

Hall D K-Long Facility E12-19-001. Experiment Readiness Review Phase I. Jefferson Lab , 2023 Charge and Brief Answers.

- Is there any R&D needed to be done prior to start the construction of the KLong Facility? **No.**
- What is the status of the Compact Photon Source (CPS)?
- 1. Conceptual design:
- 2. **Approximations** in the MC simulations and Code used:
- 3. Evaluation of the **produced radiation**:
- 4. Energy deposition , **Absorber** and **Lead temperature**:
- 5. Prompt **dose** and **activation** around the CPS (Tagger Hall):
- 6. Magnet and insulation lifetime:
- 7. Cooling system & ground waters contaminations:
- What will the photon **beam quality** be:
- **Cost and schedule estimates** for the construction of the CPS:
- **Civil constructions** to contain the radiation in the Tagger Hall:
- **Decommissioning Plan** for CPS and Activated Components:

Specifically the Presented below. Simplified Tagger & KPT Halls. FLUKA2021.2.9. 12 GeV beam 3.1E+13 e/s, (5μA), FWHM=**2.5 mm**, < **1 mrem/hr** on top of Tagger Hall and Tunnel Mounds. $<2 \text{ kW/cm}^3$, Cu Absorber $< 220^{\circ}\text{C}$, Pb shield $< 110^{\circ}\text{C}$. Dose < 10 rad/hr, <20 mrem/hr. Maps available. 0.25×0.5 Tm, I ≤ 1.8 kA, wire 2×2 cm², T $< 150^{\circ}$ C, LT=15 years. Tritium Activity **2.6*10⁷ Bq** & **200 Bq/L** after 1 year. \sim **2.E+13** γ /s, FWHM=4 cm, neutrons & ± part<**2%**. **\$800,000** without magnet.

No.

To be mounted on rails to **move aside** for storage.

Compact Photon Source and K_L Beam for Hall D.





Compact Photon Source for KLF beamline. Conceptual design and Simulations using FLUKA 2021.2.9.

(Electron beam 12 GeV, 5 μ A (3.1×10⁺¹³ s⁻¹), FWHM=2.5 mm.)

V. Baturin , for KLF Collaboration.

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Outline

- 1. CPS in FLUKA. Location, Design, and Alignment.
- 2. Radiation and Temperature inside CPS.
- 3. Photon **Beam Quality**.
- 4. Radiation in CPS Magnet and Lifetime of Coil Insulation.
- 5. Prompt **Dose and Activation** around CPS.
- 6. Tritium **Contamination** in Soil and Cooling Waters.
- 7. Lifetime of construction materials.
- 8. Conclusion and Outlook.

CPS Conceptual Design and Simulations using FLUKA 2021.2.9 Model approximations.

CPS location in Tagger Hall. Beam 5 μ A, Gaussian, FWHM=2.5 mm.



CPS, Tagger Hall, KPT and Magnet Prototype in FLUKA model.



CPS in FLUKA: Magnet Yoke/platform, Two Coils, Cu Absorber, and 4 shield layers.



Source of radiation. Hot spot in the absorber. Power deposition



- Upstream magnet forms the Hot Spot; Downstream cleans the photon beam.
- The **wider is** the Hot Spot **the lower** is deposited power/temperature in the maximum.

Magnetic Field, Beam Channel, and Hot Spot Size.



R-**trajectory** radius , $R \propto B^{-1}$. z -counts from **L/2** - **coil area** length, where B>0. z'-counts from z=0. L_M - length of **Beam Channel and Absorber**.

 $\langle z' \rangle = L_M/2$ is constrained to be in the middle of Channel.

From two triangles on this figure we find:

$$\begin{split} (R-s)^2+L^2=R^2, &=> \quad s\approx \frac{L^2}{2R}\,,\\ &\frac{L}{R-y}=\frac{y-s}{z},\\ z\approx \frac{R}{L}(y-s)=\frac{R}{L}y-\frac{L}{2},\\ &\approx < y>\frac{R}{L}\,,\\ \mathrm{rms}(z')\approx \mathrm{rms}(y)\frac{R}{L}=< z'>\frac{\mathrm{rms}(y)}{< y>}\,. \end{split}$$

- At given rms(y) and channel length L_M for a lower power deposition and temperature reduce channel diameter.
- However, keep $d > d_{min} = \sim 2 \text{ rms(y)}$, otherwise beam tail hits the Channel.

CPS Absorber and Alignment.

Segmented Copper Absorber - possible solution.



- Segments $\sim 4.4 \times 20 \times 50$ cm³, round beam hole. => Edvantage compared square holes.
- (1) No problem of **thermal contact** between 2 parts (if squared hole) and (2) may be **vacuumized**.
- Segments are connected by fittings with **left/right-**hand threads; may be **brazed**.
- Provides direct **copper-water contact** inside segments: => no interface; **better cooling**.



Magnet Yoke as Precise Platform for Absorber



- 1. **Iron shield** and **precision <u>platform</u>** for Absorber. Specified **flatness** within **500** μ m.
- 2. <u>Housing</u> for all parts with narrow beam channels, including protruded segments.
- 3. **Precision Assembling** at a bench and **in-hall <u>Alignment</u> with 5 DOF** only.

Energy deposition and Temperature of CPS components.

Borned hippedare

Power Deposition in -0.5<x/cm<0.5 layer. Coarse mesh 0.5 cm.



• Protruding **copper segment** around Radiator to mitigate lead overheating.

• T^o-calculations **in progress**. Channel widening in coil area - to **reduce dose** rates.

• [baturin@hallal1 PEDFASTGUN4]\$ ls -lt *.inp | grep or

-rw-r--r - 1 baturin clas 49936 Feb 9 11:07 CPSKPTLEAD1712narrGUNvacTRP_org.inp

Power breakdown between CPS components.

lacksquare

CPS part	$\mathrm{GeV/e}$	kW/5 μA
DS Shield (W)	0.063	0.316
US Shield (W)	0.033	0.163
Side Shield (W)	0.013	0.064
Top Water Pipe	0.001	0.005
Bottom Pipe	0.001	0.006
Magnet Pole Right	0.322	1.610
Magnet Pole Left	0.321	1.619
Coils	0.058	0.289
Magnet Yoke	0.101	0.504
Lead Shield	0.006	0.032
Polyethylene (B)	0.002	0.011
Lead Skin	0.001	0.004
Converter (Cu)	0.002	0.010
Total	0.923	4.620

Segment	$\mathrm{GeV/e}$	kW/5 μA
$1 \mathrm{W/Cu}$	0.230	1.151
2	2.013	10.077
3	4.743	23.744
4	2.034	10.183
5	0.385	1.929
$6 \mathrm{W/Cu}$	0.164	0.822
Radiator	0.002	0.010
Total	9.571	47.916

Total deposition 53 kW out of 60 kW of e-beam.

B: Steady-State Thermal Temperature Type: Temperature Unit: *C Time: 1 s 3/2/2023 8:03 AM

> 210.54 Max 196.2

181.85 167.51 153.17



Temperature field in the entire CPS at thermal contact between Shield Layers via 100 micron Air.



- Copper $T < 210^{\circ}$ C ($T_m = 1084^{\circ}$ C). Absorber Channel does not melt.
- Lead $T < 110^{\circ}$ C. ($T_m = 327^{\circ}$ C). Lead Shield does not melt.
- Iron $T < 150^{\circ}$ C. ($T_m = 1538^{\circ}$ C). $T < 150^{\circ}$ C. Cooling not required.

Power Deposition in Hot Segment. Fine mesh 0.05 cm



Calculation by Tim Whitlatch Temperature field in the Hot Segment at Heat Transfer Coefficient 9 kW/m²C.



Photon Beam Quality at KPT

Particles exiting from the CPS . Angular profile.



- Photon beam at the CPS exit **looks very clean** (< 1.E-3). Left plot.
- What happens to the beam **after 67 m of beam line?** Right plot.

Beam quality at KPT.



- After 67 m of beam line the total background of charged particles and neutrons is of 2. %.
- Be target acceptance r=2.5 cm; => **80%** of photon beam hits the Be target of KPT.
- Photon beam **intensity at KPT entry** ~ **2.8 E+13 photons/s.**

Energy deposition in KPT. Effect of photon beam.



• T^o-field is **calculated** using this map and **cooling** system **designed** by T. Whitlatch.

K_L from KPT and on H_2 -target of GlueX detector.



- K_L beam **intensity** on H₂-target ($\Delta \Omega = 1.3E-3$ sr) is not a primary goal.
- From the right plot we may estimate it on H_2 target: $dK_L/dt \sim 10^4$ Hz.
- Agrees with the KLF proposal.

Radiation in CPS Magnet

and

Coil insulation lifetime.

For a closed shielding can :S = 4/3 μ t/D where μ - the permeability (relative) t : material thickness D : Shielding Diameter.

For a long hollow cylinder in a magnetic transverse field : $S = \mu t/D$.

For a cubic shielding box : $S = 4/5 \mu t/a$; a - box side length.

Coil Design and Insulation Exposure to Radiation.



- Attractive force of bent parts $F = 25 \text{ N/m}^* 0.3 \text{ m} = 7.5 \text{ N}.$
- Copper 1.7 cm -wires (tubes) will not touch. Attractive deformation ~ 12 microns only!



Prompt Dose in Coils and Insulation Lifetime (straight part).



- **Dose 2.E-8 GeV/g/e** \times 1.6E-10 J/Gev=3.2E-18 Jg⁻¹e⁻¹=3.2E-15 Gy/e;
- **Translates** to 3.2E-15 [Gy/e]×3.E+13 [e/s] \approx **0.1 [Gy/s]**.
- **Fiberglass** cloth withstands **50** MGy => Lifetime =5.E+8 s = 15 years.
- Bent part dose rate is ~ 10 times higher.

Benefit of wider magnet (+14 cm).



- Dose rate in critical points **0.1 Gy/s** (**2.E-8 GeV/g/e**).
- For 14 cm wider Magnet Insulation Lifetime in Coil return area is of **15 years.**

Tim Whitlatch's solution.



Prompt Dose (equipment) and Activation (human) around CPS

Prompt Dose Rate around CPS < 10 rad/hr. Effect of Tail shield.



Activation After 1000+1 hr < 20 mrem/hr.



Prompt Dose Equivalent on top of Tagger hall and Beam Channel.



1.4<fi<1.7

1550< z/cm <6500

50 < r/cm <771 r/cm

Prompt Dose Equivalent and Activation in KPT Alcove.



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Prompt Dose Equivalent

• Dose rates meet JLab radiation safety requirements.

Tritium activity in Soil and Cooling Water

Tritium detector in FLUKA model



Neutron fluence and Tritium in ground waters ($V=2.4 \text{ m}^3$).



³H yield per year $\mathbf{N}=_{1.E-7 [T/e] 3.E+13 [e/s]3.14E+7[s]}=\mathbf{1.E+14}$. Activity of soil volume after one year:= - dN/dt=1.E+14 / (12*3.14E+7 s) = **2.6E+4 Bq** Or ~200 Bq/L in water (~20% by volume in soil).

• Tritium activity in ground water is 3% of VA drink water limit 7000 Bq/L.



Tritium in water of cooling pipes.



We read the yield of ³H in the cooling water: **1.E-5** [**T**/**e**] Number of T nuclei produced in one year: = N_T =1.E-5 [T/e] 3.E+13 [e/s] 3.14E+7[s] =1.E+16 [T] Actility: $-dN_T/dt$ =1.E+16 / (12*3.14E+7 s) = **2.6 E+7 Bq**

• This amount of Tritium may be accumulated by tritium absorbers.

Lifetime of various materials from

FLUKA simulations.

Material lifetime from FLUKA simulations

CPS Material	"Lethal" Dose	Max. Dose rate	Life time	Life time	Comment
	(unit)	(unit)	(unit)	(year)	
SuperNG [16]	$4 \times 10^7 \text{ (rad)}$	10 (rad/h)	4×10^6 (h)	≥ 400	Connectors
EVA [12]	$2 \times 10^7 \text{ (rad)}$	10 (rad/h)	2×10^6 (h)	≥ 200	Cable insulation
Low Den. Polyeth. [12]	$1 \times 10^7 \text{ (rad)}$	10 (rad/h)	1×10^6 (h)	≥ 100	Cable insulation
Low Den. Polyeth. [12]	$1 \times 10^7 \text{ (rad)}$	$5 \times 10^3 \text{ (rad/h)}$	2×10^3 (h)	≥ 0.2	Shield
Alumina ceramics [14]	$10^{21} ({\rm n/cm}^2)$	$5 \times 10^9 (n/cm^2/s)$	2×10^{11} (s)	$\geq 6,000$	Coil ins.
Alum./Silica glass [13]	$10^{7} (Gy)$	0.1 (Gy/s)	1×10^8 (s)	≥ 3	Opt. Prop. study
Silica ceramics [14]	$> 0.3 \times 10^{21} \ (n/cm^2)$	$5 \times 10^9 (n/cm^2/s)$	6×10^{10} (s)	> 2,000	3 m Coil insul.
Silica ceramics [12]	$> 10^8 (Gy)$	0.1 (Gy/s)	10^{9} (s)	> 30	Coil insul.
Kapton [7]	$10^7 (Gy)$	0.1 (Gy/s)	10^{8} (s)	≥ 3	Coil insulation
Fiber Glass Cloth [7]	$5 imes 10^7 { m (Gy)}$	0.1 (Gy/s)	5×10^8 (s)	≥ 15	Coil insulation
Epoxy [12]	$6 \times 10^7 ~(\mathrm{Gy})$	0.1 (Gy/s)	6×10^8 (s)	≥ 20	Coil insul.

• Blowing He through CPS may prevent oxidation and improve lifetime of some materials.

Conclusion

In our concept, the **CPS is** an **Orientable Unit** containing the **entire Beam Channel**. CPS is **surrounded** with several **layers of shielding** materials. CPS provides a 98% **clear beam** of **2.E+13 photons/s** on KPT.

This concept allows **to avoid risks** and provide:

- 1. **No Overheating** of Copper Absorber $(T_{max} = 210^{\circ} \text{ C})$.
- 2. No Short Circuit in Magnet Coil for up to **15 years** with fiberglass based insulation.
- 3. No Prompt Radiation > 10 rad/hr around CPS and > 0.1 mrem/hr on top of Tagger Hall.
- 4. No Activation > 20 mrem/hr around CPS after 1000+1 hrs of continuous operation .
- 5. No Tritium Activity > 200 Bq/L in ground and cooling waters. (~3% of VA limit).



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- 6. Magnet and insulation lifetime:
- 7. Cooling system & ground waters contaminations:
- What will the photon **beam quality** be:
- **Cost and schedule estimates** for the construction of the CPS:
- **Civil constructions** to contain the radiation in the Tagger Hall:
- **Decommissioning Plan** for CPS and Activated Components:

Specifically the Presented below. Simplified Tagger & KPT Halls. FLUKA2021.2.9. 12 GeV beam 3.1E+13 e/s, (5μA), FWHM=**2.5 mm**, < **1 mrem/hr** on top of Tagger Hall and Tunnel Mounds. $<2 \text{ kW/cm}^3$, Cu Absorber $< 220^{\circ}\text{C}$, Pb shield $< 110^{\circ}\text{C}$. Dose < 10 rad/hr, <20 mrem/hr. Maps available. 0.25×0.5 Tm, I ≤ 1.8 kA, wire 2×2 cm², T< 150°C, LT=15 years. Tritium Activity **2.6*10⁷ Bq** & **200 Bq/L** after 1 year. \sim **2.E+13** γ /s, FWHM=4 cm, neutrons & ± part<**2%**. **\$800,000** without magnet.

No.

To be mounted on rails to **move aside** for storage.

Optimized CPS with external layers of "elliptical" shape.



Thank you for your attention.

Hall D K-Long Facility E12-19-001. Experiment Readiness Review Phase I. Jefferson Lab, 2023 Charge.

- Is there any R&D needed to be done prior to start the construction of the KLong Facility? • No 5μ A electron beam on the CPS
- What is the status of the Compact Photon Source (CPS)? ٠
- Conceptual design: 1.
- 2. Evaluation of the **produced radiation**:
- 3. **Approximations** in the MC simulations and Code used:
- 4. Energy deposition , **Absorber** and **Lead temperature**:
- 5. Prompt **dose** and **activation** around the CPS (Tagger Hall):
- Magnet and insulation lifetime: 6.
- 7. Cooling system and ground water contaminations:
- What will the photon **beam quality** be: •

- FWHM=**2.5 mm**, **3.1E+13 e/s**, steering magnet.
 - Specifically the :

Presented.

- < **1 mrem/hr** on top of Tagger Hall and Tunnel Mounds. Simplified Tagger & KPT Halls. FLUKA2021.2.9.
- 2 kW/cm^3 , Cu Absorber $< 200^{\circ}\text{C}$, Pb shield $< 100^{\circ}\text{C}$.
- Dose < **10** rad/hr, <**20** mrem/hr. Maps available.
- 0.25×0.5 Tm, I≤1.8 kA, 4-6 turns, wire 2×2 cm², T<**150°C**, LT=**15** years.
- Tritium Activity **2.6*10⁷ Bq** and **200 Bq/L** after 1 year.
- **1%** of neutrons and \pm part . FWHM=4 cm, **3E+13** s⁻¹

No

- What are the **cost and schedule estimates** for the construction of the CPS: 800 k\$ (no magnet). •
- Will **civil constructions** be needed to contain the radiation in the Tagger Hall: •
- What is **Decommissioning Plan** for CPS and Activated Components: mounted on a platform, **move aside**. •

CPS Components. Weight and Cost.

CPS Component	Material	Density	Cost	Weight	Total Cost
		(g/cm^3)	(\$/kg)	(MetricT)	(\$)
Absorb. In/Out	W	16.3	80.00	0.2	15,500
Lead skin	Pb	11.4	5.8	15. <mark>1</mark>	87,500
Plastic shield	Borated PE	1.2	20.5	0.5	10,100
Lead shield	Pb	11.4	5.8	36.5	211,400
Left shield	W	16.3	80.0	1.4	108,000
Top shield	W	16.3	80.0	0.8	67,000
Right shield	W	16.3	80.0	1.4	108,000
Bottom shield	W	16.3	80.0	0.8	67,000
Magnet	Fe	7.9	50.0	2.0	101,800
Absorber	Cu	9.0	122.6	0.2	27,400
Upstream shield	W/Cu	15.2	140.0	0.2	21,600
Downstream shield	W/Cu	15.2	140.0	1.2	171,400
CPS		8		60.9	894,100
Total tungsten				5.8	543,200

- CPS weight 61,000 kg.
- CPS cost without magnet \$793,000.
- Including Tungsten cost \$543,000.

Coil Deformation due to Ampere's force.



Consider a squared **Cu wire S=(1.7 cm)²**, **L=20 cm** as a rod with fixed end under load including gravitation +25.5 N/m, total **f = f'+25.5 = 50.5 N/m**. From **tabulated formula** the maximum sag at the end of the rod:

$$\begin{split} \delta = 3/2 \ f \ (L/W)^4 E^{-1} \\ = 1.5^* (50/1.2)^* (20/1.7)^4 * 10^{-11} = 12 \ \text{microns} \ (\text{compare with 8 mm gap}) \\ \text{where } E = 1.2E + 11 \ \text{N/m}^2 \ \text{-} \ \text{Young's module tabulated for copper.} \end{split}$$

• Insulation is not required for Coil return in high radiation area.

Magnet at CPS exit cleans photon beam.

USRBIN CPSKPTLEAD1712narrGUNvacTRP 58



Charged tracks from radiator.

Charged tracks from beam channel.

Power Deposition in Skinny Layer of Hot Segment. Fine map 0.05 cm.



- Maximum $dP/dV = \sim 2 kW/cm^3$
- **ANSYS calculations** are done by Tim Whitlatch (JLab) using this Map.

Constitution of the second distances of the second s



"Hot" Absorber (Cu), 53 cm long, 6.35mm Beam Hole with Air, 30 mm Water Channel (**5 kW/m² C**) evacuates 29 kW at **T**_{water}~**45** °C.

• Maximum Copper Temperature 286 °C (melts at 1,084 °C).

Prompt dose and Polyethylene lifetime.



- BPE elastic properties degrade significantly after **1.E+7 rad** / 5000 rad/hr = ~0.2 year.
- Borated polyethylene can **not** be used as **construction material**.
- Possible **solution**:- BPE granules in **metal tanks** or containers.

https://www.osti.gov/biblio/4640611

Neutron Flux r-profile in Hot Spot. Steel is OK up to 10^{22} n/cm²



https://www.osti.gov/biblio/4640611 Life Time = 10^{11} s =3200 years. Steel is OK up to 10^{22} n/cm².

Problem of High radiation in return part of Coils.



Coil Design and Insulation Exposure to Radiation.



- Attractive force of bent parts $F = 25 \text{ N/m}^* 0.3 \text{ m} = 7.5 \text{ N}.$
- Copper 1.7 cm -wires (tubes) will not touch .

Leakage Current between wires.

Current through gas :

 $dI/ds [A/cm²] = n [e/cm³] \times v [cm/s] \times e [C]$

- 1. What is concentration of electrons n?
- 2. What is the drift velocity of electrons w?

1. What is n and Ionisation in Magnet Coil.

 $dI/ds [A/cm²] = n [e/cm³] \times v [cm/s] \times e$

Assume maximum dose D in space between coil windings is D = 1.E-5 [GeV/g/e] (~10 × of FLUKA estimate). Assume 10 eV is required to produce one electron -ion pair.

Dose D translate to ion **pair production** \sim **1.E+3[pair/g/e]** = 1.E-5 [GeV/g/e] / 1.E-8 [GeV]). Ion pair production rate **per unit of mass** is at beam intensity 3.E+13 [e/s] :

$$dN/dt = 3.E+16 \text{ [pair/g/s]} = 1.E+3 \text{ [pairs/g/e]} \times 3.E+13 \text{ [e/s]}.$$

Assume we have 1 cm of argon between windings (ρ_A =1.7E-3 [g cm⁻³] = ~2.E-3). Air – 1.3E-3 ; He – 0.17E-3 So we find the ion production rate between coil wires :

 $dn_p/dt = (dN/dt) \ \boldsymbol{\varrho}_A = 3.E + 16 \ [pairs g^{-1} s^{-1}] \times 2.E - 3 \ [g cm^{-3}] = 6.E + 13 \ [pair cm^{-3} s^{-1}]$

This rate is **balanced by recombination** of argon ions and electrons.

Drift velocity of electrons and ions in dry and humid air and in water vapour H. RYZKO Institutet for Hogspbningsforskg vid Uppsala Universitet, Uppsala, Sweden MS. received 7th Septembw 1964 https://journals.aps.org/pr/abstract/10.1103/PhysRev.32.624#.~.text=From%20the%20measured%20rate%20of, because%20of%20several%20unavoidable%20errors.

1. What is n. Ionisation in Magnet Coil and Leakage Current. $dI/ds [A/cm^2] = n [e/cm^3] \times v [cm/s] \times e$

 $dn_{n}/dt = 6.E + 13$ [pairs cm⁻³ s⁻¹] is balanced by recombination of argon ions and electrons defined as: $dn_/dt = \alpha n_n$, where $\alpha = 2.E-10 [cm^3 i^{-1} s^{-1}]$ recombination coeff. for Argon. $(\alpha = \sim 1.E-8 \text{ [cm}^3 \text{ i}^{-1} \text{ s}^{-1} \text{]}$ for He, and $\alpha = 1.E-6 - 1.e-7$ for Air.)

Assuming equal densities $\mathbf{n}_{\perp} = \mathbf{n}_{\perp} = \mathbf{n}$ for the equilibrium density of electrons \mathbf{n} we write:

 $\alpha n^2 = dn_n/dt = 6.E+13$ [pairs cm⁻³ s⁻¹] from the previous slide and $n^2 = \alpha^{-1} dn_{,}/dt = 0.5E + 10$ [pairs s cm⁻³]×6.E+13 [pairs cm⁻³ s⁻¹] = 3.E+23 (pairs/cm³)².

The equilibrium **density of electrons** yields $n = 6.E+11 (pairs/cm^3)$. •

Density of electrons is **proportional** to the gas specific factor $(\alpha^{-1} \boldsymbol{\varrho}_{A})^{\frac{1}{2}}$. •

2. What is *v* and Electric Field between Wires at 2 kA current.

What is Voltage between windings?

Copper resistivity $\varkappa = 1.7E-6$ [Ohm·cm]; $L_w/S_w = 100 \text{ cm}/3 \text{ cm}^2 = 25 \text{ cm}^{-1}$ => Voltage between windings (V= I × R_w where $R_w = \varkappa × L_w/S_w$) V = 2000 [A]× 1.7E-6 [Ohm·cm] ×25 [cm⁻¹] = 2.E-6 ×5.E+4 [Ohm·A]

V = 0.1 V.

From **Top Plot**⁽¹⁾ we see **drift velocity** as $\boldsymbol{v} = \boldsymbol{v}(\mathbf{E}/\mathbf{P})$ where

E -electric field, P=gas pressure.

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In our case E=0.1 [V cm<sup>-1</sup>]; P=~1000 [mmHg] =>
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E/P=1.E-4 [V cm⁻¹/mmHg]

From Top Plot we read v(0.1)=2.E+6 [cm/s] and linear interpolation yields: v(1.E-4)=2.E+3 [cm/s].

From Bottom Plot for air we find v(1.E-4)=5.E+1 cm/s.





Figure 5. Electron drift velocity in dry air, humid air and water vapour as a function of reduced electrical field. Pressure readings reduced to temperature of 20°c; humid air, $p_{elp} = 16\%$. Broken line, Townsend and Tizard 1913; \triangle , Raether; \Box , Rieman 1944; NB, Nielson and Bradbury 1937; LR, Lowke and Rees 1963.

2. What is leakage current between wires.

Current density between windings: $dI/ds [A/cm²] = n [e/cm³] \times v [cm/s] \times 1.6E-19 [C/e] \qquad \propto \quad v (\alpha^{-1} \boldsymbol{\varrho}_{\lambda})^{1/2}$ Where n=6.E+11 [e/cm³]. v = 2.E + 3 [cm/s]. For the current density we find : $dI/ds [A/cm^{2}] = 6.E + 11[e/cm^{3}] \times 2.E + 3 [cm/s] \times 1.6E - 19 [C/e] = 12 \times 1.6 E(+11+3-19) = 12 \times 1.6 E(+11$ $=20.E-5 [A/cm^{2}].$ Wire area S=2 cm×100 cm =**2.E+2 cm²**, and the maximum possible current yields: $I[A] = 20.E-5 [A/cm^{2}] \times 2.E+2 [cm^{2}] = 40.E-3 [A] = 40 [mA].$ Compare to 2 kA !

- Leakage is of 2.E-5 of the wire current. It does not affects the coil performance.
- For Helium the leakage is ~10 times lower due to the gas specific factor $\psi (\alpha^{-1} \varrho_{He})^{1/2}$.

