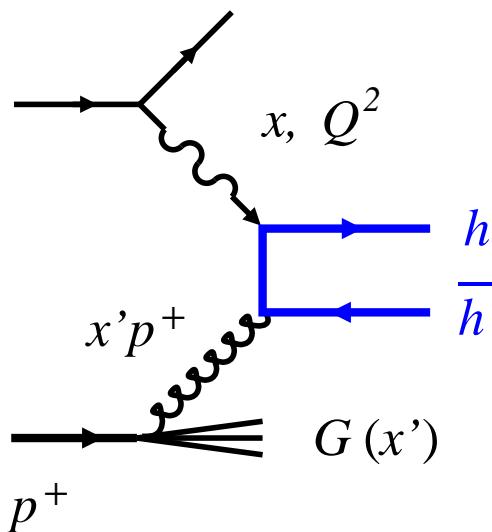


# $F_2^c$ and rate estimates using analytic methods

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C. Weiss, LDRD Project "Nuclear gluons with charm at EIC," Meeting 16-Dec-15

- Heavy-quark structure function  $F_2^h$  in LO QCD



$$F_2^h(x, Q^2) = \int_{ax}^1 \frac{dx'}{x'} x' G(x') \hat{F}_g^h(x/x', Q^2, m_h^2, \mu^2)$$

$$\hat{F}_g^h(\dots) = \frac{\alpha_s(\mu^2)}{m_h^2} \frac{Q^2}{4\pi^2} e_h^2 \times \text{function}(x/x', Q^2)$$

$$a = 1 + \frac{4m_h^2}{Q^2} \quad \text{sets limit of } x' \text{ integral}$$

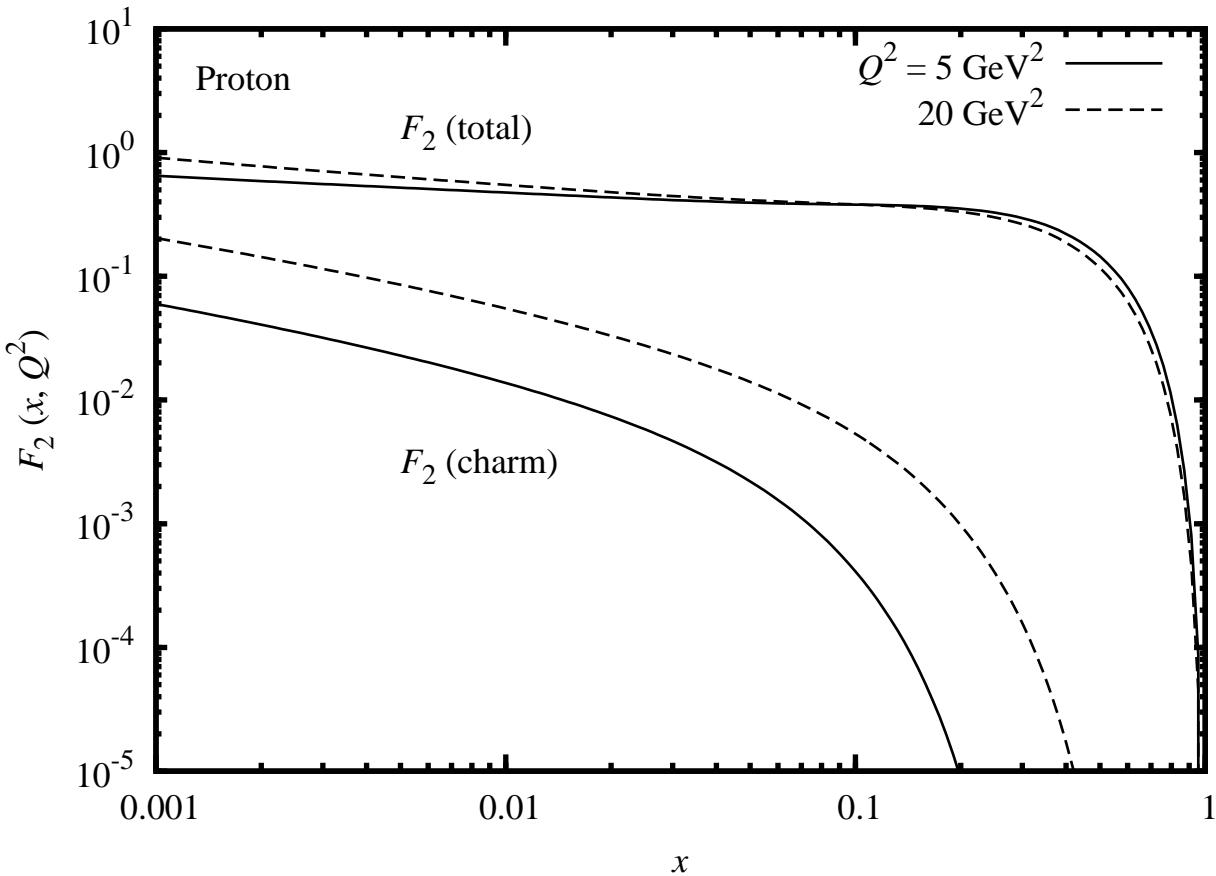
LO scale set at  $\mu^2 = 4m_h^2$ , perturbative stability  
Gluck, Reya, Stratmann, NPB 422, 37 (1994)

Charm mass  $m_c \sim 1.5 \text{ GeV}$

Can be generalized to photoproduction

# Charm structure function $F_2^c$ : $x$ -dependence

2

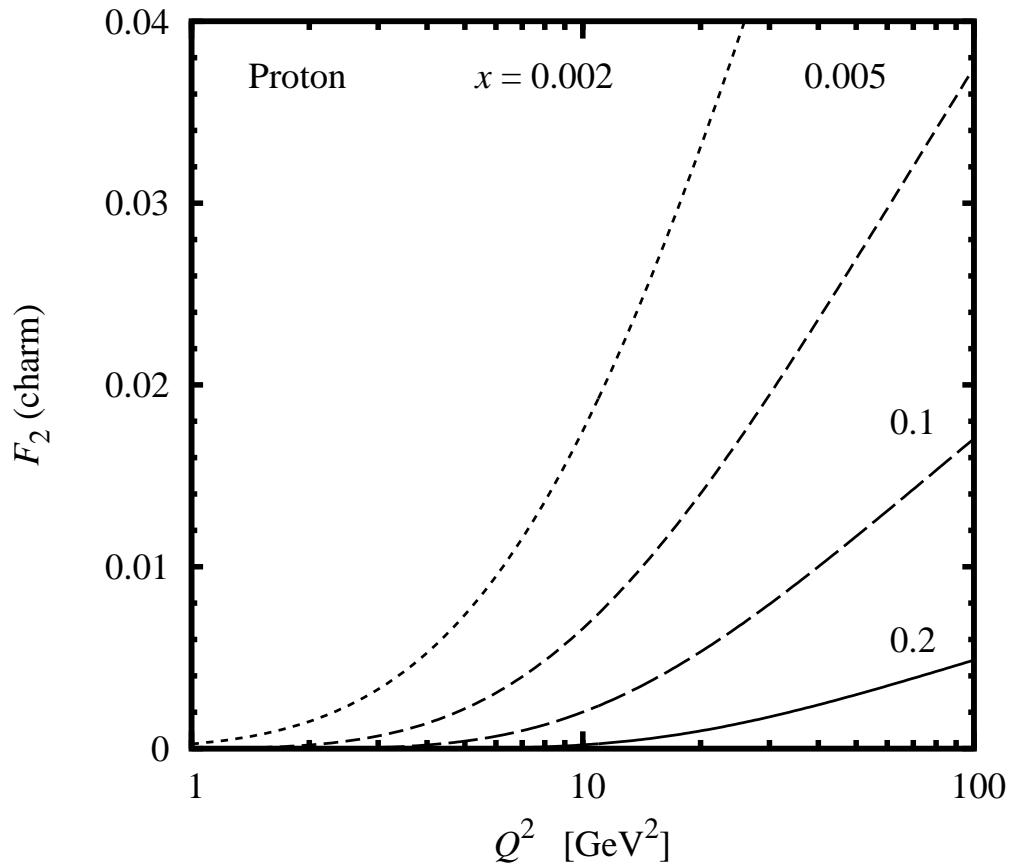


$F_2^c$  and ratio  $F_2^c/F_2$  decrease rapidly with  $x$

Strong  $Q^2$  variation of  $F_2^c$  at fixed  $x$ : Kinematic effect

# Charm structure function $F_2^c$ : $Q^2$ -dependence

3



$F_2^c$  increases rapidly with  $Q^2$  at fixed  $x$ : Kinematic effect

# Charm cross section and rate

$$d\sigma(eN \rightarrow e' + c\bar{c} + X) = \mathcal{F}(x, Q^2) dx dQ^2 \quad \text{diff cross section, } \int d\phi(e')$$

$$\mathcal{F}(x, Q^2) = \frac{2\pi\alpha_{\text{em}}^2 y^2}{Q^4(1-\epsilon)} \left[ \frac{F_2^c}{x} - (1-\epsilon)\frac{F_L^c}{x} \right]$$

$$\Delta N = L_{\text{int}} \int_{x_1, x_2} dx \int_{Q_1^2, Q_2^2} dQ^2 \mathcal{F}(x, Q^2) \quad \text{event nr in bin } [x_1, x_2] \times [Q_1^2, Q_2^2]$$

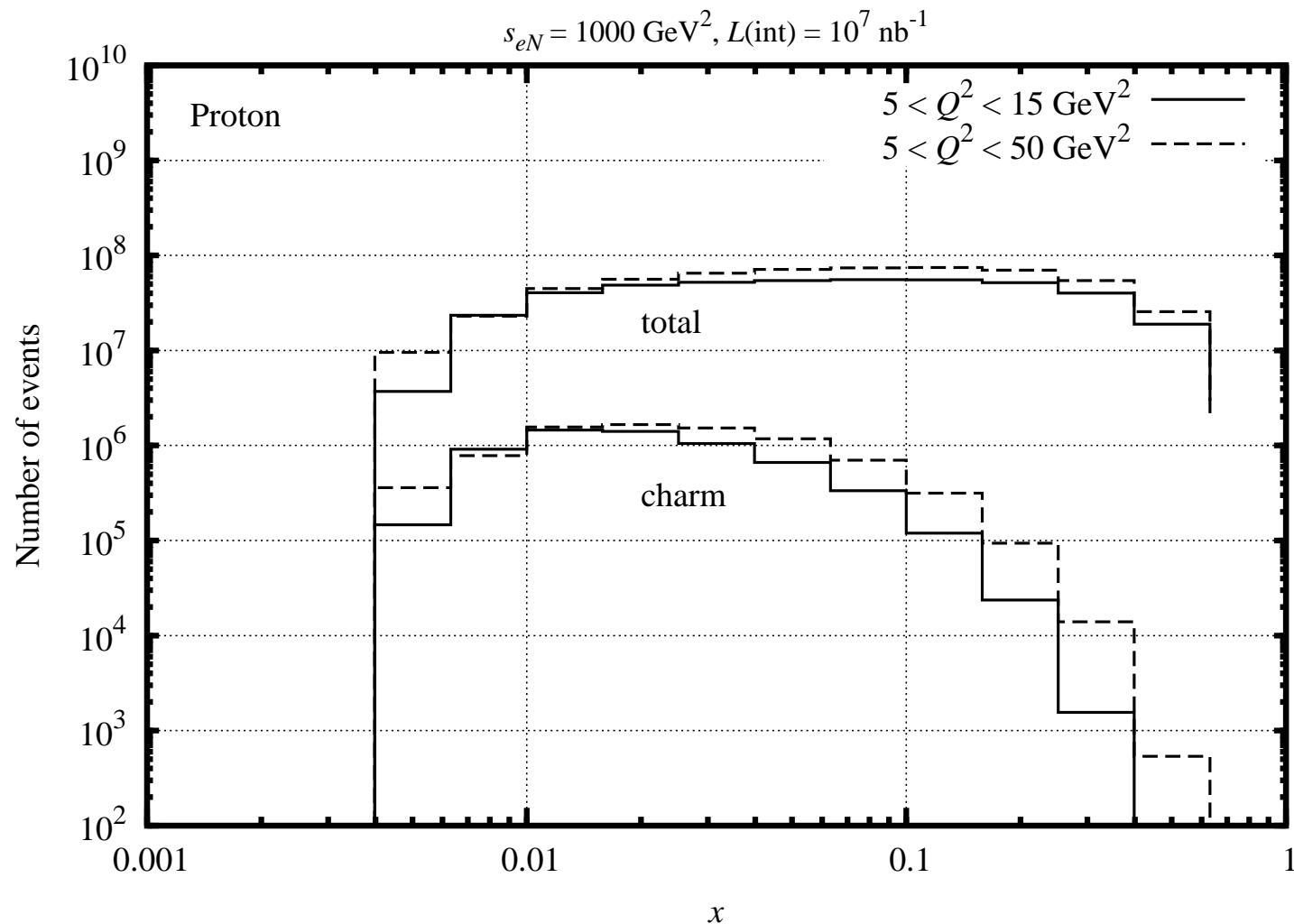
$$L_{\text{int}} = LT \quad \text{integrated luminosity}$$

$$L_{\text{int}} = 10^7 \text{ nb}^{-1} \quad \text{for} \quad L = 10^{34} \text{ cm}^{-2} \text{s}^{-1}, \quad T = 2 \text{ weeks} \approx 10^6 \text{ s} \quad \text{ref value}$$

Rates estimated by numerical integration of LO cross section

# Charm rate: $x$ -dependence

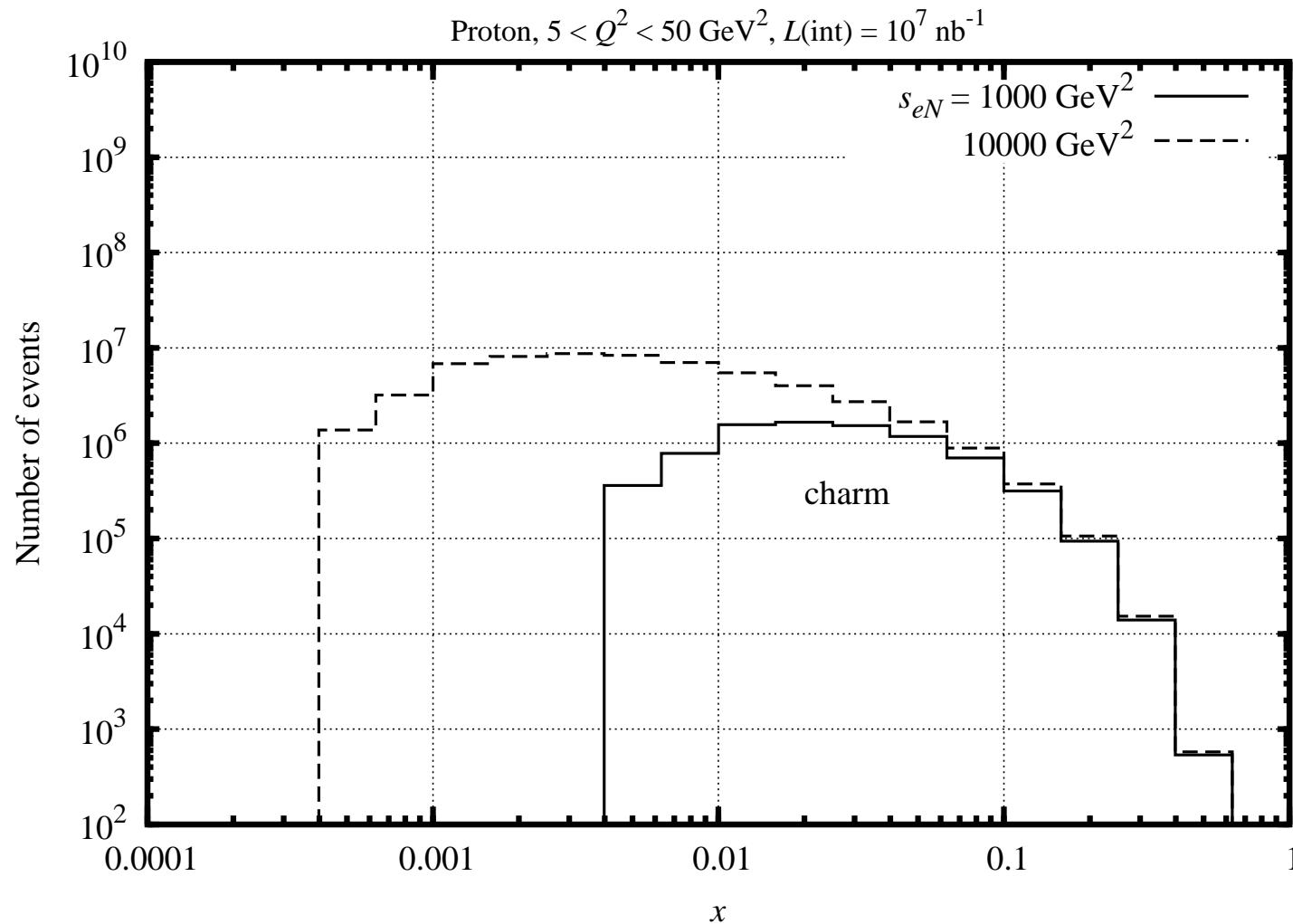
5



- Here 5 bins per decade in  $x$ , single wide bin in  $Q^2$
- Rates drop rapidly at large  $x$
- Nuclear rates comparable: Structure function  $F_{2A}^c \sim A F_{2N}^c$ , but luminosity  $L_A \approx L_N/A$

# Charm rate: CM energy dependence

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- Little dependence on  $s_{eN}$  at large  $x$ , because flux  $y^2/(1 - \epsilon)$  independent of  $s_{eN}$  for  $y \ll 1$
- Lower limit in  $x$  depends on  $s_{eN}$
- Angular distributions at given  $x$  will change with  $s_{eN}$

# Questions and tasks

- Analytic estimates should be confirmed by MC integration
- Sensitivity to gluon PDF can be studied using analytic estimates
- What does ratio charm/total imply for charm identification/reconstruction?