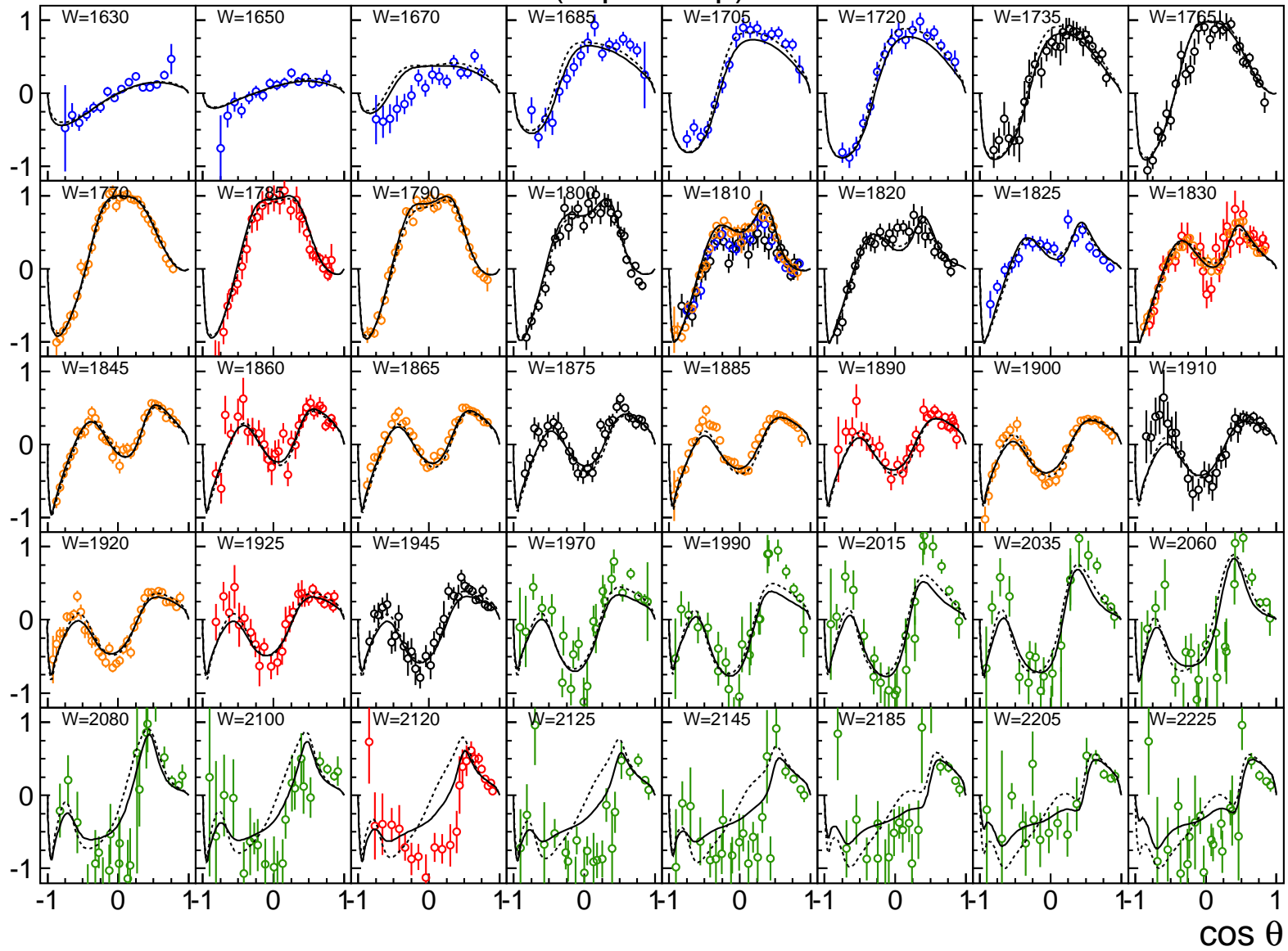
Mass scan of additional states



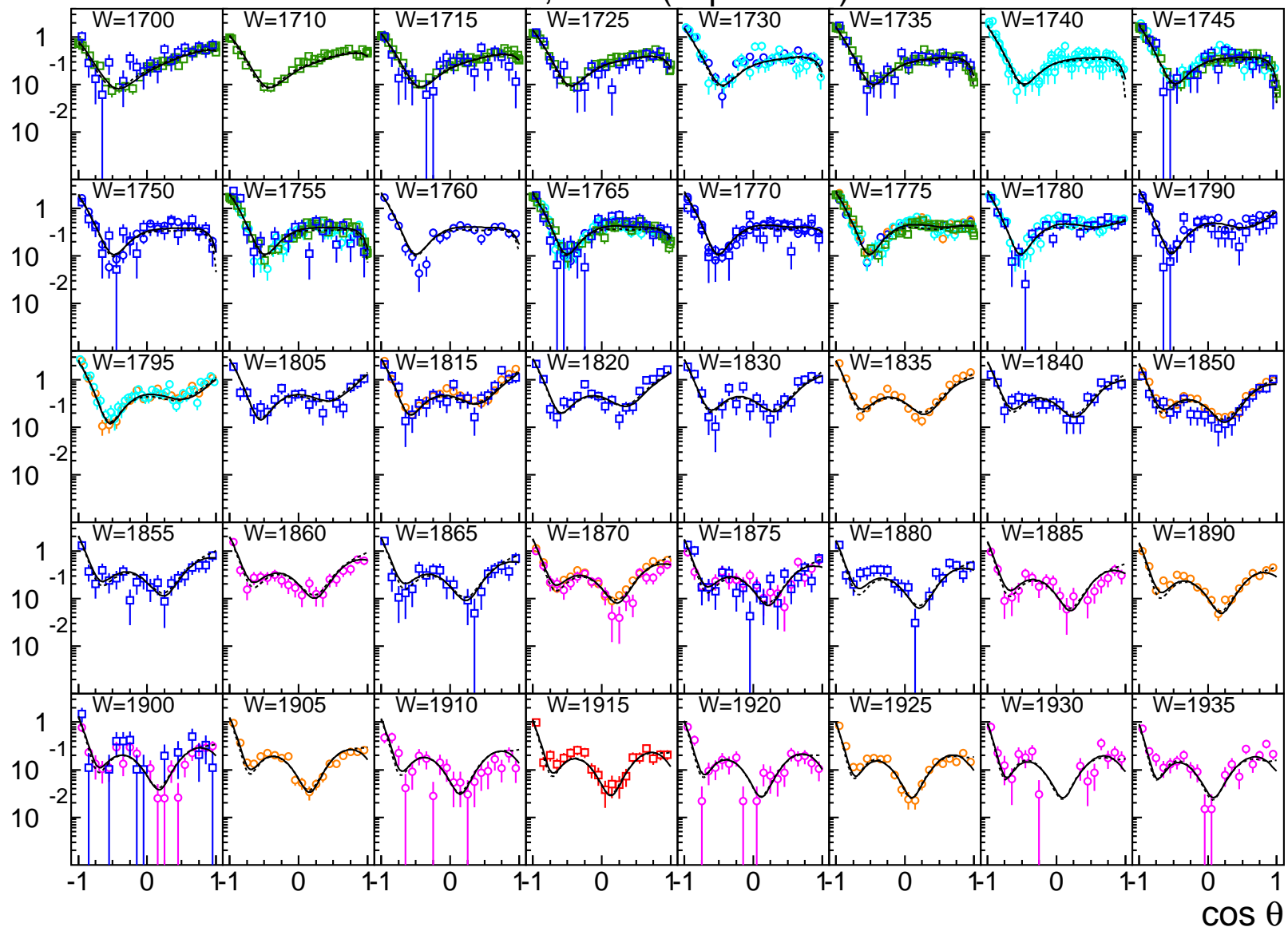
$d\sigma/d\Omega$, mb/sr ($K^-p \rightarrow K^-p$)



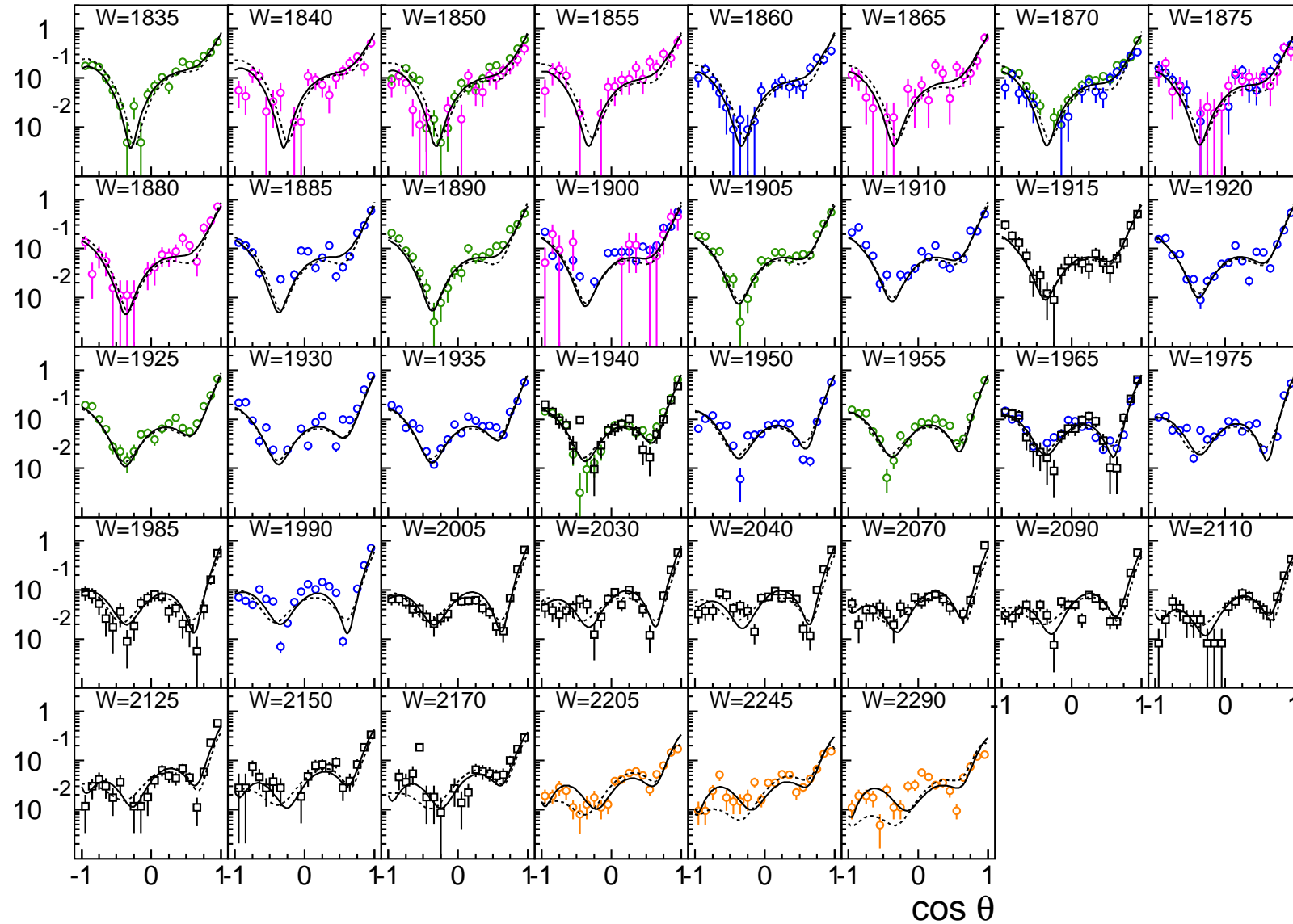
$P(K^-p \rightarrow K^-p)$

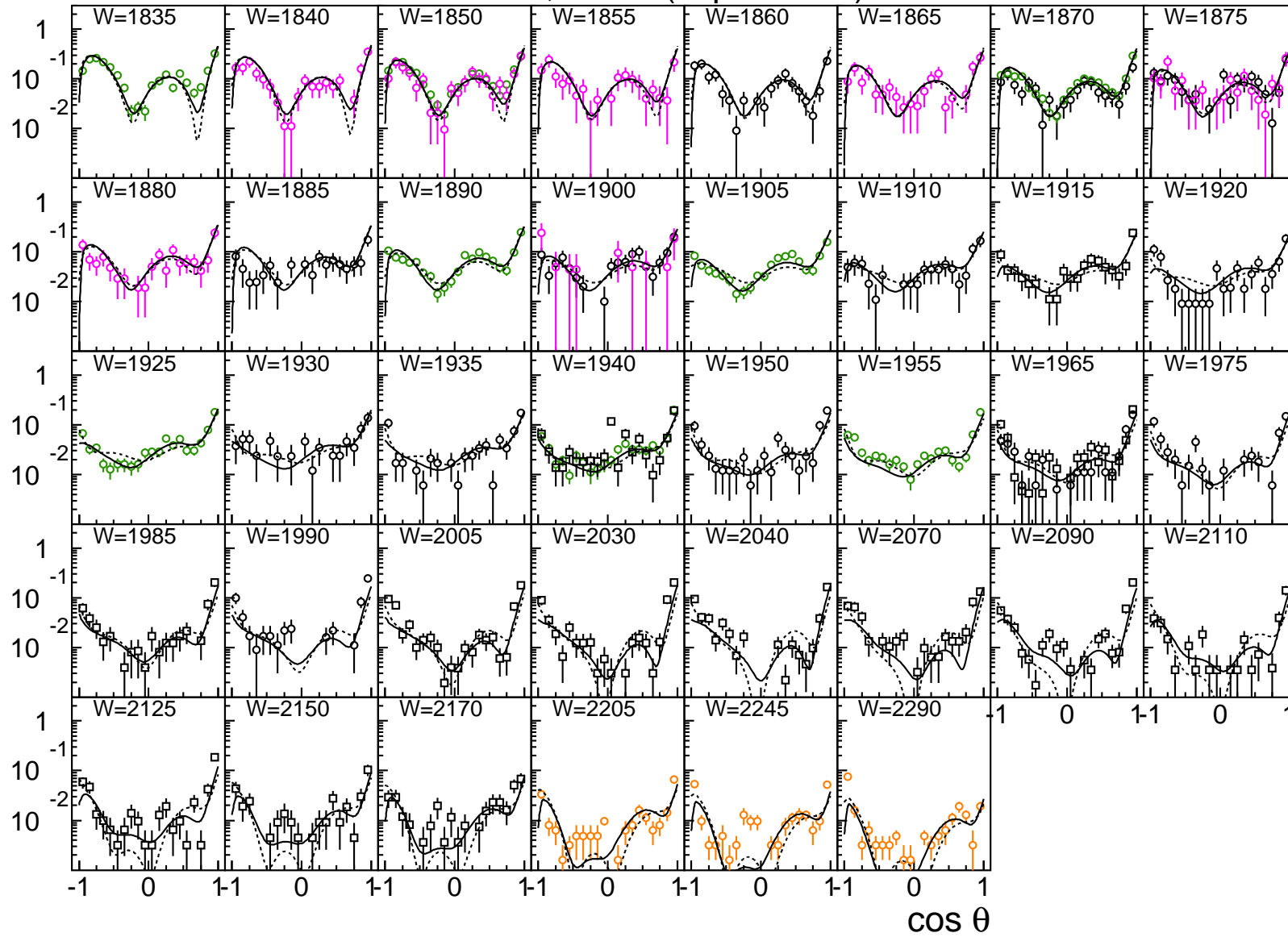


$d\sigma/d\Omega$, mb/sr ($K^-p \rightarrow K^0n$)

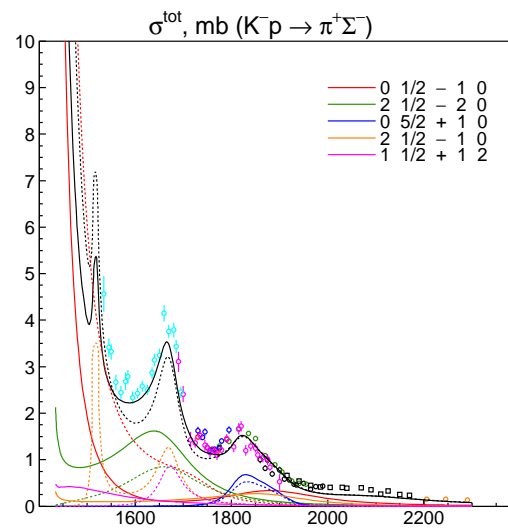
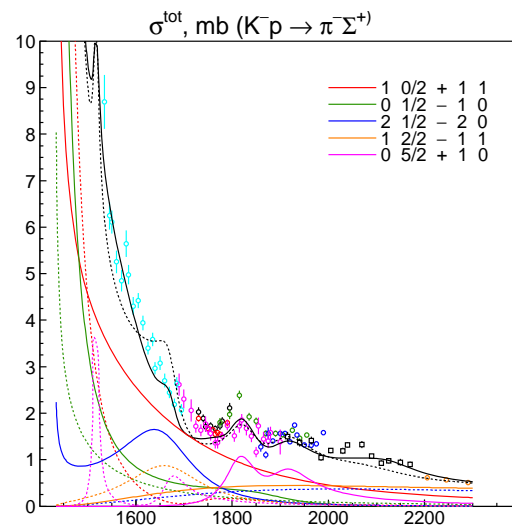
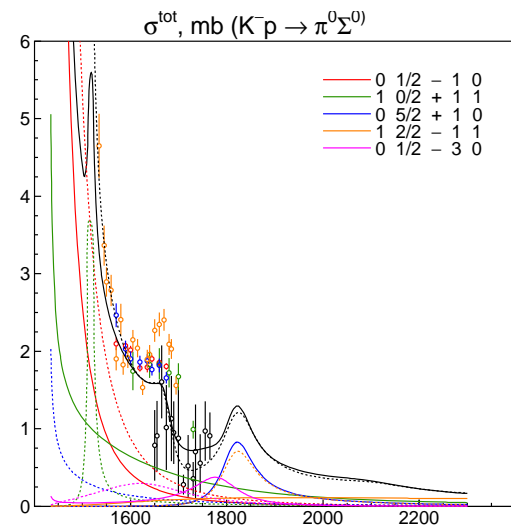
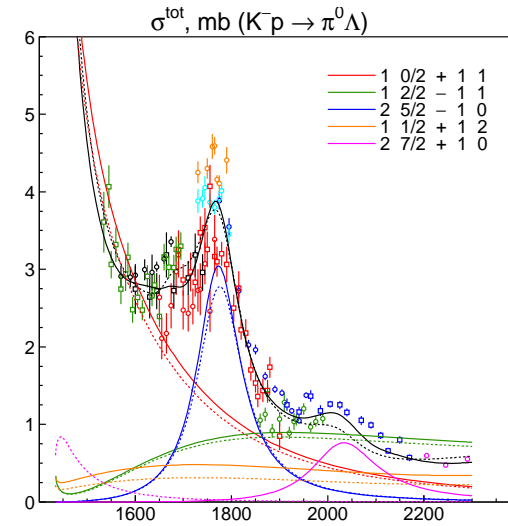
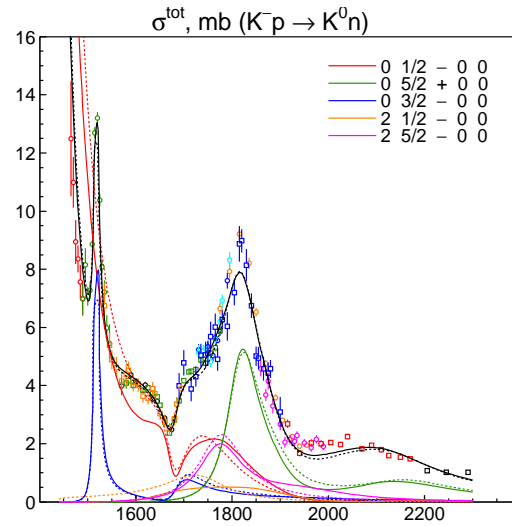
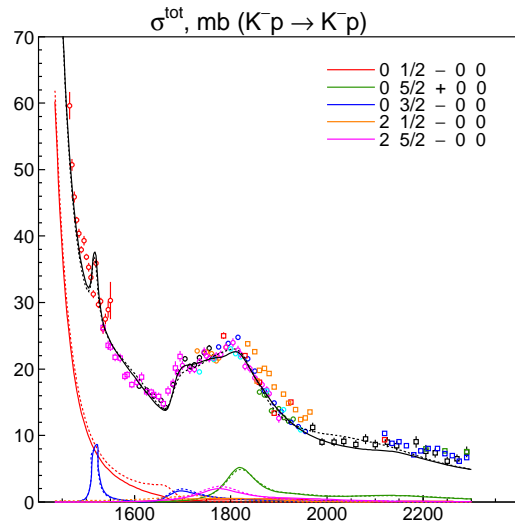


$d\sigma/d\Omega$, mb/sr ($K^-p \rightarrow \pi^- \Sigma^+$)



$$d\sigma/d\Omega, \text{ mb/sr } (K^- p \rightarrow \pi^+ \Sigma^-)$$


Analysis of the Kp collision reactions (Preliminary) (M. Matveev)



		ANL-Osaca	Bn-Ga	Model A	Model B	Bn-Ga
$K^- p \rightarrow K^- p$	$d\sigma/d\Omega$	3962	5170	3.07	2.98	1.80
	P	510	1180	2.04	2.08	1.41
$K^- p \rightarrow \bar{K}^0 n$	$d\sigma/d\Omega$	2950	3445	2.67	2.75	1.55
$K^- p \rightarrow \pi^- \Sigma^+$	$d\sigma/d\Omega$	1792	2455	3.37	3.49	1.45
	P	418	593	1.30	1.28	2.09
$K^- p \rightarrow \pi^0 \Sigma^0$	$d\sigma/d\Omega$	580	691	3.68	3.50	1.96
	P	196	124	6.39	5.80	2.41
$K^- p \rightarrow \pi^+ \Sigma^-$	$d\sigma/d\Omega$	1786	2082	2.56	2.18	1.59
$K^- p \rightarrow \pi^0 \Lambda$	$d\sigma/d\Omega$	2178	2478	2.59	3.71	1.66
	P	693	892	1.41	1.73	1.25
$K^- p \rightarrow \eta \Lambda$	$d\sigma/d\Omega$	160	160	2.69	2.03	1.50
$K^- p \rightarrow K^0 \Xi^0$	$d\sigma/d\Omega$	33	67	1.24	1.61	0.89
$K^- p \rightarrow K^+ \Xi^-$	$d\sigma/d\Omega$	92	193	2.05	1.74	1.31
$K^- p \rightarrow \Lambda \omega$	$d\sigma/d\Omega$	—	300	—	—	1.03
$K^- p \rightarrow \Lambda \omega$	$\rho_{00}, \rho_{10}, \rho_{1-1}$	—	158	—	—	1.30

Table 4: Σ -Hyperons Observed states

J^P		Known state	New state	Mass
$1/2^+$	$N(1440)$	$\Sigma(1660)$		
$3/2^+$	$\Delta(1230)$	$\Sigma(1385)$		
$5/2^+$	$N(1680), \Delta(1905)$	$\Sigma(1915)$????	
$7/2^+$	$N(1990), \Delta(1950)$	$\Sigma(2030)$????	
$3/2^-$	$N(1520)$	$\Sigma(1670)$		
$1/2^-$	$N(1535), \Delta(1620), N(1650)$	$\Sigma(1750)$	$\Sigma(1620)$	1680 ± 8
			$\Sigma(1900)$	1936 ± 10
$5/2^-$	$N(1675)$	$\Sigma(1775)$		
$3/2^-$	$N(1700), \Delta(1700)$	$\Sigma(1940)$	$\Sigma(1860)$	1856 ± 10
$1/2^-$	$N(1895)$		$\Sigma(2120)$	2158 ± 25

Let us consider the decay of the isospin 0 and isospin 1 states into $K^- p$ and $K^0 n$

$$|A(K^- p)|^2 = \left(A_1 \frac{1}{\sqrt{2}} + A_0 \frac{1}{\sqrt{2}} \right)^2 = \frac{1}{2} (|A_1|^2 + |A_0|^2 + 2\text{Re}(A_1 A_0^*))$$

$$|A(K^0 n)|^2 = \left(A_1 \frac{1}{\sqrt{2}} - A_0 \frac{1}{\sqrt{2}} \right)^2 = \frac{1}{2} (|A_1|^2 + |A_0|^2 - 2\text{Re}(A_1 A_0^*))$$

$$A_{KN} = \omega^* [G(s, t) + H(s, t)i(\vec{\sigma}\vec{n})] \omega' \quad \vec{n}_j = \varepsilon_{\mu\nu j} \frac{q_\mu k_\nu}{|\vec{k}||\vec{q}|}.$$

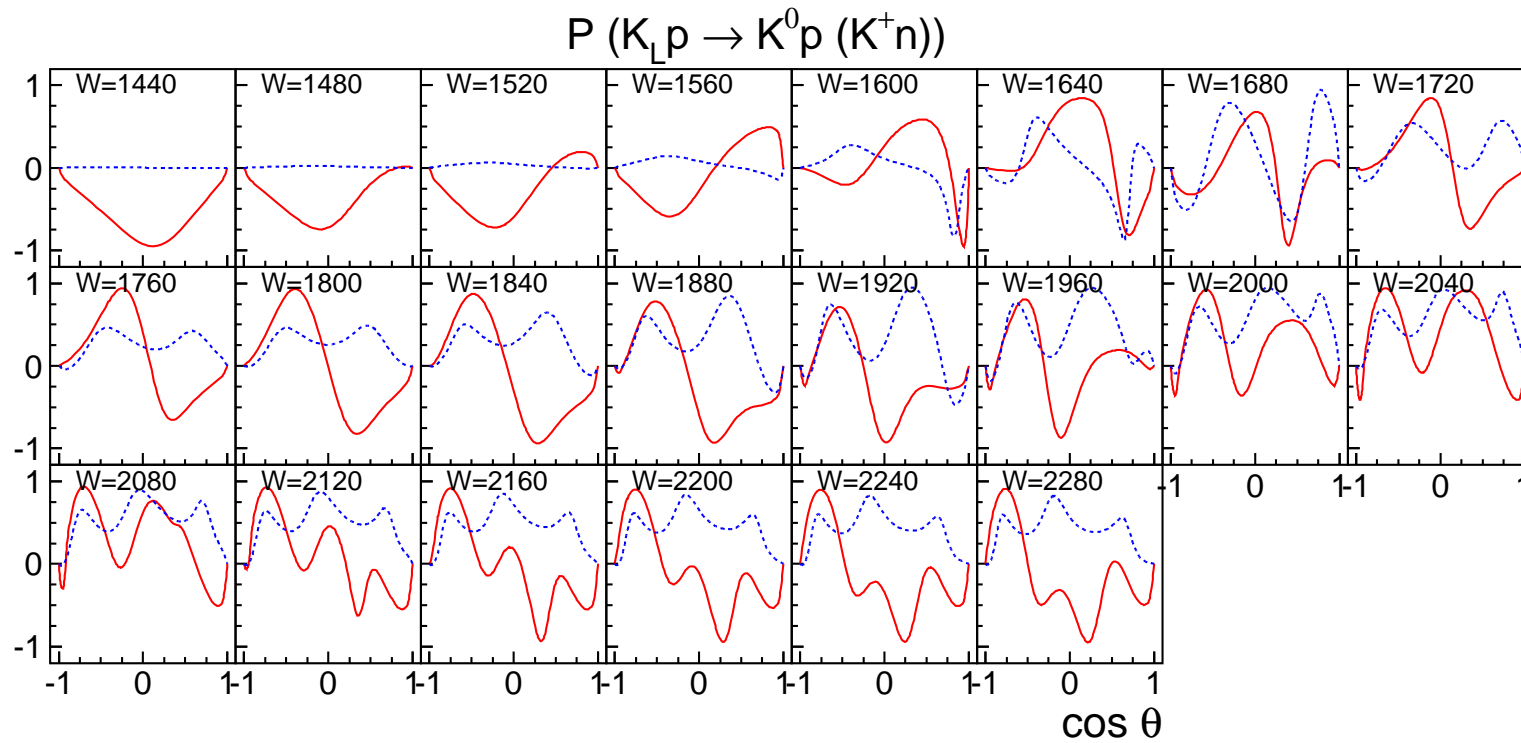
Differential cross section in c.m.s. of the reaction

$$|A|^2 = \frac{1}{2} \text{Tr} [A_{\pi N}^* A_{\pi N}] = |G(s, t)|^2 + |H(s, t)|^2 (1 - z^2)$$

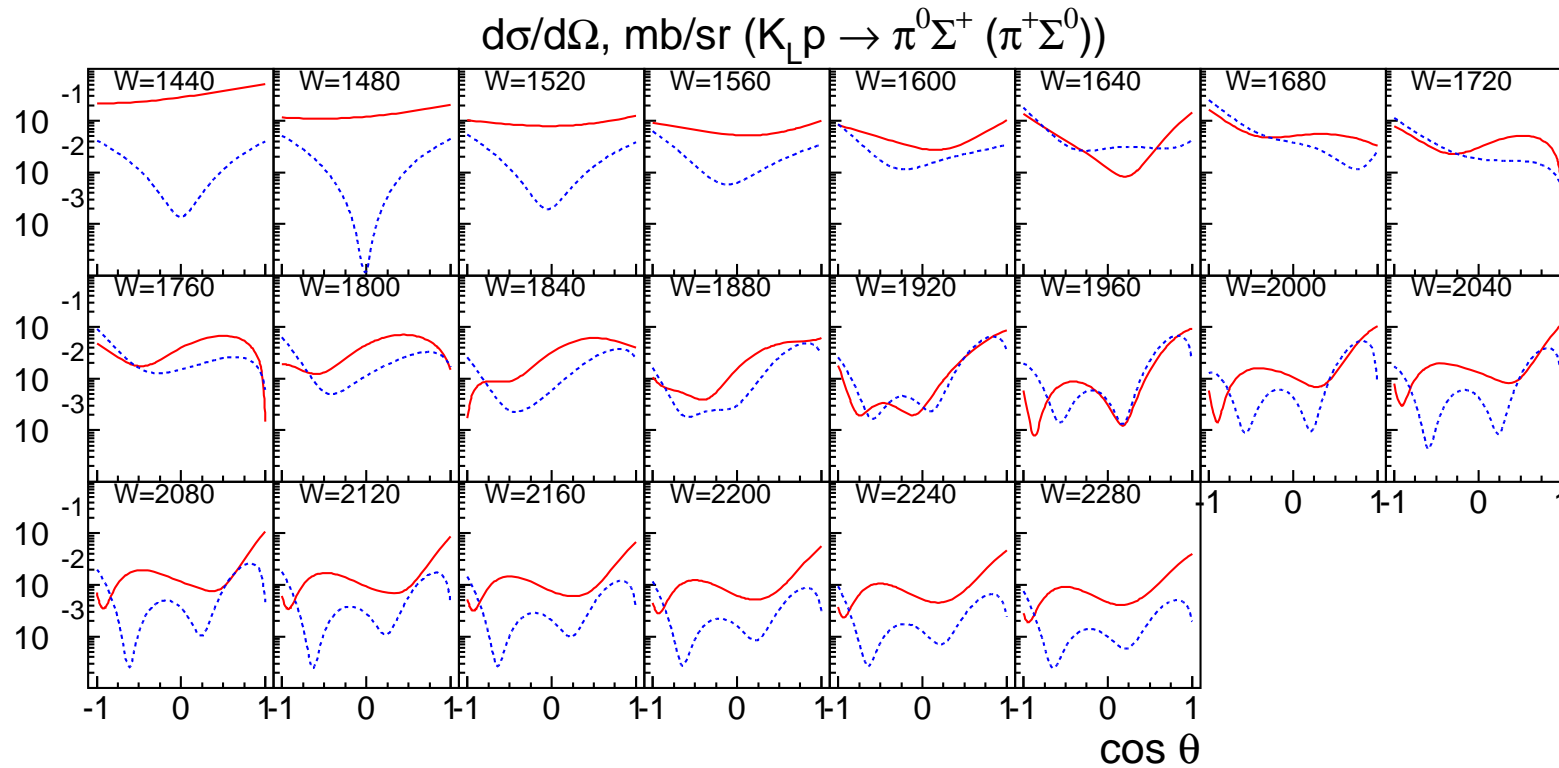
the recoil asymmetry:

$$P = \frac{\text{Tr} [A_{\pi N}^* \sigma_2 A_{\pi N}]}{2|A|^2 \cos \phi} = \sin \Theta \frac{2\text{Im} (H^*(s, t)G(s, t))}{|A|^2}.$$

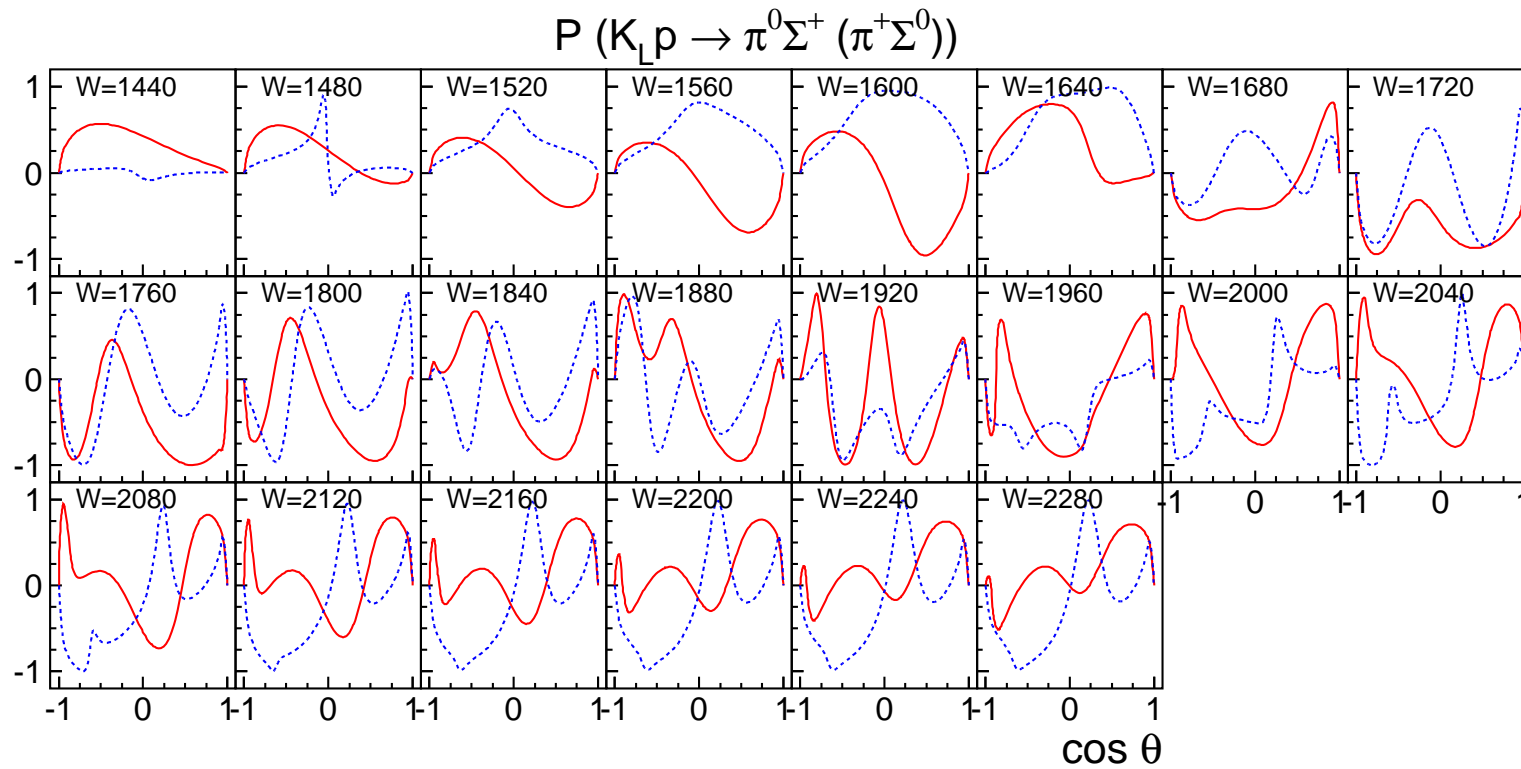
Prediction for the recoil asymmetry $K_L p \rightarrow K^0 p(K^+ n)$



Prediction for $\frac{d\sigma}{d\Omega} (K_L p \rightarrow \pi^0 \Sigma^+ (\pi^+ \Sigma^0))$

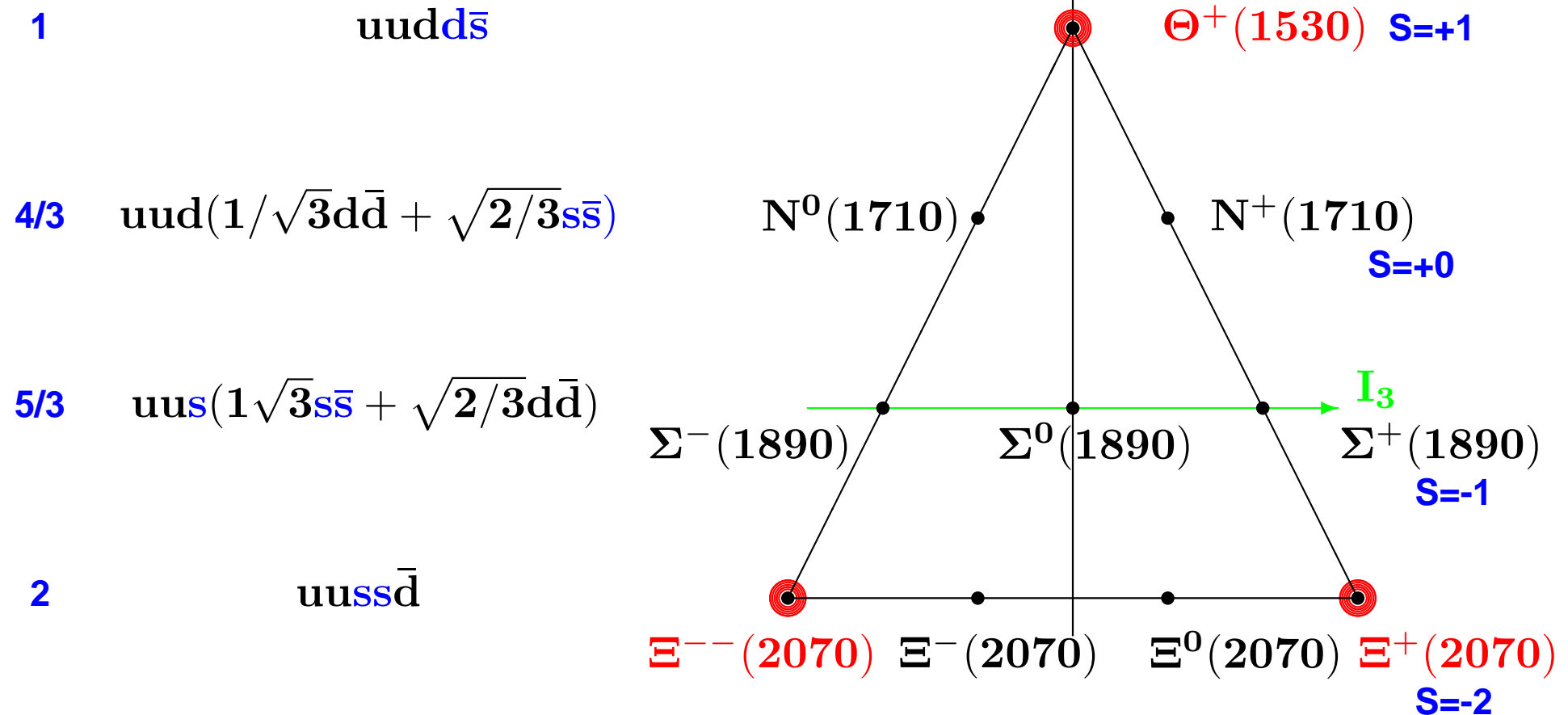


Prediction for the recoil asymmetry $K_L p \rightarrow \pi^0 \Sigma^+ (\pi^+ \Sigma^0)$



The chiral soliton model (Дьяконов, Петров, Поляков) predicts the existence of an **antidecuplet**:

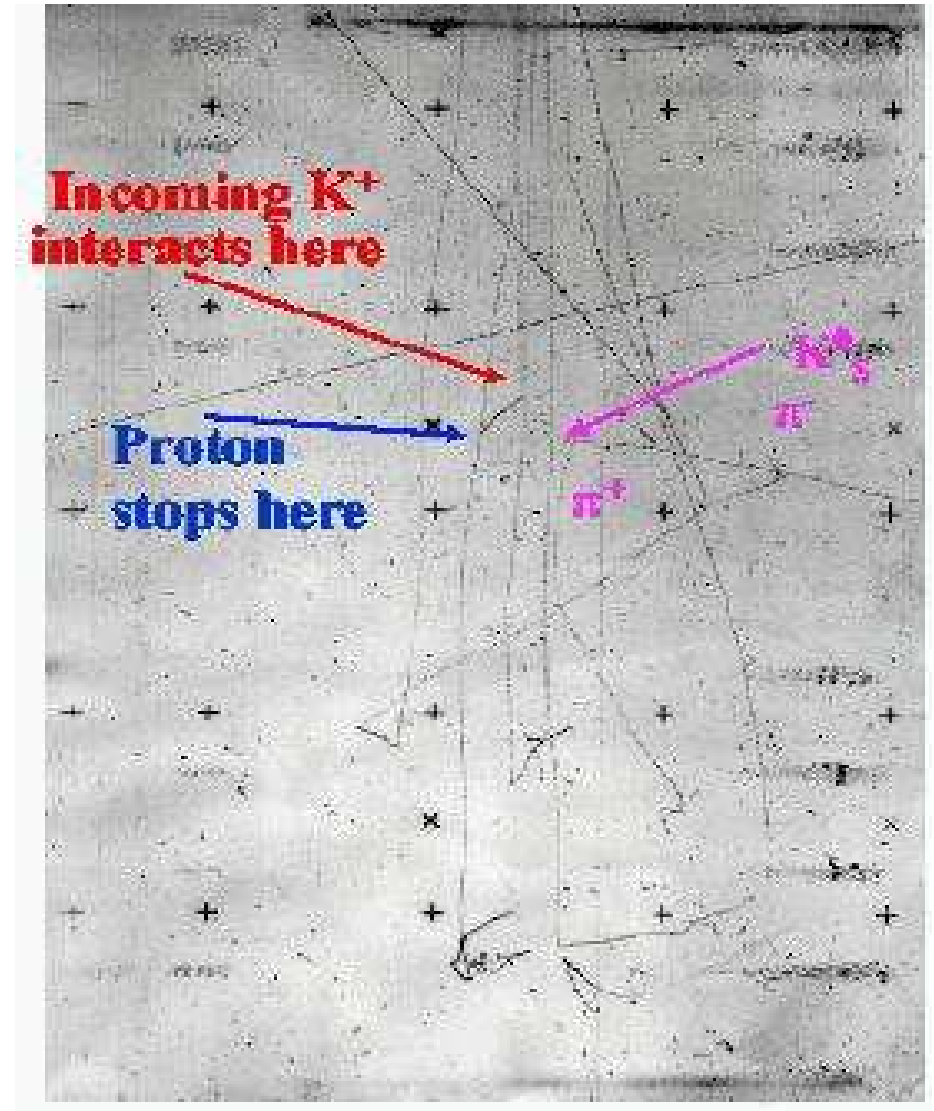
Antidecuplet



DIANA/ITEP:

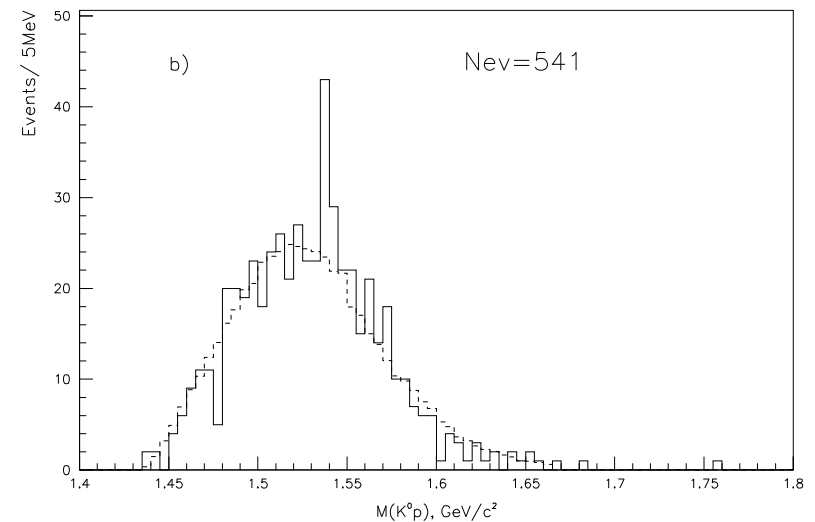
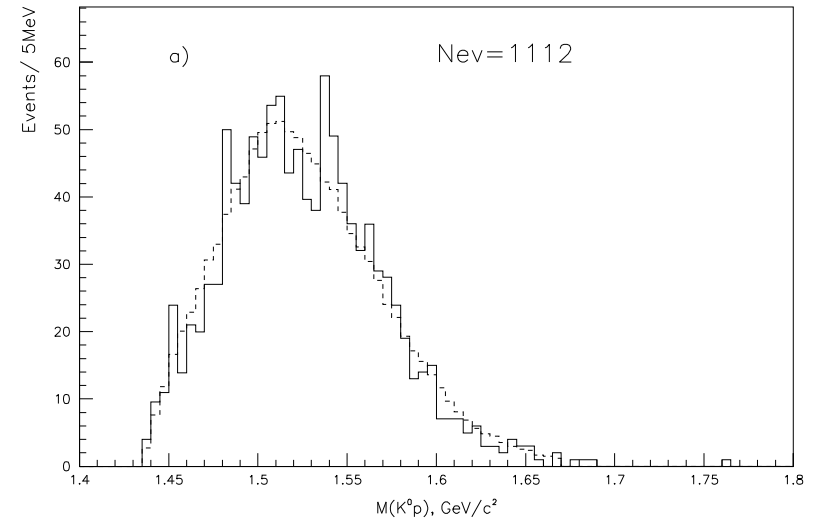
Charge exchange expt.

- $K^+n \rightarrow \Theta^+(1540) \rightarrow pK_s^0$
- 'quasifree' in Xe bubble chamber
- $K^+Xe \rightarrow Xe'pK_s^0$
- K^+ momentum from range in Xe



- Stereo photos taken and evaluated
- secondary vertex $K_s^0 \rightarrow \pi^+ \pi^-$
- and a proton track
- Particle ID and momentum from track (density and range)
- 41,000 K^+ tracked
- 73 seen Θ^+ 300 produced ('two-body' cut, nK^+)

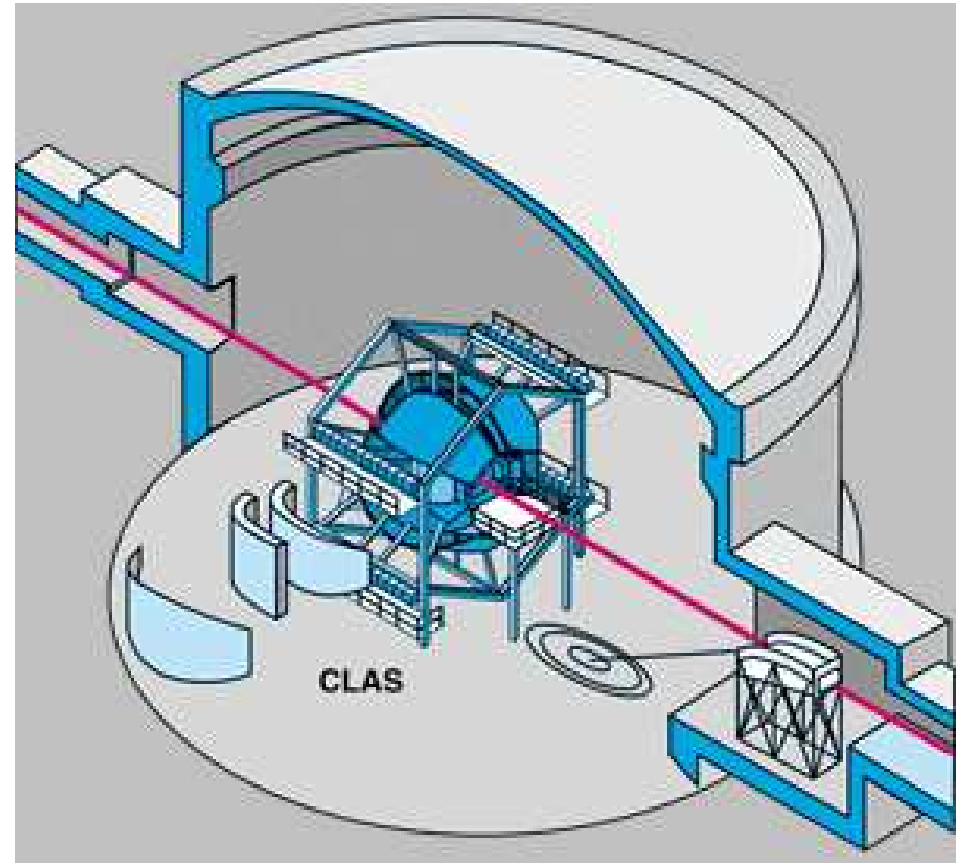
The width of the Θ^+ is < 9 MeV



pK_s^0 invariant mass for all protons (top) and loose 'two-body' cut

CLAS/Jlab:

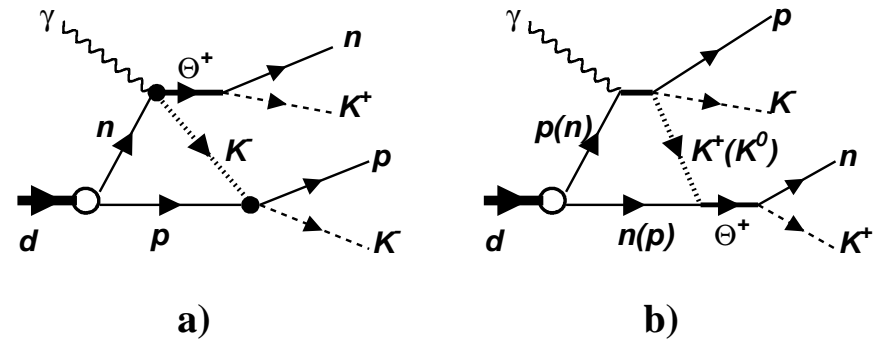
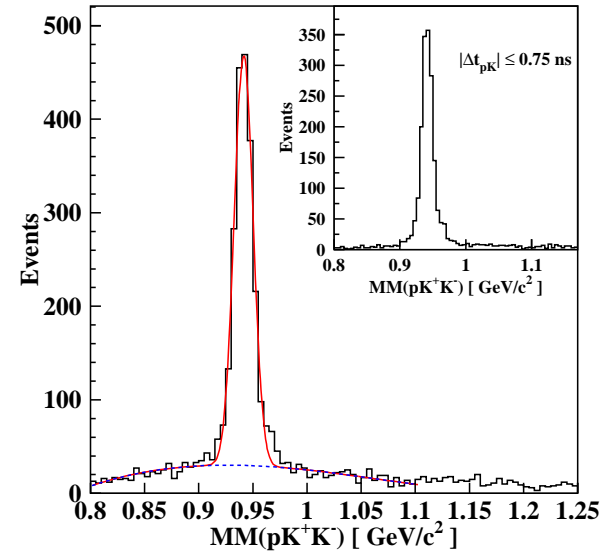
- Torus magnet with 6 superconducting coils
- Liquid H_2/D_2 target, trigger counters
- Drift chambers with 35,000 cells
- TOF system
- Electromagnetic Pb/sci sandwich calorimeter
- Gas Cerenkov counters, e/π separation



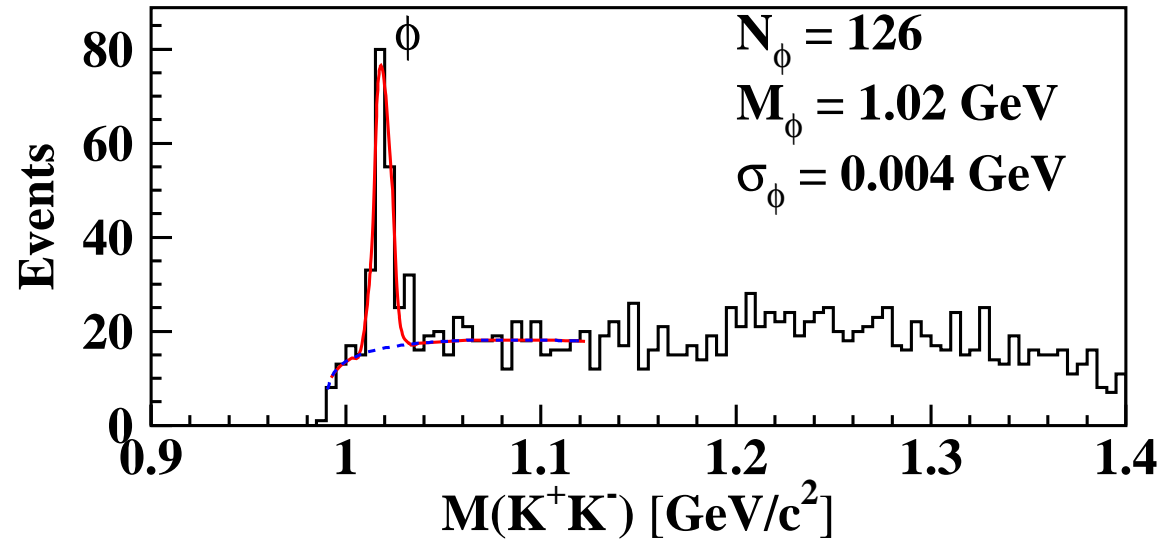
Study of the reaction



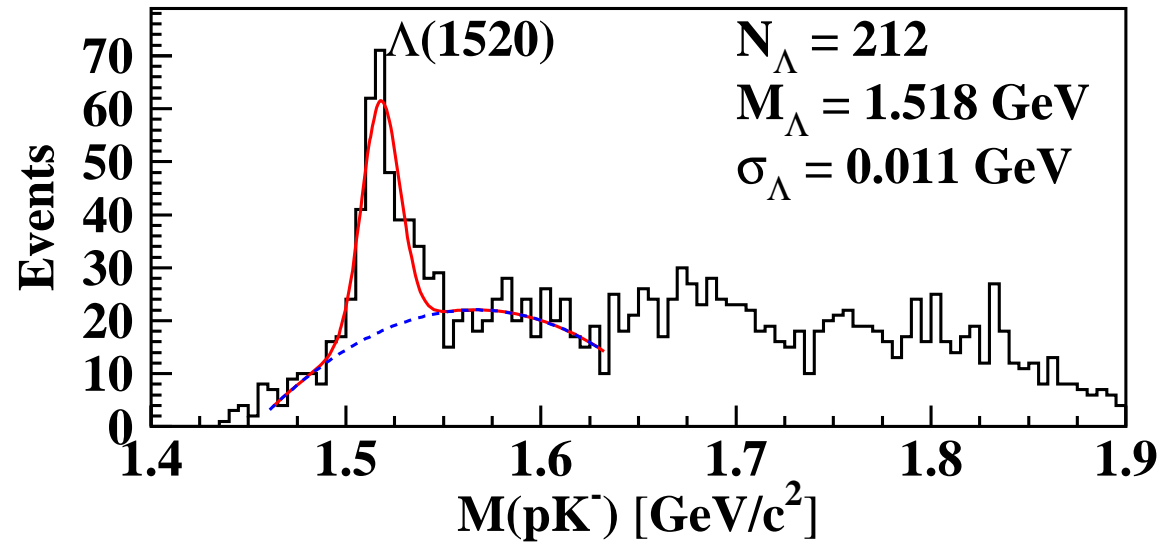
1. **Detected:** K^+, K^-, p , hence
"no spectator" nucleon
2. TOF for particle identification
3. Missing mass calculated and
neutron reconstructed
4. Proposed reaction mechanisms:



The K^+K^- invariant mass



The pK^- invariant mass



The nK^+ invariant mass

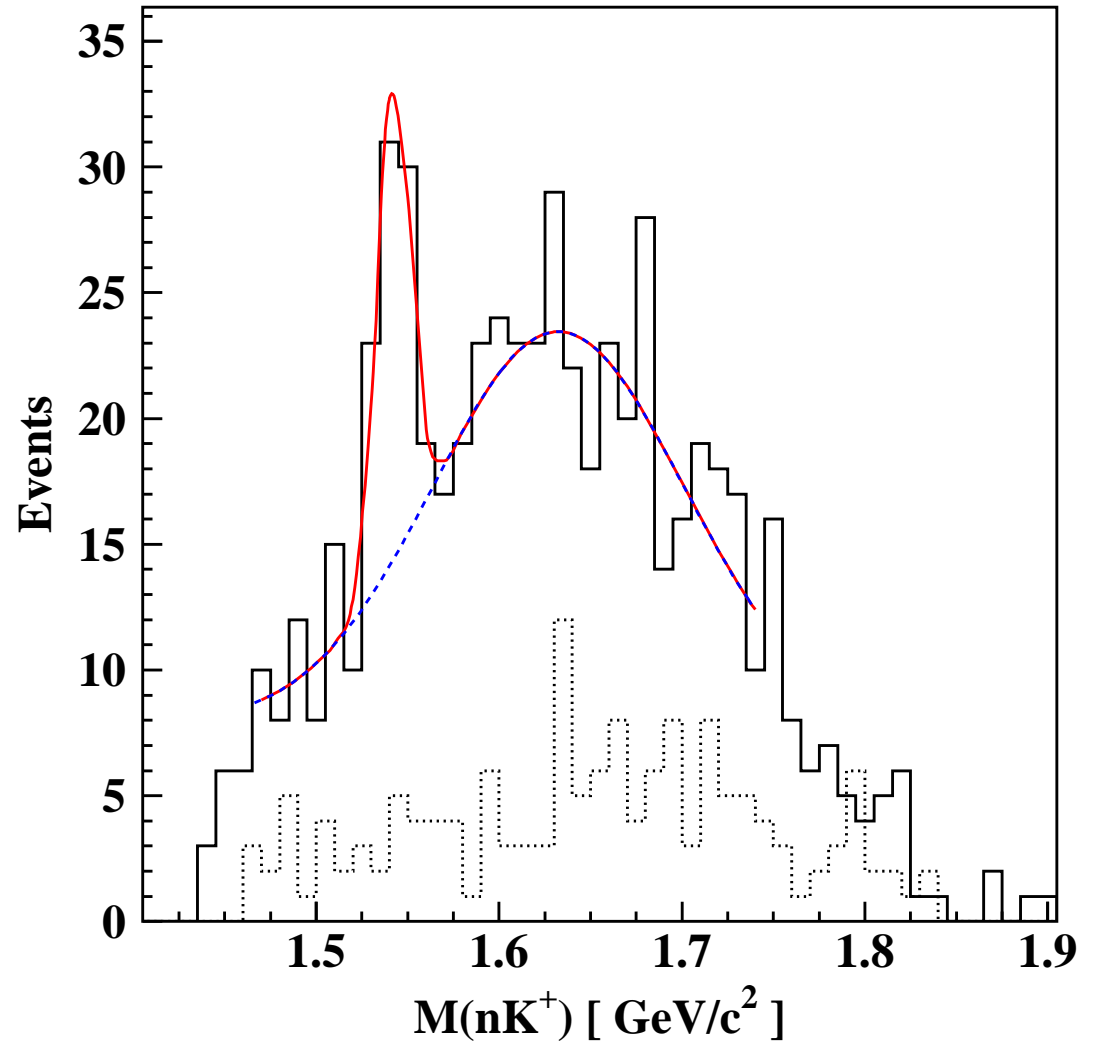
$$M_{\Theta^+} = 1542 \pm 5 \text{ MeV}$$

$$\Gamma_{\Theta^+} \leq 21 \text{ MeV}$$

Decay: nK^+

Yield: 212 $\Lambda(1520)$,

43 Θ^+

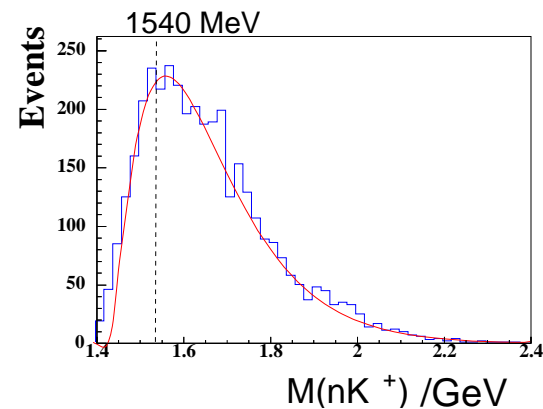
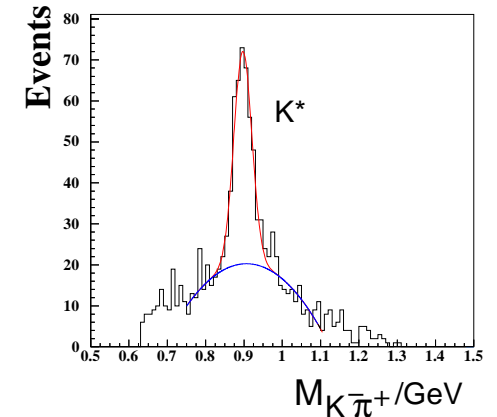
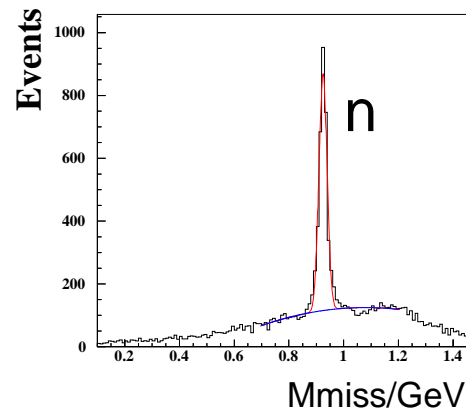
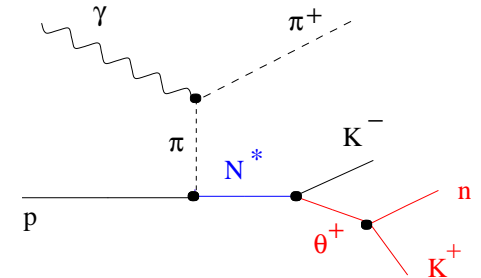
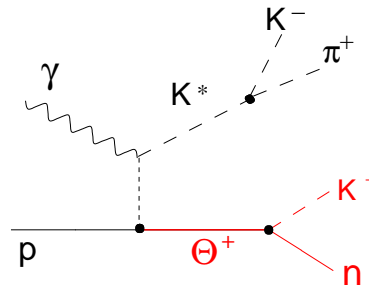


Study of the reaction



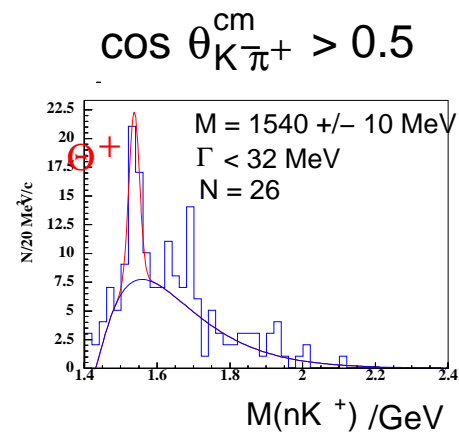
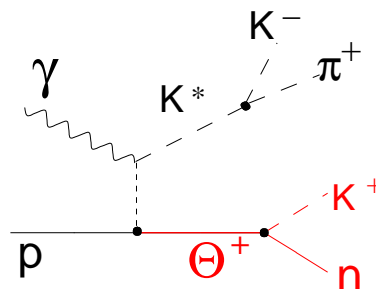
1. Detected: K^+ , K^- , π^+
2. TOF for particle identification
3. Missing neutron reconstructed from kinematics

possible reaction mechanisms:

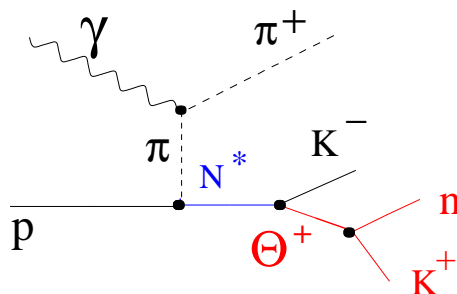


no signal without further cuts !

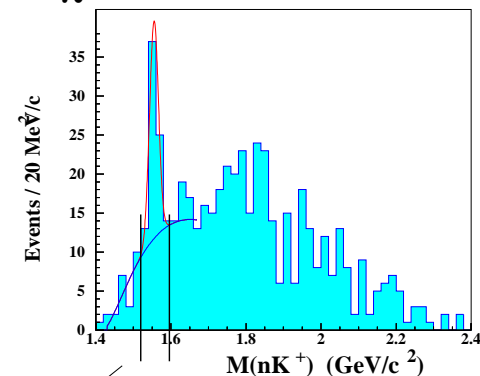
$\Theta^+(1540)$ seen after cut in angle \Rightarrow 26 Θ^+



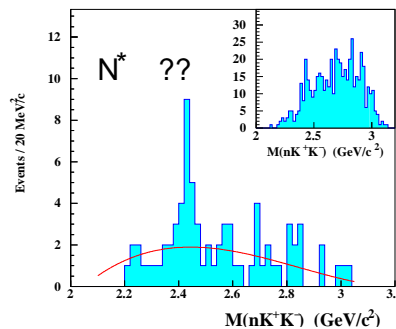
Does the $\Theta^+(1540)$ come from a $N^*(2400)$?
 42 Θ^+



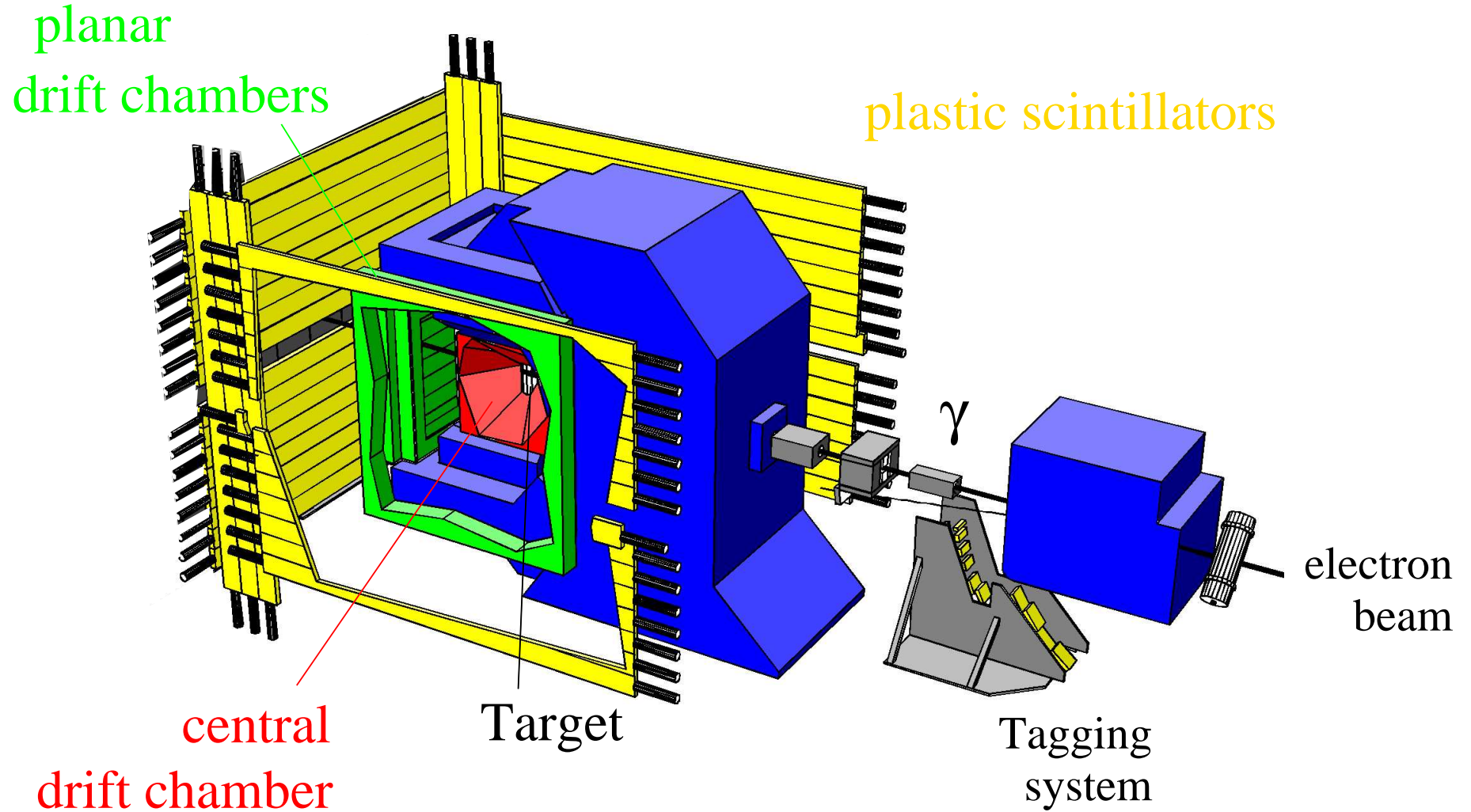
$\cos \theta_{\pi^+}^{\text{cm}} > 0.8$ $\cos \theta_{K^+}^{\text{cm}} < 0.6$

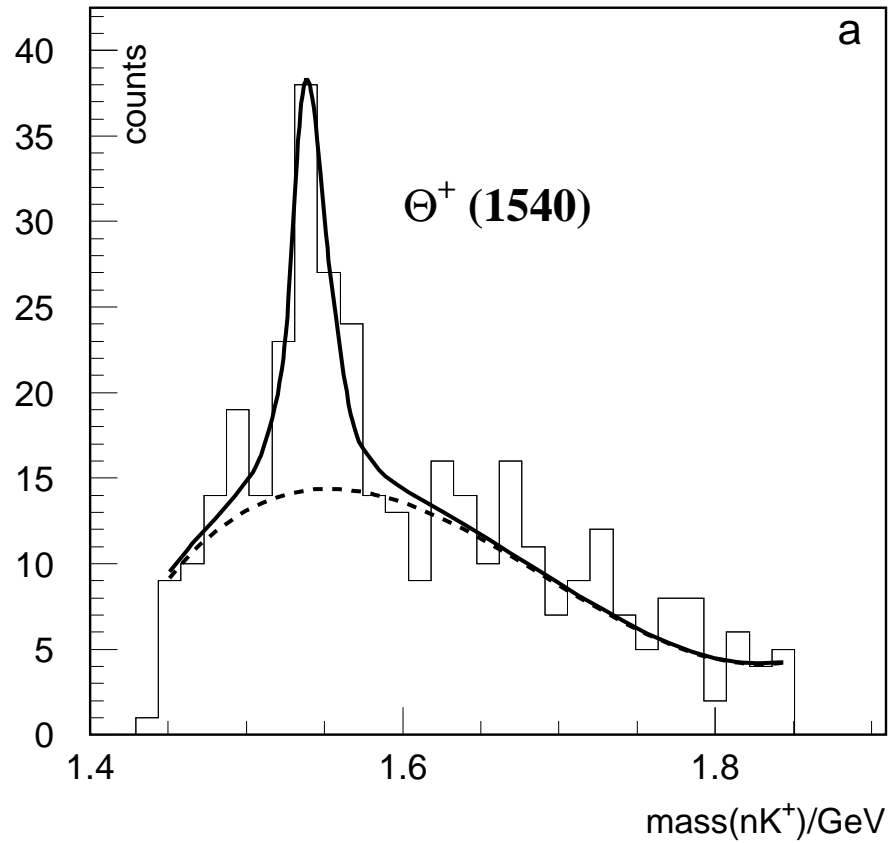


$M = 1555 \pm 20 \text{ MeV}$
 $\Gamma < 26 \text{ MeV}$



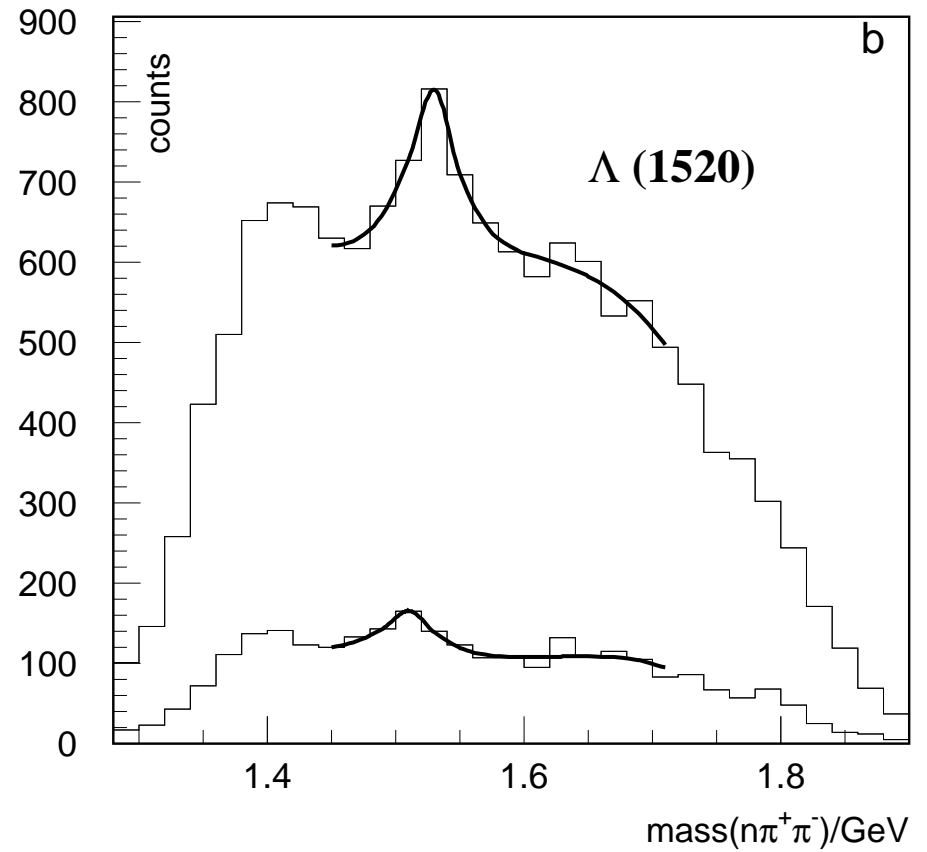
SAPHIR/ELSA:



$\gamma p \rightarrow n K^+ K_s^0$ 

nK^+ mass with $\pi^+\pi^- = K_s^0$

Left: $\cos \vartheta_{K_s^0} > 0.5$



nK_s^0 mass with $\pi^+\pi^- = K_s^0$

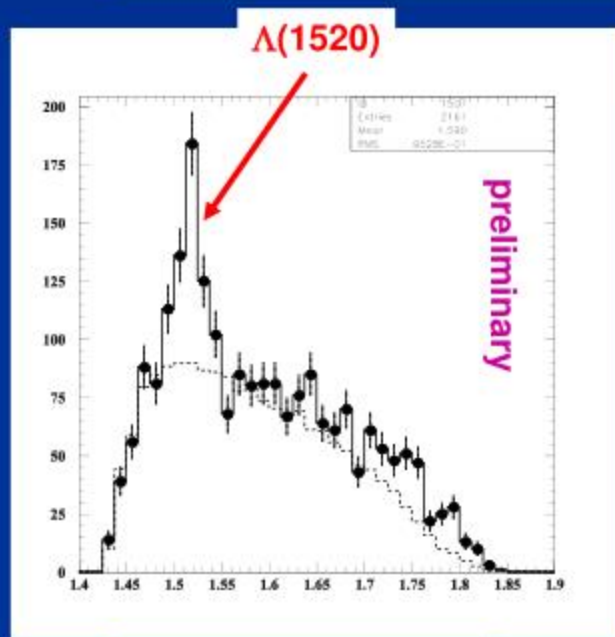
Right: with/without $\cos \vartheta_{K_s^0} > 0.5$

Old and New Signal from LEPS/SPring8

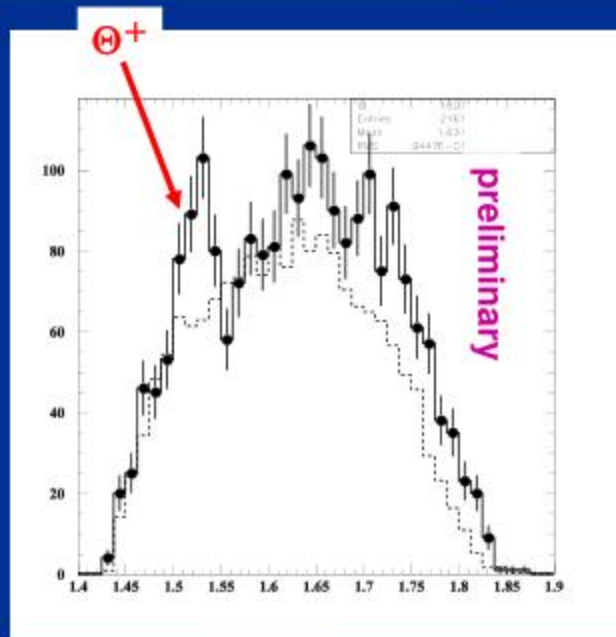
N. Muramatsu

$\gamma D \rightarrow K X$

- Mix K^+ , K^- , γ from different events in LH_2 data.
- $\Lambda(1520)$ contribution was removed from the sample.



$MM^C(\gamma, K^+) \text{ GeV}/c^2$



$MM^C(\gamma, K^-) \text{ GeV}/c^2$

Θ^+ : Comparison of different results

experiment	reaction	decay channel	mass (MeV)	statistical significance
Spring-8	$\gamma n \rightarrow K^- \Theta^+$	$K^+ n$	1540 ± 10	5σ
DIANA	$K^+ n \rightarrow K^- \Theta^+$	$K_S^0 p$	1539 ± 2	4σ
SAPHIR	$\gamma p \rightarrow \overline{K}_S^0 \Theta^+$	$K^+ n$	1540 ± 6	5σ
CLAS	$\gamma n \rightarrow K^- p \Theta^+$	$K^+ n$	1542 ± 5	5σ
CLAS	$\gamma p \rightarrow K^- \pi^+ \Theta^+$	$K^+ n$	1555 ± 10	8σ
CLAS	$\gamma p \rightarrow \overline{K}_S^0 \Theta^+$	$K^+ n$	1571 ± 10	
BC	$\nu A \rightarrow \Theta^+ \mathbf{X}$	$K_S^0 p$	1533 ± 5	7σ
HERMES	$ed \rightarrow \Theta^+ \mathbf{X}$	$K_S^0 p$	1526 ± 5	6σ

width determination limited by experimental resolution $\Gamma < 20 MeV$

The most worrying results from kaon (meson) beams

Total cross section:

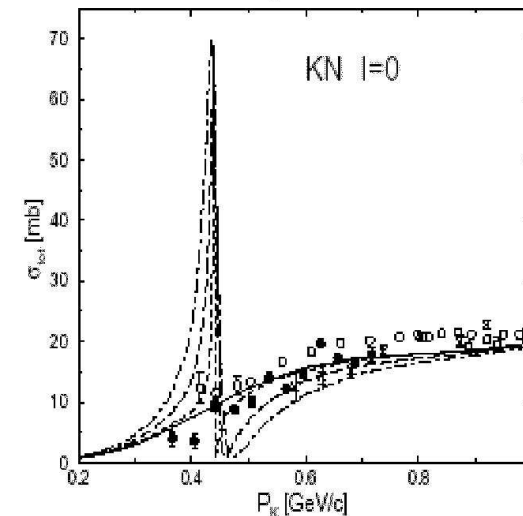
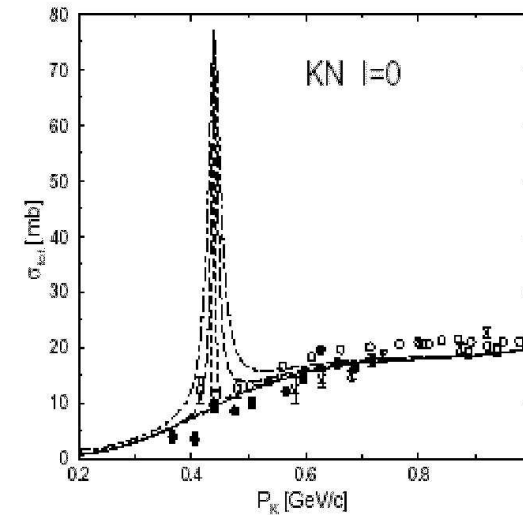
$$\sigma = \frac{4\pi}{k^2} \frac{(2J+1)0.389}{(2S_1+1)(2S_2+1)} B_{in} B_{out}$$

$$k^2 = \frac{(M^2 - (m_p + m_K)^2)(M^2 - (m_p - m_K)^2)}{4M^2}$$

$$M = 1540 \text{ MeV} \quad k^2 = 0.073 \text{ MeV}^2$$

$$\text{If e.g. } B_{in} = B_{out} = 1$$

$$\sigma = 70 \text{ mb}$$

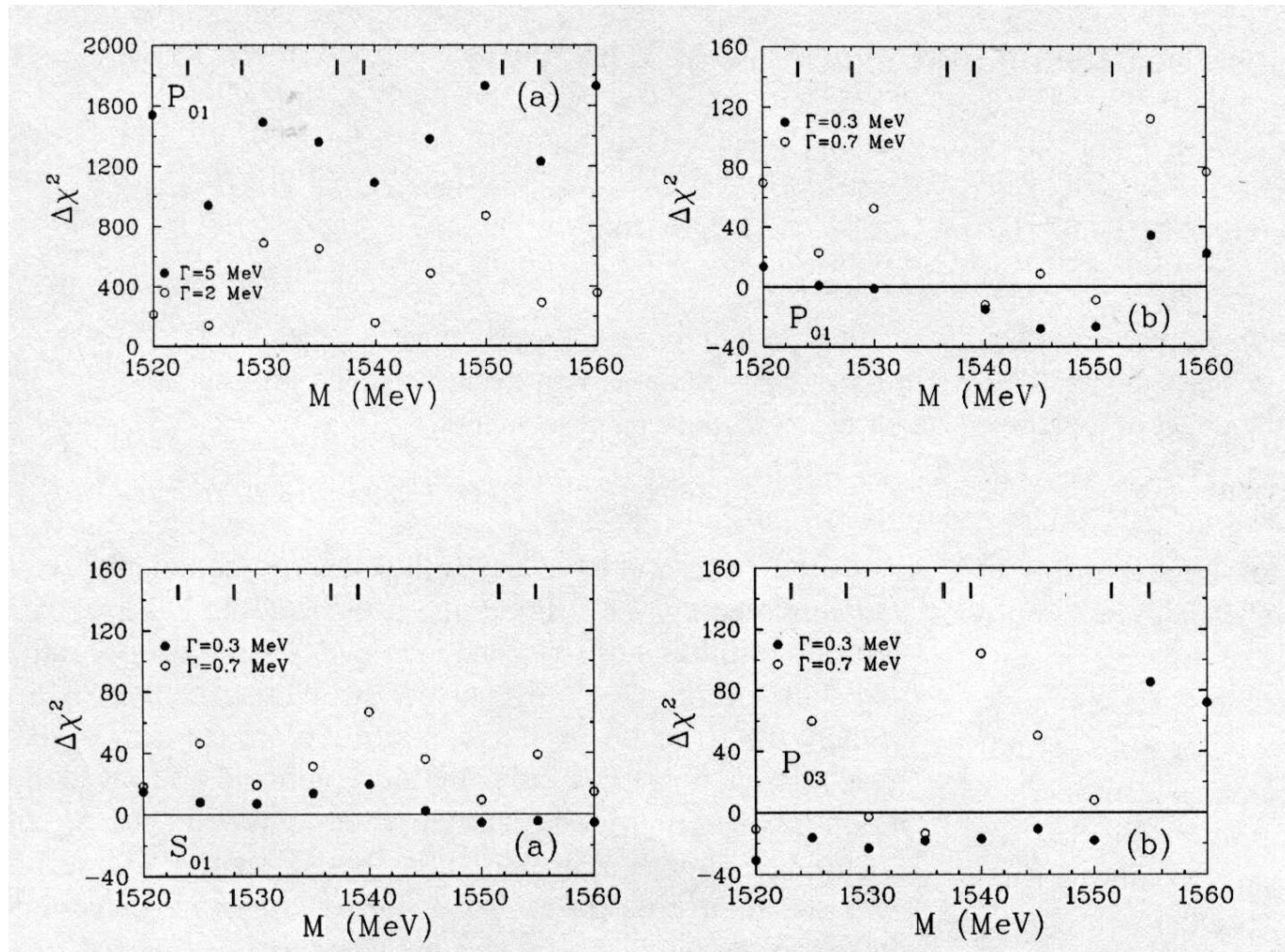


Study of K^+ -nucleon scattering

R.A. Arndt, I.I. Strakovsky and R.L. Workman

Restrictions on
width of Θ^+ :

$$\Gamma < 2 \text{ MeV}$$



Combined analysis of Θ^+ production in **Kaon** induced experiments

J. Haidenbauer, S. Krewald, A. Sibirtsev, Ulf-G. Meissner

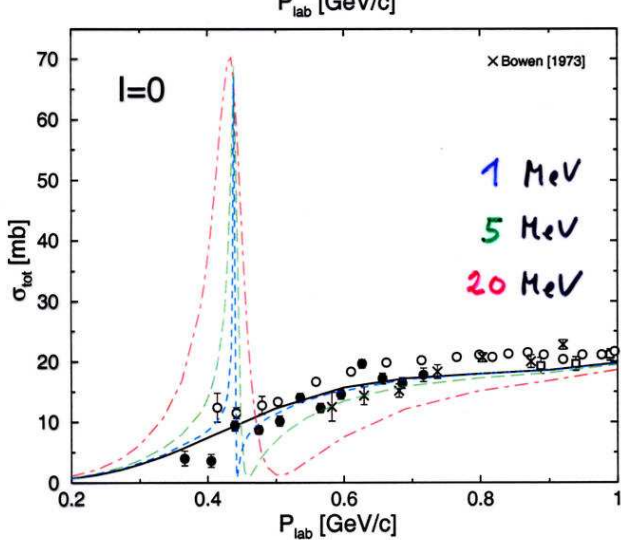
Reactions: $K^+ d \rightarrow K^0 + p + p$

$$K^+ d \rightarrow K^+ + n + p$$

$$K^+ d \rightarrow K^+ d$$

$K_L p$ - scattering

$$\Gamma < 1 \text{ MeV} \quad \text{even} \quad \Gamma < 0.8 \text{ MeV}$$



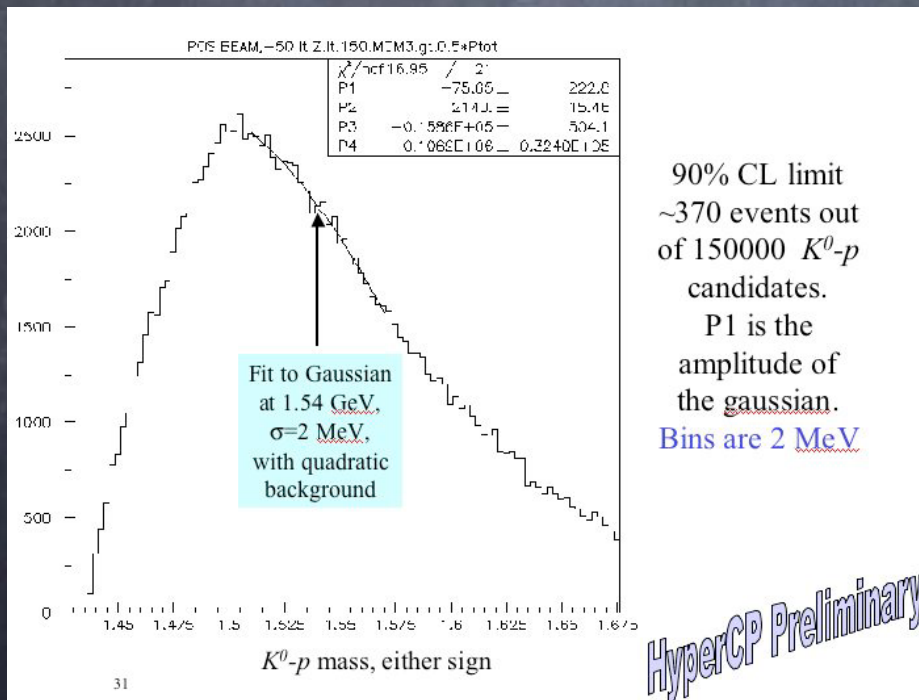
$$\sigma \propto \frac{1}{k^2} \sum_l \sin^2 \delta_l(k)$$

FNAL E871/HyperCP Experiment

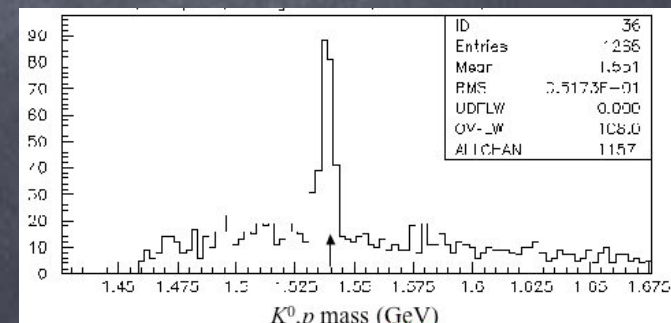
- Designed for studying CP violation in the hyperon decay sequence, $\Xi \rightarrow \Lambda\pi$, $\Lambda \rightarrow p\pi$.
- Hyperon channel, fast chambers, simple trigger, high resolution spectrometer, fast DAQ
- Took data in 1997 and 1999
- Mixed beam with protons, pions, kaons, hyperons, with a broad momentum spread, ~ 120 -250 GeV/c.

Data Summary

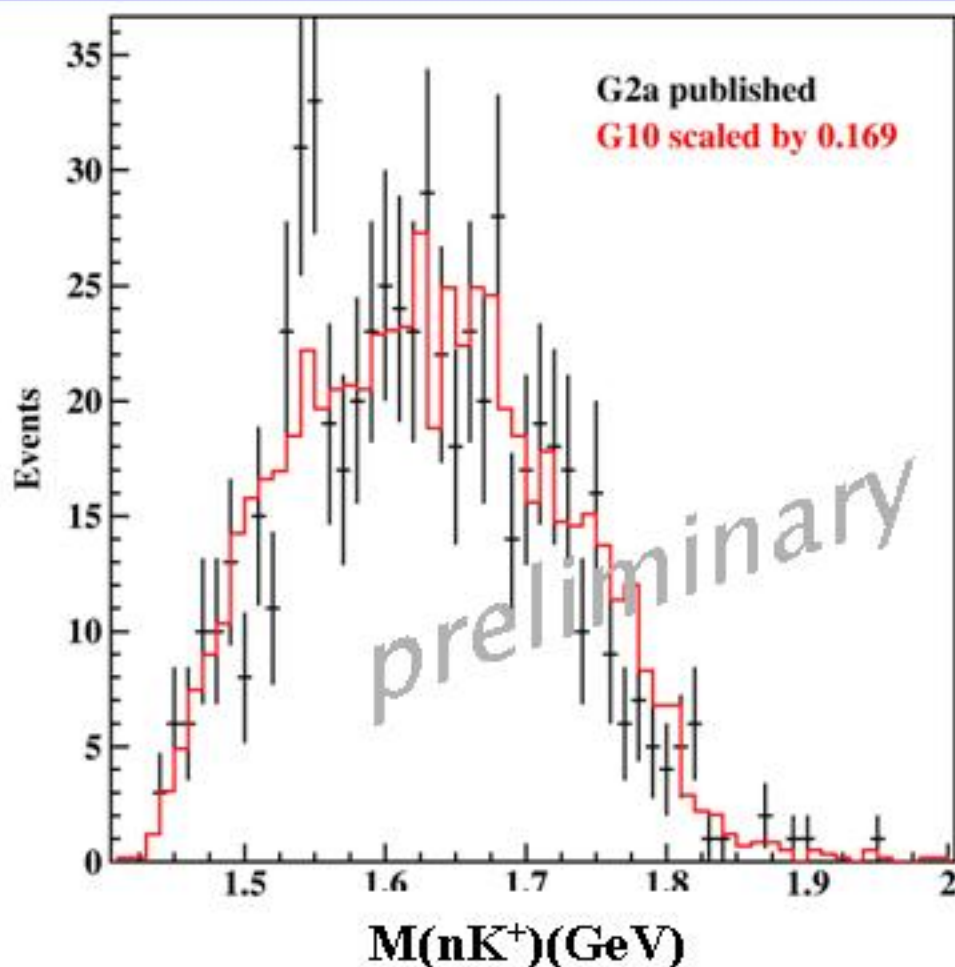
- 30,000 Exabyte tapes.
- Total data comprise ~ 120 terabytes, a volume of data greater than that in the Library of Congress.
- $\sim 230 \times 10^9$ events on tape
- $\sim 2.5 \times 10^9$ Ξ^- and Ξ^+ decays.
- 0.5×10^9 K decays
- 19×10^6 Ω^- and $\bar{\Omega}^+$ decays.
- Beam polarity changed by reversing magnets.
- $\sim 50\%$ of triggers came from titanium and kapton thin windows upstream of decay region, or from nearby material.



Ghost tracks with can produce a peak at 1.54 GeV



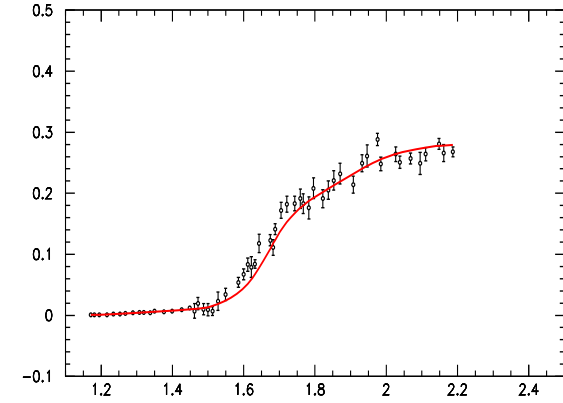
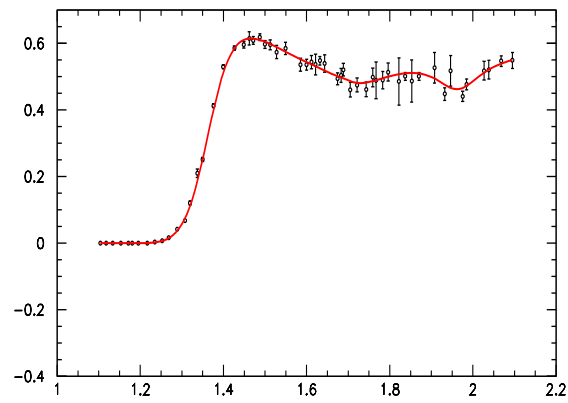
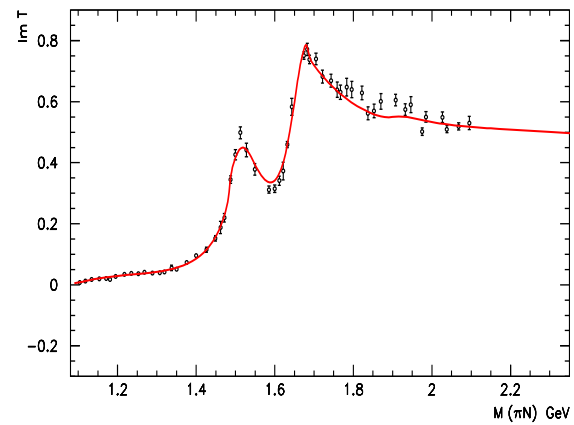
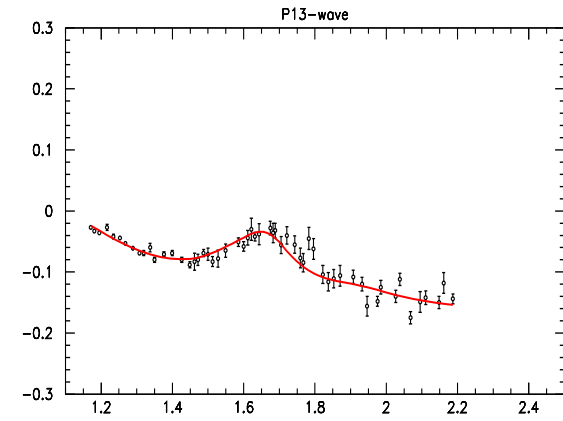
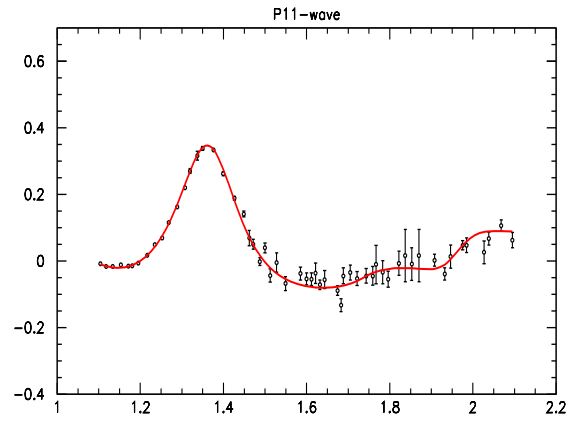
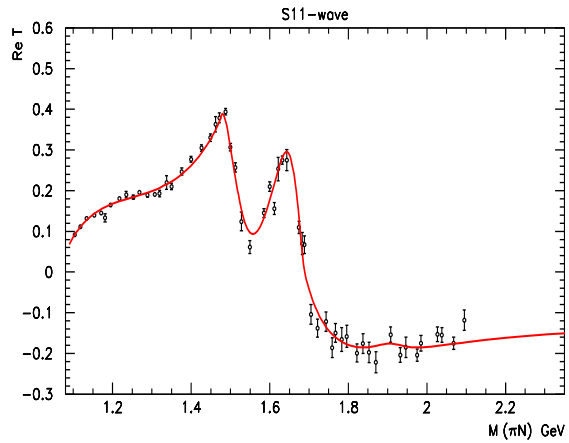
High Statistics CLAS(d) result



- Model-independent upper limit 95% CL for Θ^+ is **< 20nb**.
- With assumptions about the spectator, we can set a model-dependent upper limit to the cross section of **< 4-5 nb**.

$N(1710)$ **and** $N(1680)$

$N\pi \rightarrow N\pi$ S_{11} , P_{11} and P_{13} waves



The πN (KN) interaction.

$$A_{\pi N} = \omega^* [G(s, t) + H(s, t)i(\vec{\sigma}\vec{n})] \omega' \quad \vec{n}_j = \varepsilon_{\mu\nu j} \frac{q_\mu k_\nu}{|\vec{k}||\vec{q}|} .$$

$$G(s, t) = \sum_L [(L+1)F_L^+(s) + LF_L^-(s)] P_L(z) ,$$

$$H(s, t) = \sum_L [F_L^+(s) - F_L^-(s)] P_L'(z) .$$

Differential cross section in c.m.s. of the reaction

$$|A|^2 = \frac{1}{2} \text{Tr} [A_{\pi N}^* A_{\pi N}] = |G(s, t)|^2 + |H(s, t)|^2 (1 - z^2)$$

the recoil asymmetry:

$$P = \frac{\text{Tr} [A_{\pi N}^* \sigma_2 A_{\pi N}]}{2|A|^2 \cos \phi} = \sin \Theta \frac{2 \text{Im} (H^*(s, t) G(s, t))}{|A|^2} .$$

and the rotation parameter.

$$|A|^2 = |G(s, t)|^2 + |H(s, t)|^2(1 - z^2) \quad |A|^2 \frac{P}{\sin \Theta} = 2Im(H^*(s, t)G(s, t)) .$$

$$\underline{S_{1,1}}; \quad G = F_0^+; \quad H = 0; \quad |A|^2 = |F_0^+|^2 \quad (1)$$

$$\underline{P_{1,1}}; \quad G = F_1^- z; \quad H = -F_1^-; \quad |A|^2 = |F_1^-|^2 \quad (2)$$

$$\underline{P_{1,3}}; \quad G = 2F_1^+ z; \quad H = F_1^+; \quad |A|^2 = |F_1^+|^2(3z^2 + 1)$$

Both S_{11} and P_{11} distributions are flat. Recoil asymmetry is zero for single partial wave.

$$\underline{S_{1,1} + P_{1,1}} : \quad P \frac{|A|^2}{\sin \Theta} = -2Im(F_0^+ F_1^{-*}) \quad |A|^2 = |F_0^+|^2 + |F_1^-|^2 + 2zRe(F_0^{+*} F_1^-)$$

$$\underline{S_{1,1} + P_{1,3}} : \quad P \frac{|A|^2}{\sin \Theta} = 2Im(F_0^+ F_1^{+*}) \quad |A|^2 = |F_0^+|^2 + |F_1^+|^2(3z^2 + 1) + 4zRe(F_0^{+*} F_1^+)$$

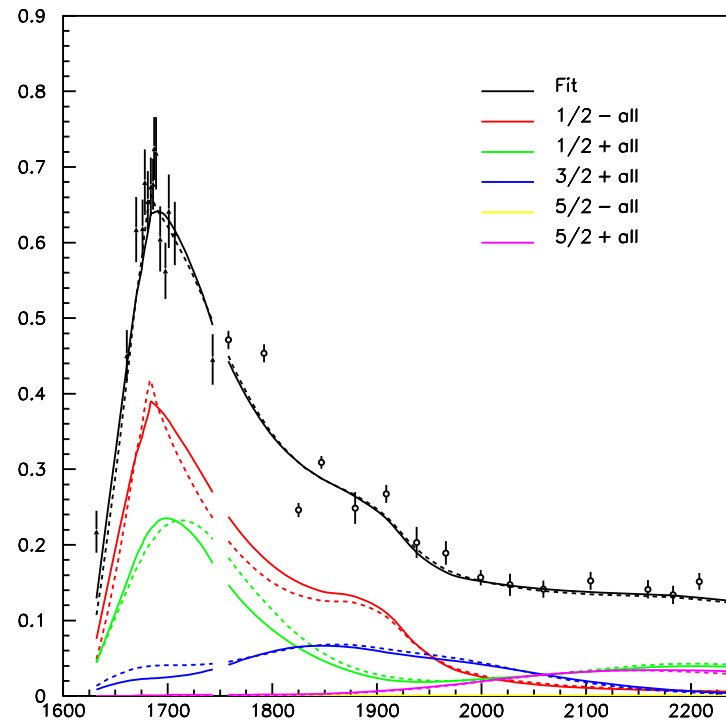
$$\underline{P_{1,1} + P_{1,3}} : \quad P \frac{|A|^2}{\sin \Theta} = 6zIm(F_1^{+*} F_1^-) \quad |A|^2 = |F_1^+ - F_1^-|^2 + z^2 \left(3|F_1^+|^2 - 2Re(F_1^{+*} F_1^-) \right) .$$

S and P-waves can be extracted from the differential cross section and recoil asymmetry. For higher partial waves the rotation parameter is needed.

The fit of the the $\pi^- p \rightarrow K \Lambda$ reaction

Full experiment for $\pi N \rightarrow K \Lambda$:
differential cross section, analyzing
power, rotation parameter.

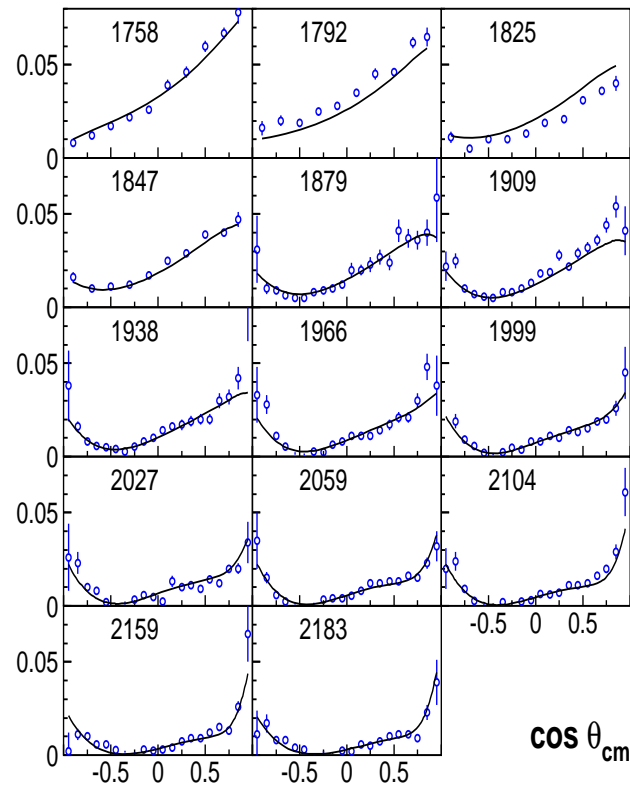
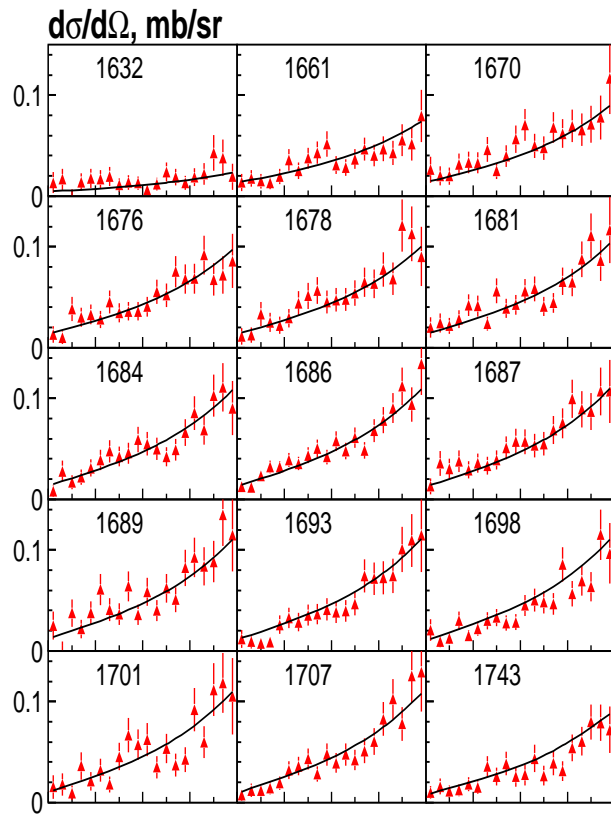
**A clear evidence for resonances which
are hardly seen (or not seen) in
the elastic reactions:** $N(1710)P_{11}$,
 $N(1900)P_{13}$,



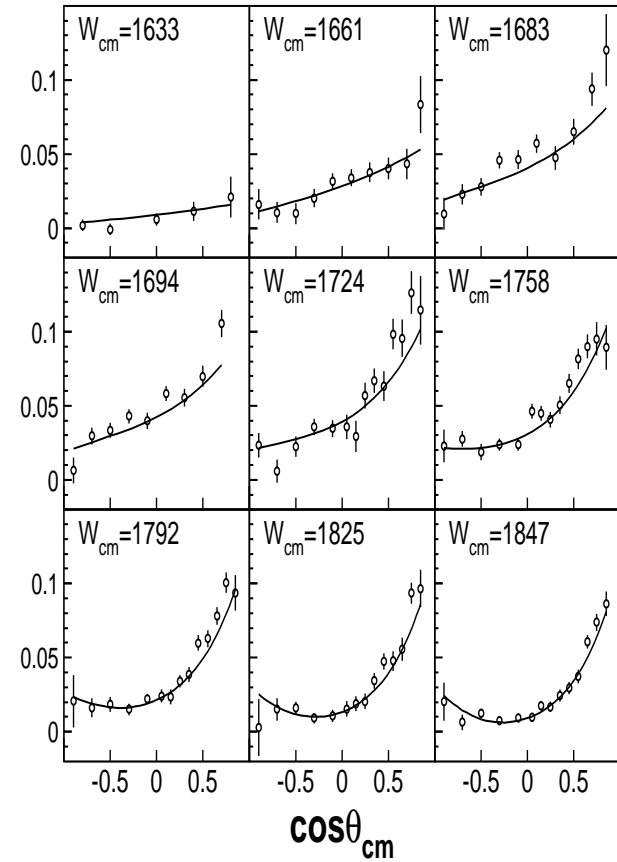
The total cross section for the reaction $\pi^- p \rightarrow K^0 \Lambda$ and contributions from leading
partial waves.

The fit of the $\pi^- p \rightarrow K \Lambda$ reaction

$N(1710) : M = 1690 \pm 15 \text{ MeV}, -2Im = 155 \pm 25 \text{ MeV}$

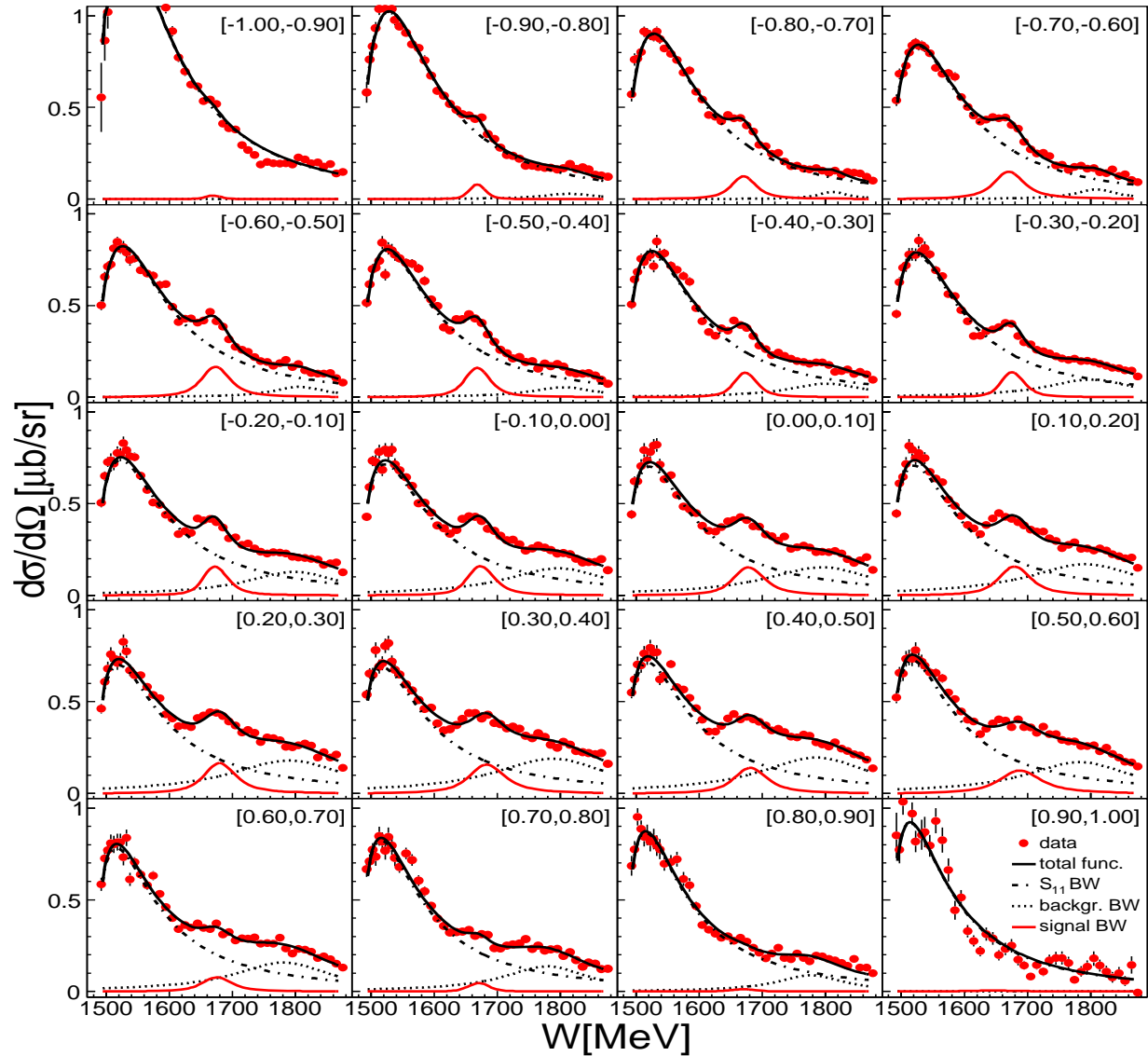
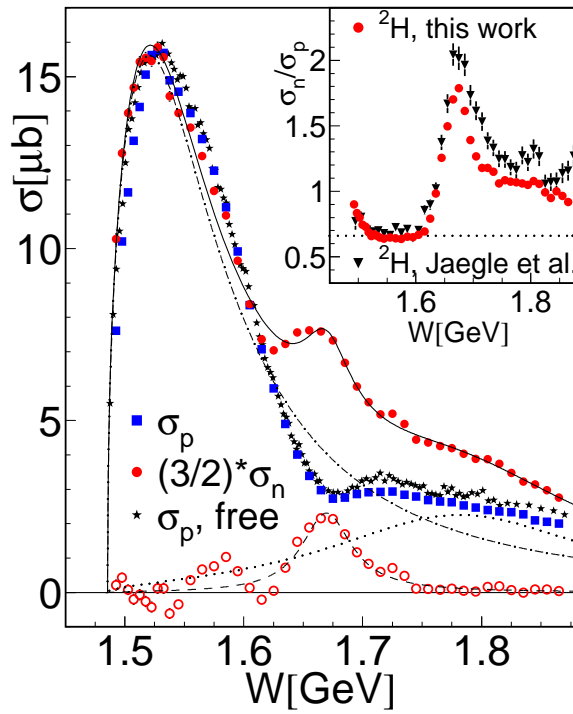


$P d\sigma/d\Omega / \sin\theta, \text{mb/sr}$

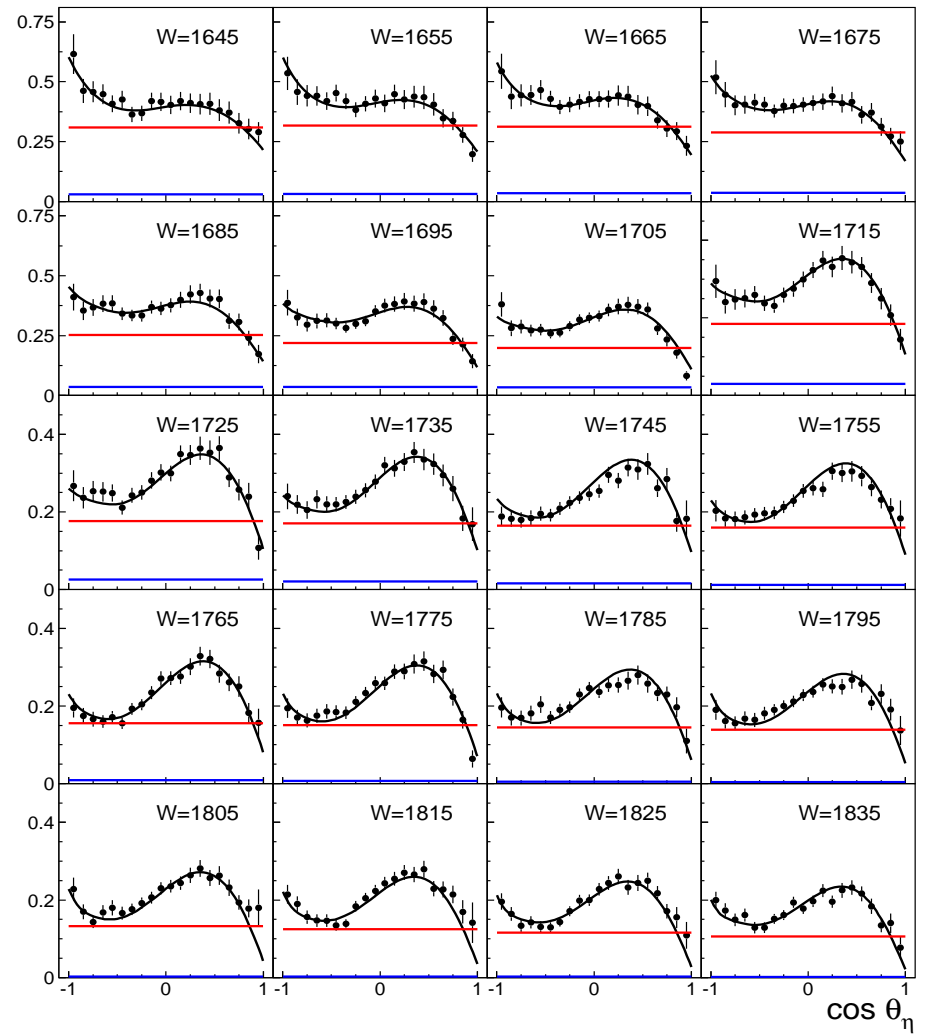
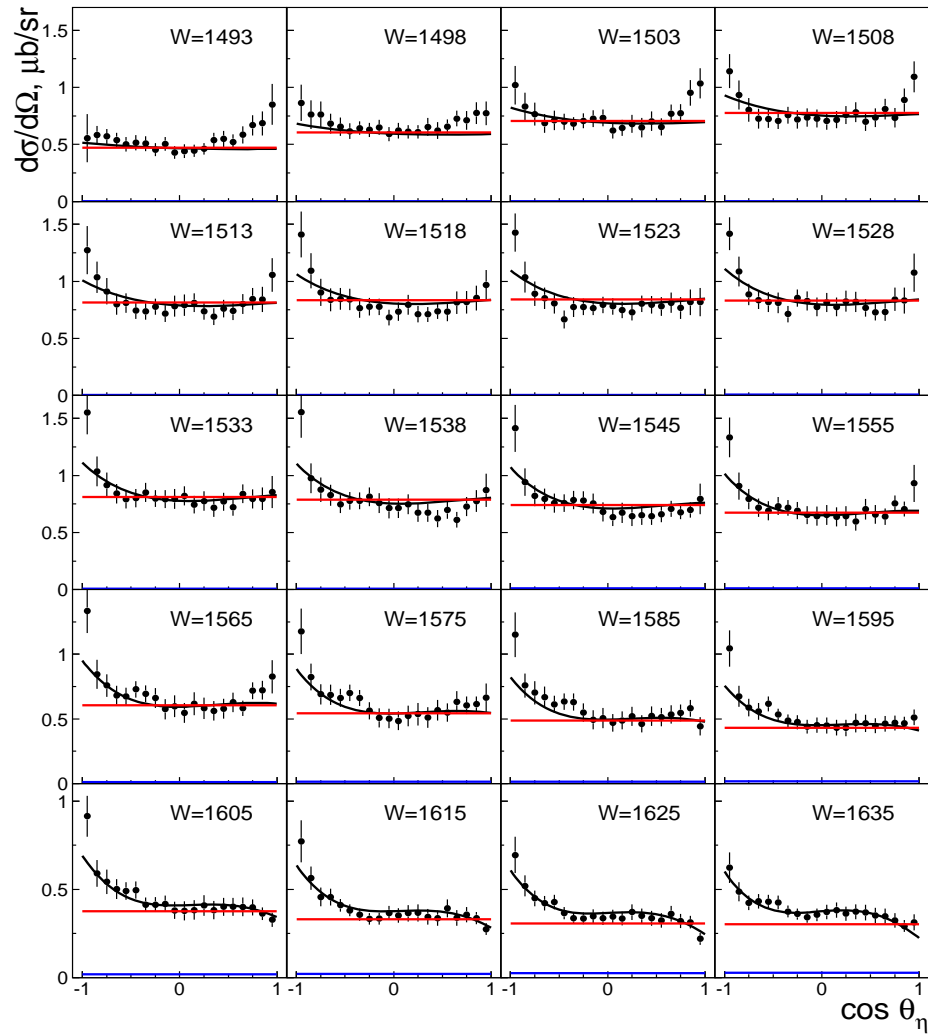


$\gamma p \rightarrow \eta p$ and $\gamma n \rightarrow \eta n$ data

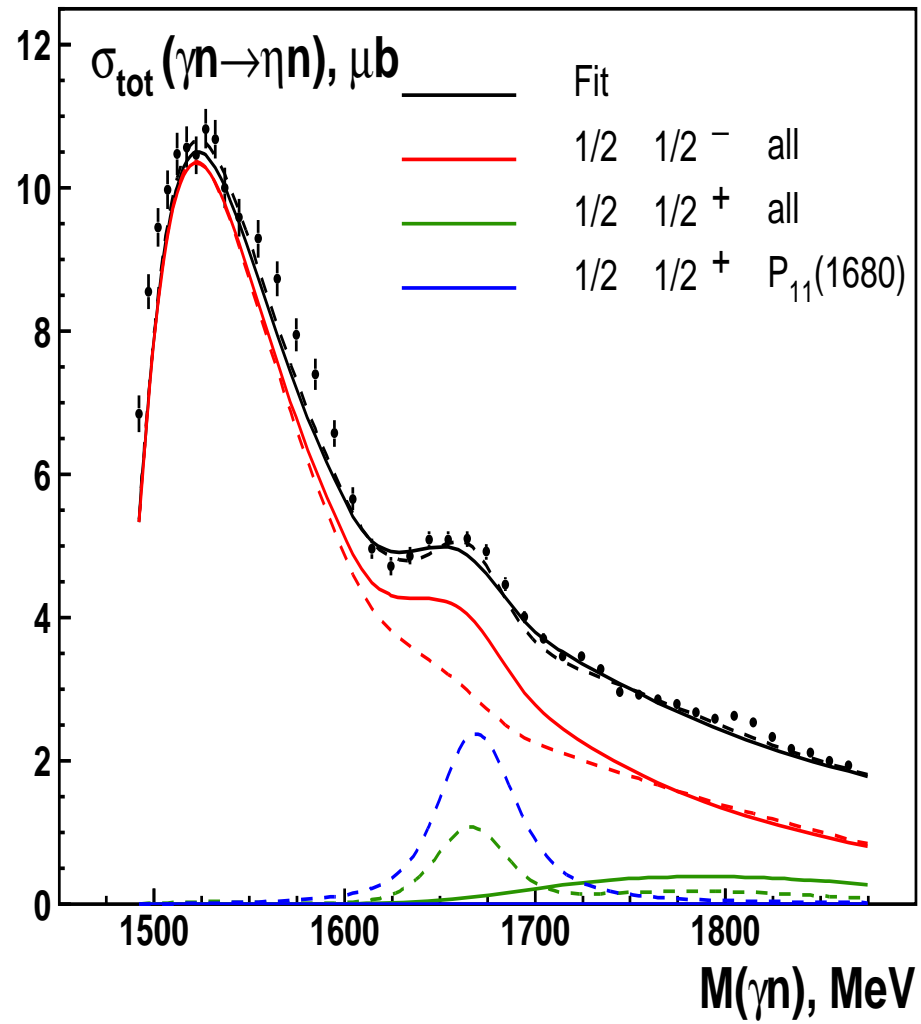
Energy resolution of η : $\Delta W = 10\text{-}42$ MeV ($W = 1500\text{-}1850$ MeV)



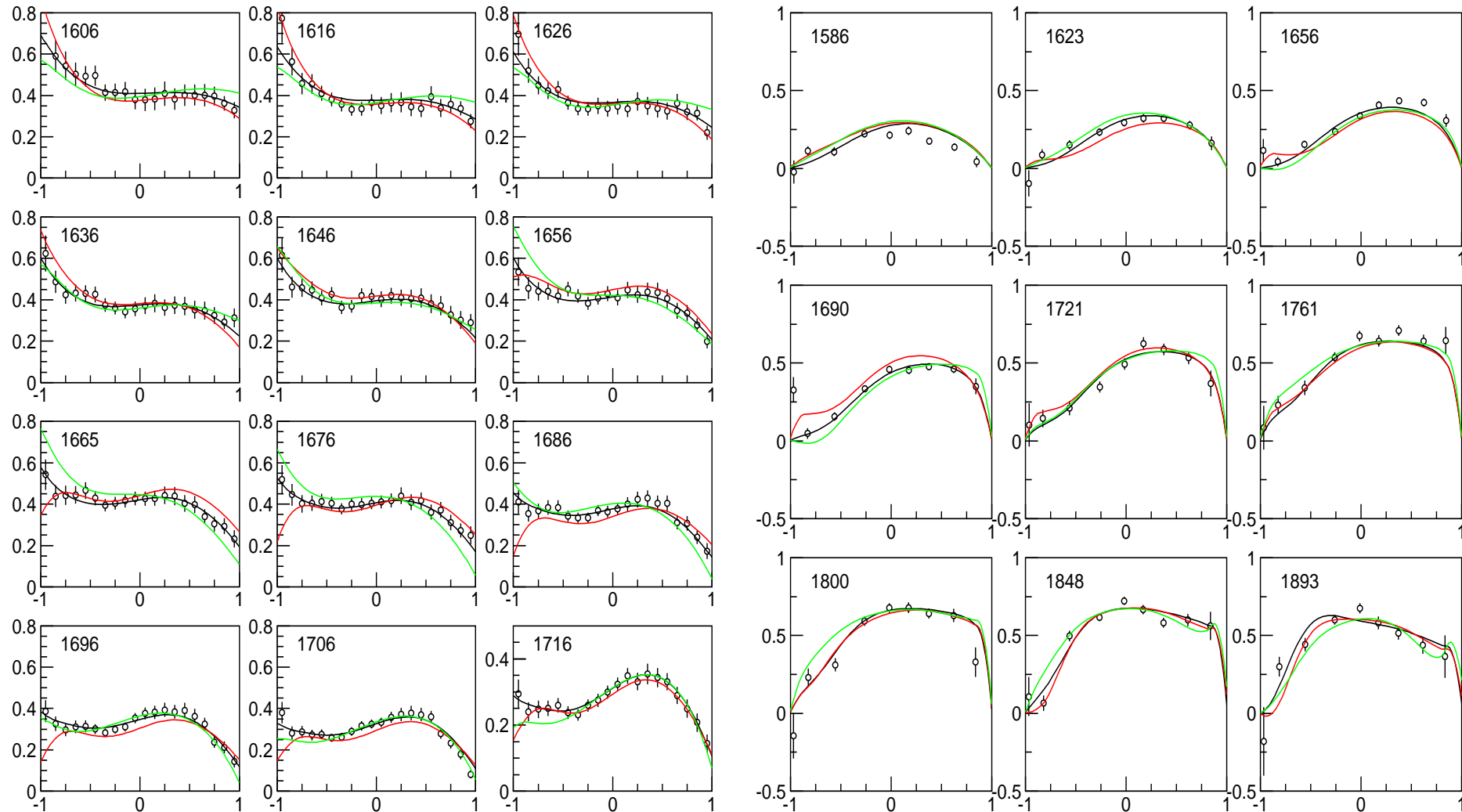
Solution with interference between S_{11} states



Solution with a narrow P_{11} state



The description of the differential cross section and GRAAL data is notably worse



Limit for the production of $P_{11}(1680)$: $|A^{\frac{1}{2}}| Br(\eta\pi) < 5 \text{ GeV}^{-\frac{1}{2}} 10^{-3}$

In c.m.s. of the reaction

$$A = \sum_i u(k_1) V_{\alpha_1 \dots \alpha_n}^{*(i\pm)\mu} F_{\alpha_1 \dots \alpha_n}^{\beta_1 \dots \beta_n} N_{\beta_1 \dots \beta_n}^{(\pm)} u(q_1) \varepsilon_\mu BW_L^\pm(s) = \omega^* J_\mu \varepsilon_\mu \omega' ,$$

$$J_\mu = i\mathcal{F}_1 \sigma_\mu + \mathcal{F}_2(\vec{\sigma}\vec{q}) \frac{\varepsilon_{\mu ij} \sigma_i k_j}{|\vec{k}||\vec{q}|} + i\mathcal{F}_3 \frac{(\vec{\sigma}\vec{k})}{|\vec{k}||\vec{q}|} q_\mu + i\mathcal{F}_4 \frac{(\vec{\sigma}\vec{q})}{q^2} q_\mu .$$

$$\mathcal{F}_1(z) = \sum_{L=0}^{\infty} [LM_L^+ + E_L^+] P'_{L+1}(z) + [(L+1)M_L^- + E_L^-] P'_{L-1}(z) ,$$

$$\mathcal{F}_2(z) = \sum_{L=1}^{\infty} [(L+1)M_L^+ + LM_L^-] P'_L(z) ,$$

$$\mathcal{F}_3(z) = \sum_{L=1}^{\infty} [E_L^+ - M_L^+] P''_{L+1}(z) + [E_L^- + M_L^-] P''_{L-1}(z) ,$$

$$\mathcal{F}_4(z) = \sum_{L=2}^{\infty} [M_L^+ - E_L^+ - M_L^- - E_L^-] P''_L(z) .$$

Differential cross section and polarization observables

$$\mathcal{I}(\theta) = |E_0^+|^2 + |M_1^-|^2 - 2z(\operatorname{Re}E_0^+ \operatorname{Re}M_1^- + \operatorname{Im}E_0^+ \operatorname{Im}M_1^-)$$

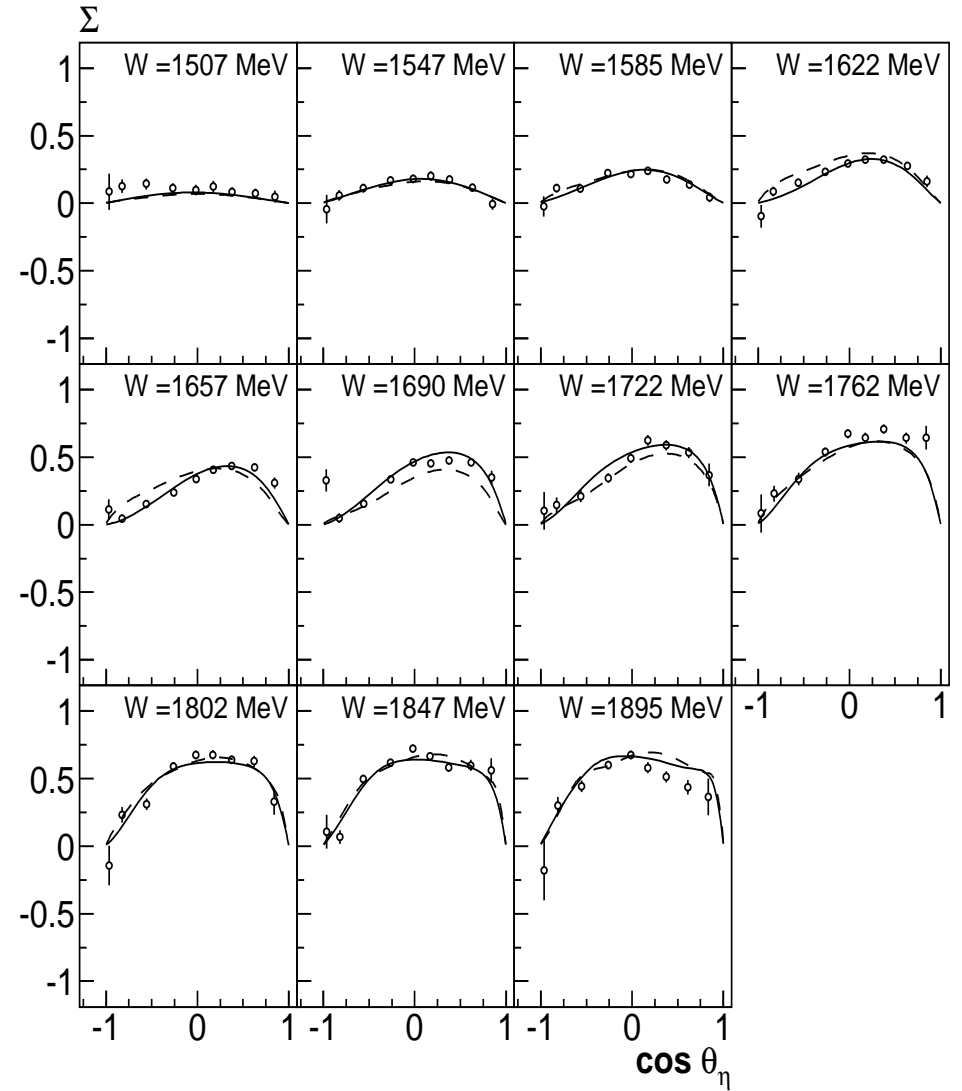
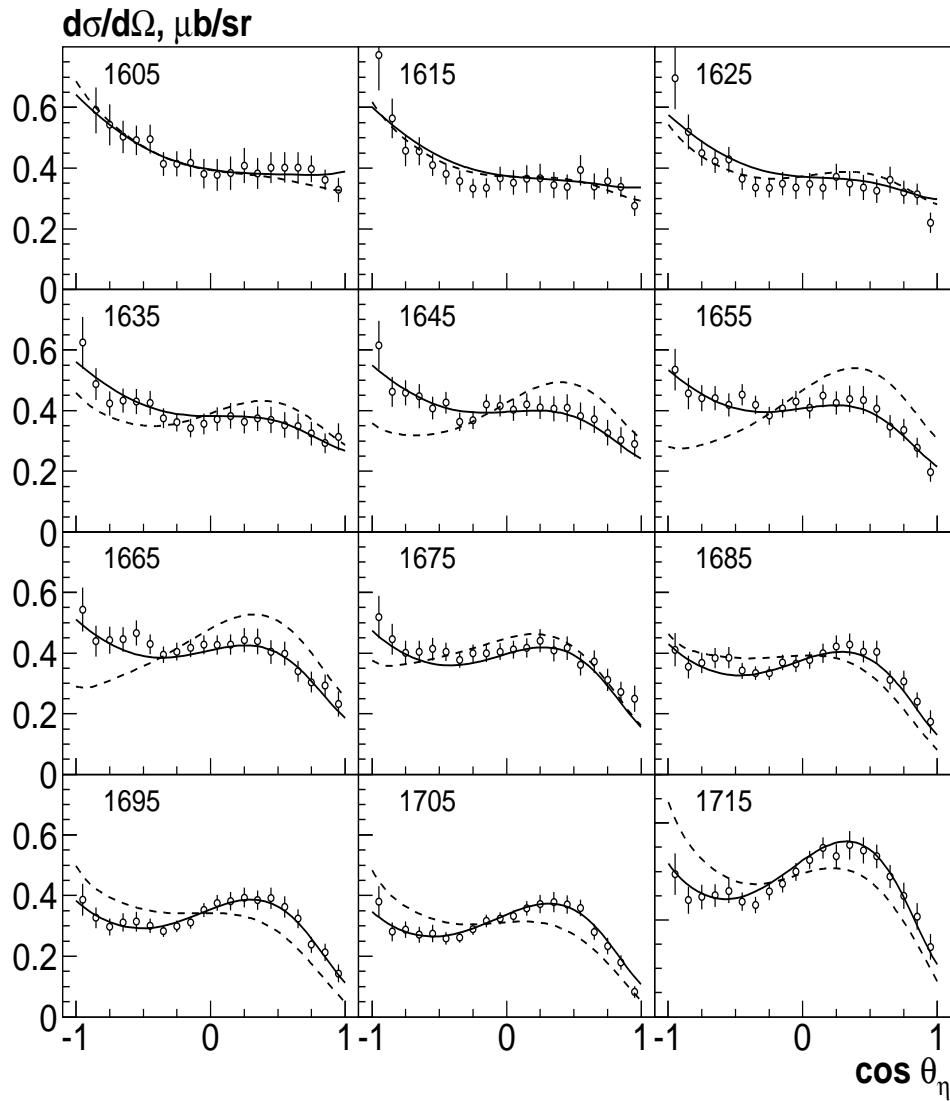
$$\Sigma\mathcal{I}(\theta) = \frac{3 \sin^2 \theta}{2} \operatorname{Re}\{-3|E_1^+|^2 + |M_1^+|^2 - 2M_1^{-*}(E_1^+ - M_1^+) + 2E_1^{+*}M_1^+\}$$

$$T\mathcal{I}(\theta) = 3 \sin \theta \operatorname{Im}\{E_0^{+*}(E_1^+ - M_1^+) - z[M_1^{-*}(E_1^+ - M_1^+) - 4M_1^{+*}E_1^+]\}$$

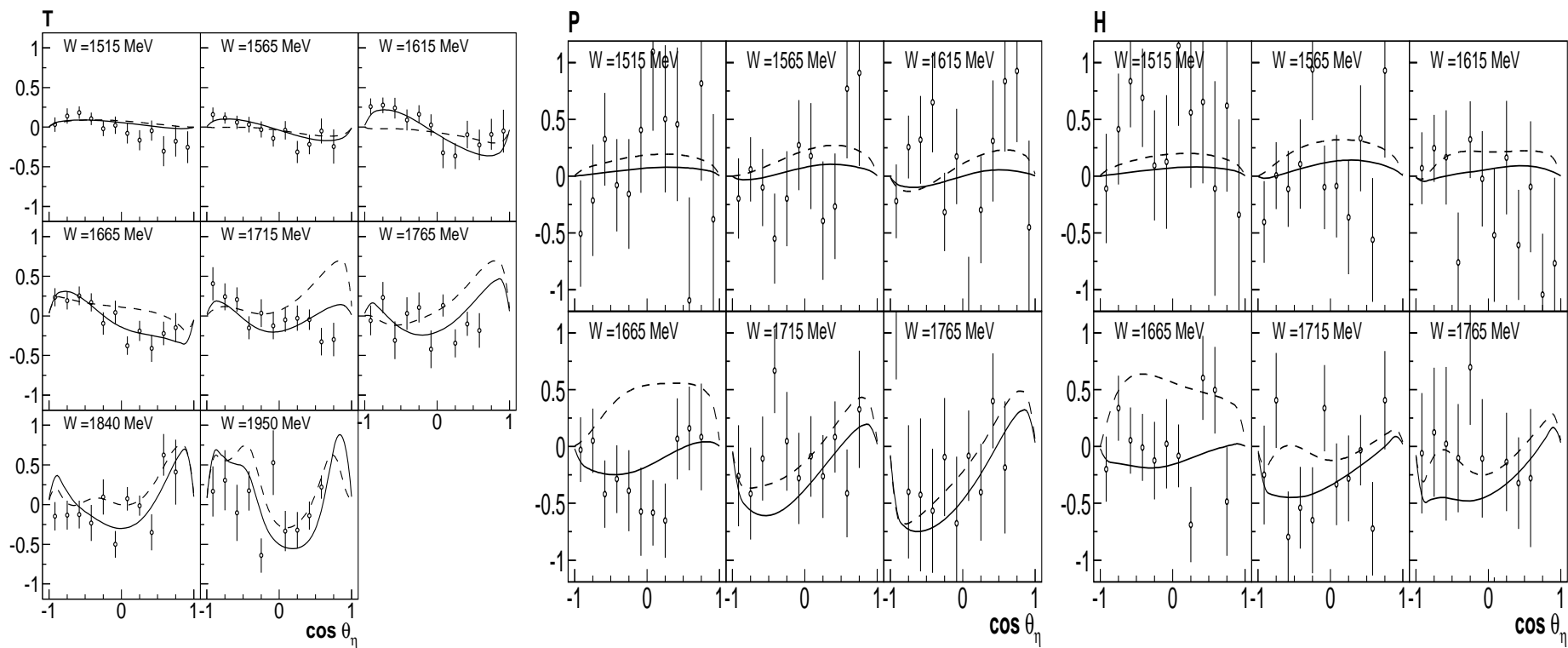
$$P\mathcal{I}(\theta) = -2 \sin \theta \{\operatorname{Re}E_0^+ \operatorname{Im}M_1^- - \operatorname{Im}E_0^+ \operatorname{Re}M_1^-\}$$

$$H\mathcal{I}(\theta) = -2 \sin \theta \{\operatorname{Re}E_0^+ \operatorname{Im}M_1^- - \operatorname{Im}E_0^+ \operatorname{Re}M_1^-\}$$

The description of the differential cross section and beam asymmetry is notably worse



The description of the T, P, H observables



Summary

- The peak in the $\gamma n \rightarrow \eta n$ reaction is defined by the interference inside S-wave
- The K_{Long} beam experiment is the nice tool for the search of the Σ hyperon states
- The pentaquark $\Theta^+(1540)$ state (if it exists) should be a very narrow one, with width $\Gamma < 1$ MeV
- Its partner $N(1680)$ should also be a very narrow. But it is not clear where it should decay
- If we see a signal from $\Theta^+(1540)$ there is a chance to observe its Σ -partner