## Meeting 06/20/23

## Homework from Meeting 06/12/23

1. PDE + Activation around CPS with 2.5 mm beam sigma.
2. Simulations of CPS with 3.5 mm beam sigma.
3. CPS material budget/cost.
4. CPS optimisation.

Next week calculations (request from Hovanes)

1. Simulations of CPS with 1.5 mm beam sigma (background, magnet).
2. Simulations with 1 mm horizontal shift (background, temperature).

## Beam 2.5 mm . PDE and Activation.



## Prompt Dose Equivalent Map (rem/hr) < 500 ; beam $2.5 \mathrm{~mm} ; \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$



Prompt Dose Equivalent (rem/hr) at r=150-180 cm from beam 2.5 mm .

PDE rem/h $\mathrm{N}=11.25 \mathrm{E}+6$ top $1 / 4$-sph. bentcoil-65-m23ref1 91


PDE rem/h $\mathrm{N}=11.25 \mathrm{E}+6$ floor profile bentcoil-65-m23ref1 91


- At beam 2.5 mm PDE meets the specification of the PAC48 proposal: $\mathrm{PDE}<25 \mathrm{rem} / \mathrm{h}$ at floor level $1.5-1.8 \mathrm{~m}$.

Activation $1000+1 \mathrm{hr}$ is below $5 \mathrm{mrem} / \mathrm{hr} . \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$. Beam 2.5 mm .

US+0' $1000+1$ hr [mrem/hr] $\mathrm{N}=36 . \mathrm{E}-5$ bentcoil- $65-\mathrm{m} 23$ ref2 24


Hot spot $1000+1 \mathrm{hr}[m r e m / \mathrm{hr}] \mathrm{N}=36 . \mathrm{E}$-5 bentcoil- 65 -m23ref2 24


Activation $1000+1 \mathrm{hr}[\mathrm{mrem} / \mathrm{hr}] \mathrm{N}=36 . \mathrm{E}-5$ bentcoil-65-m23ref2 24


Rad+1' $1000+1 \mathrm{hr}[\mathrm{mrem} / \mathrm{hr}] \mathrm{N}=36 . \mathrm{E}-5$ bentcoil-65-m23ref2 24


DS $+1^{\prime} 1000+1$ hr [mrem/hr] $\mathrm{N}=36$. E-5 bentcoil- $65-$ m23reff 24


PerMag 1000+1 hr [mrem/hr] $\mathrm{N}=336$. E-5 bentcoil-65-m23ref 24


## Beam 3.5 mm . PDE and Activation.


$\mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n} .}$ Prompt $\mathrm{DE}<25 \mathrm{rem} / \mathrm{h}$ at $\mathrm{r}=150-180 \mathrm{~cm}$ from Beam 3.5 mm .


- At beam 3.5 mm PDE meets the specification of the PAC48 proposal: $\mathrm{PDE}<25 \mathrm{rem} / \mathrm{h}$ at floor level $1.5-1.8 \mathrm{~m}$.

Beam $\sigma=3.5 \mathrm{~mm} . \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$. Activation $1000+1 \mathrm{hr}$ is below $5 \mathrm{mrem} / \mathrm{hr}$.


Activation $1000+1 \mathrm{hr}$ mrem/hr bentcoil-65-m23ref3 24


Max. dP/dV and Coil Lifetime. Beam $3.5 \mathrm{~mm} . \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$.

Hot Spot z-profile bentcoil-65-m23ref3 99


- Maximal dP/dV-2.1 kW/cm ${ }^{3}$
- In Coil the PD<2.E-9 GeV/g/e => Coil LT~300 years of continuous operation.


## Beam 3.5 mm .

## PDE and Activation.

Shield optimization.

PDE (rem $/ \mathrm{hr}$ ) at $\mathrm{r}=150-180 \mathrm{~cm}$ from beam $3.5 \mathrm{~mm} . \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$. Iron core.


- With iron core, beam 3.5 mm , PDE meets the specification of PAC48.
$1000+1 \mathrm{hr}$ Activation DE (mrem/hr) at $\mathrm{r}=150-180 \mathrm{~cm}$ from beam 3.5 mm . $\mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}^{2} \text {. Imesmen }}$. corentre to save lead.


Activation $1000+1$ hr DE top $1 / 2$ sphere bentcoil-65-m23ref4 24




- Activation is below $5 \mathrm{mrem} / \mathrm{hr}$ !



## Beam $3.5 \mathrm{~mm} . \mathrm{B}=0.9 \mathrm{~B}_{\mathrm{n}}$. Max. $\mathrm{dP} / \mathrm{dV}=2.5 \mathrm{~kW}$; Coil Lifetime $=300$ years.





- Prompt dose in DS coil <2.E-9 GeV/g/e.
- Coil LT ~ $\mathbf{3 0 0}$ years.


## Beam 2.5 mm. PDE and Activation. "Stingrey" beam channel. Shield Optimization.

$\mathrm{R}=0.5 \mathrm{~cm}$; may be higher.
$\mathrm{n}_{\mathrm{b}}$ - beam direction
$\boldsymbol{\vartheta}$-pitch angle to the tangent surface $\mathbf{n}$.
$\left(\mathbf{n}_{\mathbf{b}}, \mathbf{n}\right)=\sin (\alpha) \sin (\varphi)=\sin (\vartheta)$
$\alpha$-beam pitch angle to the screen normal.
$\varphi$-angle between n and horiz. axis.

## Comments to the video. What is the wedge effect?

1) Consider e-beam as a cylinder diameter D with uniform density; direction $\mathrm{n}_{\mathrm{b}}=(0, \sin (\alpha), \cos (\alpha))$, where $\alpha$ pitch angle to the beam axis.
2) For a squared or wedge-like channels the hot spot is a cross section of a cylinder with a plane. Plane orientations: $\mathbf{n}_{\mathbf{1}}=(0,1,0)$-for squared channel, or $\mathbf{n}_{\mathbf{2}}=( \pm \cos (\varphi), \sin (\varphi), 0)$ - for 2 wedge planes obtained as $\pm \varphi$ - rotation of yz-plane around z-axis.

Impact angle is determined by $\left(\mathbf{n}_{\mathbf{b}}, \mathbf{n}_{\mathbf{1}}\right)=\sin (\alpha)$ or $\left(\mathbf{n}_{\mathbf{b}}, \mathbf{n}_{\mathbf{2}}\right)=\sin (\alpha) \sin (\varphi)=\sin (\vartheta)$ - pitch to wedge plane.
3) But in both cases the intersection is an ellipse with the area $S=\pi \mathrm{D} \times \mathrm{L}$, where L - ellipse large axis.
4) Pitch angle $\vartheta \sim D / L$.
5) Maximum $L$ is constrained by the length of the beam channel ( $L<L_{c} \sim 2 \mathrm{~m}$ ), or the wedge ( $L<L_{w} \sim 0.5 \mathrm{~m}$ ).

- Therefore $\max \mathrm{dP} / \mathrm{dS} \propto \theta \propto \mathrm{L}^{-1}$ for the wedge is $\mathrm{L}_{\mathrm{c}} / \mathrm{L}_{\mathrm{w}}=4$ times higher.


## $B=B_{n^{\prime}}$ "stingray" chanel $d=1 \mathrm{~cm}$, 4 layers of Lead. More W-shield for DS Coil.



- PDE meets requirement of PAC48 for the floor level.

$1000+1 \mathrm{hr}$ Activation DE (mrem/hr) ; beam $2.5 \mathrm{~mm}, \mathrm{~B}=\mathrm{B}_{\mathrm{n}}$. Iron core. "Stingrey" channel.


PDE mrem/hr bentcoil-65-m23ref6 24



PDE mrem/hr $\mathrm{N}=36 . \mathrm{E}-5$ bentcoil-65-m23ref6 24


PDE mrem/hr bentcoil-65-m23ref6 24


- Activation is below 5 mrem/hr.

Beam $\sigma=2.5 \mathrm{~mm} . \mathrm{B}=\mathrm{B}_{\mathrm{n}^{.}} \mathrm{dP} / \mathrm{dV}<1.2 \mathrm{~kW}$; Coil Lifetime $\sim 300$ years.
Ds Coil $\mathrm{GeV} / \mathrm{g} / \mathrm{e}>2$.E-8 bentcoil-65-m23ref6 97



Ds Coil $\mathrm{GeV} / \mathrm{g} / \mathrm{e}>2 . \mathrm{E}-8$ bentcoil-65-m23ref6 97


## CPS Weight and Cost estimates.

| 1 | Pb Skin | $\mathrm{g} / \mathrm{cm} 3$ | z | dZ | R | Xint | $\times$-fct | V/cm3 | P/T | P/T | Cost |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | ski5 z.dz.r | 11.4 | 40 | 220 | 99 | 88.7 | 0.65 | $7.60 \mathrm{E}+5$ | 8.7 |  |  |  |
| 3 | ski1 | 11.4 | 15 | 290 | 90 | 78.6 | 0.66 | 1.03E+6 | 11.7 |  |  |  |
| 4 | ski2 | 11.4 | -6 | 351 | 80 | 66.5 | 0.69 | 1.13E+6 | 12.9 |  |  |  |
| 5 | ski3 | 11.4 | -30 | 415 | 70 | 54 | 0.72 | 1.22E+6 | 13.9 |  |  |  |
| 6 | ski4 | 11.4 | -56.5 | 476.5 | 60 | 40.5 | 0.76 | $4.11 E+6$ | -37.0 |  |  |  |
| 7 | V_tot |  |  |  | 0 |  |  | $8.25 E+6$ | 10.2 | 10.2 | \$50,996 |  |
| 8 | V_filled |  | g/cm3 $=$ | 11.4 | /kg $=$ | 5 |  | 8.95E+5 | 10.2 |  |  |  |
| 9 | B+Polyethyl. |  | z | dZ | R | Xint | X-fct |  |  |  |  |  |
| 10 | bor5 | 1.2 | 45 | 211 | 94 | 82.4 | 0.66 | 7.01E+5 | 0.8 |  |  |  |
| 11 | bor1 | 1.2 | 20 | 280 | 85 | 72.4 | 0.67 | $9.48 \mathrm{E}+5$ | 1.1 |  |  |  |
| 12 | bor2 | 1.2 | -1 | 341 | 75 | 61 | 0.70 | $1.05 \mathrm{E}+6$ | 1.3 |  |  |  |
| 13 | bor3 | 1.2 | -25 | 405 | 65 | 47 | 0.74 | 1.13E+6 | 1.4 |  |  |  |
| 14 | bor4 | 1.2 | -51 | 467 | 55 | 33 | 0.80 | $3.53 E+6$ | -2.2 |  |  |  |
| 15 | V_tot |  |  |  | 0 |  |  | $7.36 \mathrm{E}+6$ | 2.4 | 2.4 | \$47,278 |  |
| 16 | V_filled |  | g/cm3 $=$ | 1.2 | /kg= | 20 |  | 1.97E+6 | 2.4 |  |  |  |
| 17 | Lead Shield |  | z | dZ | R | Xint | X-fct |  |  |  |  |  |
| 18 | les19 | 11.4 | 55 | 190 | 80 | 66.6 | 0.69 | $6.14 E+5$ | 7.0 |  |  |  |
| 19 | les16 | 11.4 | 30 | 260 | 70 | 54 | 0.72 | 7.62E+5 | 8.7 |  |  |  |
| 20 | les15 | 11.4 | 10 | 320 | 60 | 41 | 0.76 | $8.42 \mathrm{E}+5$ | 9.6 |  |  |  |
| 21 | les14 | 11.4 | -15 | 385 | 50 | 24 | 0.84 | $9.16 \mathrm{E}+5$ | 10.4 |  |  |  |
| 22 | les13 | 7.8 | -41 | 448 | 40 | 0 | 1.00 | $2.25 E+6$ | 3.4 |  |  |  |
| 23 | V_tot |  |  |  |  |  |  | $5.39 \mathrm{E}+6$ | 39.2 | 39.2 | \$195,838 | 49 |
| 24 | V_filled |  | g/cm3 $=$ | 11.4 | /kg= | 5 |  | $3.58 \mathrm{E}+6$ | 40.8 |  |  |  |
| 25 | Iron Core |  | z | Z | dy | dx |  |  |  |  |  |  |
| 26 | Void $\mathrm{z}, \mathrm{Z}, \mathrm{x}, \mathrm{y}$ |  | -56.5 | 430 | 62 | 60 |  | $1.81 E+6$ |  |  |  |  |
| 27 | V_tot |  |  |  |  |  |  | $1.81 E+6$ |  |  |  |  |
| 28 | V_filled |  | g/cm3 $=$ | 7.87 | /kg= | 4 |  | 1.48E+6 | 11.7 | 11.7 | \$46,680 |  |
| 29 | Cu Absorber |  | -56.5 | 430 | 48 | 14 |  | $3.27 E+5$ |  |  |  |  |
| 30 | V_tot |  |  |  |  |  |  | $3.27 E+5$ |  |  |  |  |
| 31 | V_filled |  | g/cm3 $=$ | 8.96 | /kg= | 20 |  | $3.27 E+5$ | 2.9 | 2.9 | \$58,585 |  |
| 32 | Pedestal Con. |  | -40 | 420 | 126 | 100 |  | $5.80 E+6$ |  |  |  |  |
| 33 | V_tot |  |  |  |  |  |  | $5.80 E+6$ |  |  |  |  |
| 34 | V_filled | 2.3 | g/cm3 $=$ | 2.3 | /kg= | 3 |  | $5.80 E+6$ | 13.3 | 13.3 | \$39,992 |  |
| 35 | Platform Fe |  | -56.5 | 430 | 10 | 200 |  | $9.73 E+5$ |  |  |  |  |
| 36 | V_tot |  |  |  |  |  |  | $9.73 E+5$ |  |  |  |  |
| 37 | V_filled |  | g/cm3 $=$ | 7.87 | / $\mathrm{kg}=$ | 4 |  | $9.73 E+5$ | 7.7 | 7.7 | \$30,630 |  |
| 41 |  |  |  |  |  |  |  |  | All | 87.3 | \$470,001 |  |
| 42 |  |  |  |  |  |  |  |  | -Pdst | 74.0 | \$430,008 |  |
| 43 |  |  |  |  |  |  |  |  | -Pltf | 66.3 | \$399,378 |  |




| CPS Mat. | Ton | $\mathrm{g} / \mathrm{cm} 3$ | $\$ / \mathrm{kg}$ |
| :--- | :--- | :--- | :--- |
| Lead | 49 | 11.3 | 5 |
| B+PE | 2.4 | 1.2 | 20 |
| Iron | 12 | 7.8 | 4 |
| Copper | 2.9 | 8.9 | $20(100, \mathrm{Tim}) ?$ |
| Total CPS | 66 | - | $(+\$ 240,000)$ |

## CPS critical sizes and shield optimization.



Consider a source of radiation (red line) and a shield around it (cylinder R,L). Stationary case.
Total power P of red line relates to $\mathrm{dP} / \mathrm{ds}$ at the cylinder surface as

$$
\mathrm{P}=2 \pi \mathrm{RL}(\mathrm{dP} / \mathrm{ds})
$$

Assume $\mathrm{dP} / \mathrm{ds}=\varrho$ is constrained by RadCon regulations to be constant at varying sizes.

$$
=>\text { for the SPS radius we write } \quad R=(P / \varrho)(2 \pi L)^{-1}
$$

For the CPS cyl. volume we write:

$$
\mathbf{V}=\pi(2 \pi)^{-2} \mathbf{L}^{-1}(\mathbf{P} / \varrho)^{2}
$$

For a spherical case

$$
\mathrm{V}=(4 \pi / 3)(4 \pi)^{-3 / 2}(\mathrm{P} / \varrho)^{3 / 2}
$$

And we find that for constrained $\mathrm{dP} / \mathrm{ds}=\varrho$ at CPS surface
CPS volume
Temperature
Magnet power
Max. power dep.
$\mathrm{V} \propto \mathrm{L}^{-1}$
$\mathrm{T}^{0} \propto \mathrm{~L}^{-1}$ (from the previous presentations)
$B \propto L^{-1}$

- Thus, further increasing CPS length L we may save on volume, weight, and magnet cost.
- Electron beam current is limited by Absorber temperature.
- Photon beam intensity may be significantly higher.

If copper cost is $\$ 100 / \mathrm{kg}$ we may replace Cu with Fe or Pb in some locations


Shield optimization requires FLUKA and Temperature calculations.

## FLUKA Absorbed Dose (rad/Gy) and Dose Equivalent (rem/Sv).

## Equivalent Dose definition.

Calculating equivalent dose from absorbed dose;

$$
H_{T}=\sum_{R} W_{R} \cdot D_{T, R}
$$

where
$H_{T}$ is the equivalent dose in sieverts (Sv) absorbed by tissue T ,
$D_{T, R}$ is the absorbed dose in grays (Gy) in tissue $T$ by radiation type R and $W_{R}$ is the radiation weighting factor defined by regulation.

- Does FLUKA follow standard rules?


## Absorbed dose includes neutrons.

Radiation weighting factors $\mathrm{W}_{\mathrm{R}}$ (formerly termed Q factor) used to represent relative biological effectiveness according to ICRP report 103 ${ }^{[6]}$

| Radiation | Energy | $\mathbf{W}_{\mathbf{R}}$ (formerly Q) |
| :--- | :--- | :--- |
| x-rays, gamma rays, <br> beta particles, muons |  | 1 |
| neutrons | $<1 \mathrm{MeV}$ | $2.5+18.2 \cdot \mathrm{e}^{-[\ln (E)]^{2 / 6}}$ |
|  | $1 \ldots .50 \mathrm{MeV}$ | $5.0+17.0 \cdot \mathrm{e}^{-[\ln (2 \cdot \mathrm{E})]^{2 / 6}}$ |
|  | $>50 \mathrm{MeV}$ | $2.5+3.25 \cdot \mathrm{e}^{-[\ln (0.04 \cdot E)]^{2 / 6}}$ |
| protons, charged pions |  | 2 |
| alpha particles, fission <br> products, heavy nuclei |  | 20 |

