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# E-P SCATTERING PUZZLE

Marko Horbatsch – York University, Toronto, Canada  
Jefferson Lab talk, December 8, 2017

Funding: NSERC. Credits: Eric A. Hessels, Douglas Higinbotham, Jose Alarcón



# What is the proton radius puzzle?

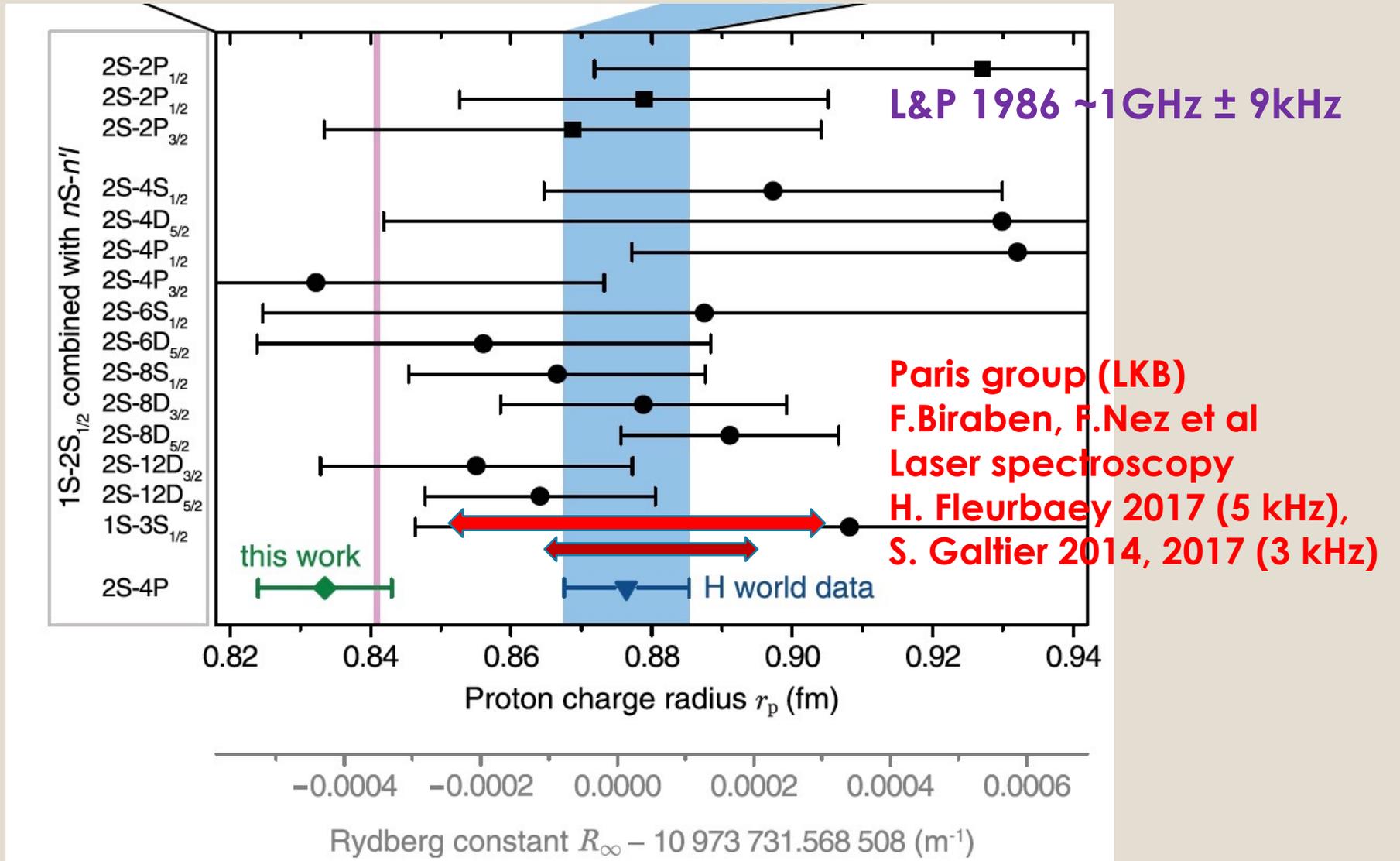
- 2010: CODATA uses regular hydrogen spectroscopy data (mostly)
- Also: elastic e-p scattering data, to declare  $R_p=0.8755(51)$  fm
- Even though: muonic hydrogen Lamb shift (CREMA):  $R_p=0.84169(66)$  fm
- Triggers: re-analysis of e-p scattering, re-analysis of hydrogen spectroscopy, much debate over 'new' physics (the muon not just a cousin to the electron?)
- Demand for new regular hydrogen spectroscopy!
- 2014 CODATA: doesn't trust the muonic hydrogen result YET!
- Rydberg constant (SI-au conversion!) is severely affected.

# Outline

- 1. Spectroscopy overview: Garching vs Paris
- 2. elastic e-p scattering problem: what is the problem?
- 3. using moments from theory? C.Peset and A.Pineda; J.Alarcón and C.Weiss
- 4. need the z-expansion, or the  $\zeta$ -expansion (shifted z-expansion at fixed  $Q^2_{\max}$ )
- 5. Are 8 parameters sufficient to fit the MAMI data up to 1 GeV<sup>2</sup> ? (instead of 24)
- Will the scattering puzzle come to rest soon? Will the spectroscopy puzzle?

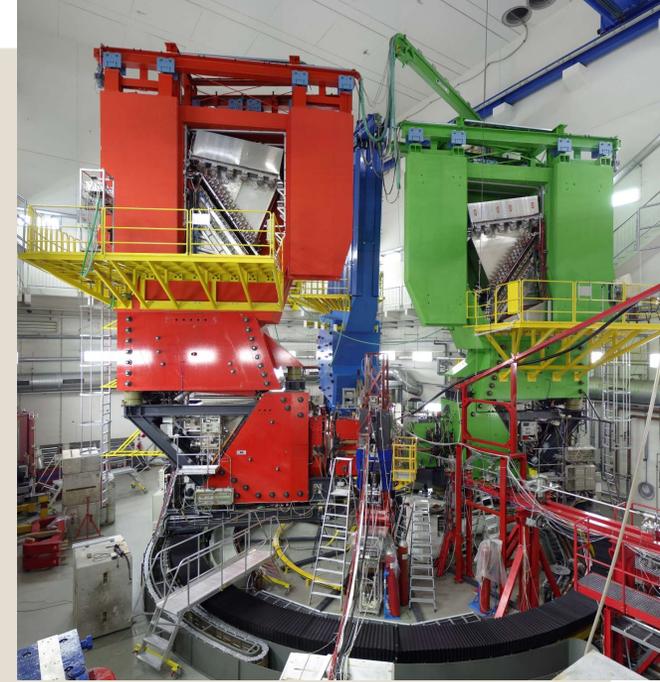
# Spectroscopy results (Science 358, 79)

MPQ Garching:  
Fluorescence  
following  
Laser excitation  
Big quantum  
interference  
systematic!



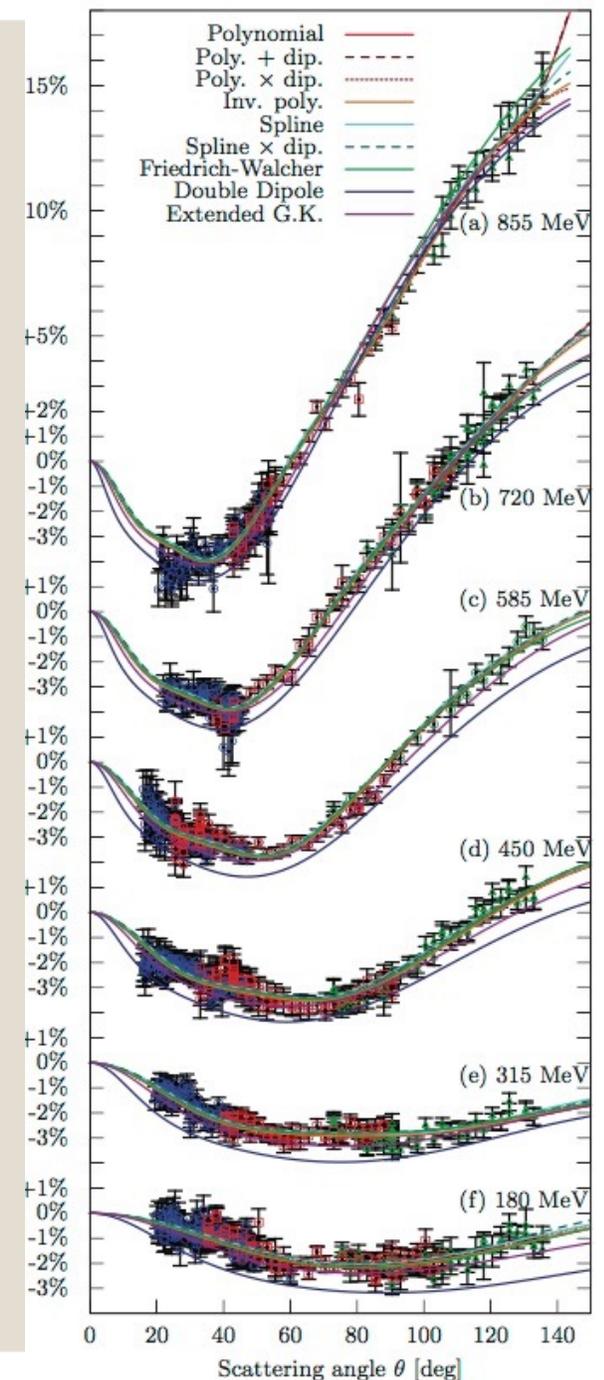
# Elastic e-p scattering (post-2010)

- Elastic e-p scattering with relativistic electrons
- De Broglie wavelength chosen to not look inside the proton
- Mainz (MAMI); Jan Bernauer et al.: 1422 data at momentum transfer squared  $Q^2 < 1 \text{ GeV}^2/c^2$  using 6 beam energies
- Probing electric and magnetic charge distributions at the same time, except when  $Q^2$  small
- Scattering problem: can it be inverted?
- Dispersion relations = analytic property of the form factors!
- Photoproduction ( $\gamma$ -p scattering) of pions has a threshold at twice the pion mass squared!
- Are fits in  $Q^2$  justified when the range exceeds threshold ( $0.078 \text{ GeV}^2/c^2$ )???
- Conformal mapping to the rescue!



# MAMI (J. Bernauer et al)

- Used many fits to arrive at [Phys Rev C90, 015206 (2014)]
- $R_p = 0.879(5)_{\text{stat}} (4)_{\text{sys}} (2)_{\text{model}} (4)_{\text{group}}$  fm
- Magnetic radius:  $\sim 0.80$  fm (depends on TPE model)
- Problem: reduced  $\chi^2$  of 1.14 ! (problem with error bars)
  
- Disputed by a number of different analyses:
- Horbatsch&Hessels: different models can give 0.84 and 0.89 fm
- Low- $Q^2$  data fits: favor small radius (Higinbotham et al, Griffioen et al)
- I. Sick and D. Trautmann fight back (PRC 95, 012501) defending large  $R_p$ , and defending the need to go to high  $Q^2$ .



# Low- $Q^2$ fit: using moments from $\chi$ PT

- H&H&Pineda: PRC 95, 045203 (2017)
- Peset&Pineda: effective field theory: QCD reduced to heavy baryons ( $p$ ,  $\Delta$ ) and  $\pi$
- Cannot predict  $\langle R_p^2 \rangle$ , but  $\langle R_{\text{mag}}^2 \rangle$  and  $\langle R_p^4 \rangle$ , etc., really the form factors minus  $R_p$
- Fit low- $Q^2$  MAMI data to:      and please note the VIRTUAL PHOTON POLARIZATION  $\epsilon$  !!!

$$\sigma_{\text{red}} = (1 + \tau) \frac{d\sigma}{d\Omega} / \frac{d\sigma_{\text{Mott}}}{d\Omega} = G_E^2 + \frac{\tau G_M^2}{\epsilon},$$

$$G_E(Q^2) = 1 - \frac{R_p^2}{3!} Q^2 + \frac{\langle r^4 \rangle_E}{5!} Q^4 - \frac{\langle r^6 \rangle_E}{7!} Q^6 + \dots$$

$$\frac{G_M(Q^2)}{\mu_p} = 1 - \frac{\langle r^2 \rangle_M}{3!} Q^2 + \frac{\langle r^4 \rangle_M}{5!} Q^4 - \frac{\langle r^6 \rangle_M}{7!} Q^6 + \dots$$

$$\tau = Q^2 / (4m_p^2)$$

$$\epsilon = \left[ 1 + \frac{4Q^2 + \frac{Q^4}{m_p^2}}{8E^2 - 2\frac{Q^2}{m_p}(2E + m_p)} \right]^{-1}$$

Note:

At the lowest  $Q^2$   $G_E$  only, but...

$$R_p = \sqrt{-3 \frac{d\sigma_{\text{red}}}{dQ^2} \Big|_{Q^2=0} + \frac{3\mu_p^2}{4m_p^2}}$$

# One-parameter $R_p$ fits? - 'kind of'; show ' $G_E^2$ '

$\chi$ PT moments come with substantial uncertainties. Fits work up to some  $Q^2_{\max}$  with  $\chi^2_{\text{red}} < 1.14$

Data come in groups (here five) with floating normalization constants (less than 1 % different from 1).

Extracted charge proton radius  $R_p$  has **statistical** and **systematic** uncertainties

Beam energies:

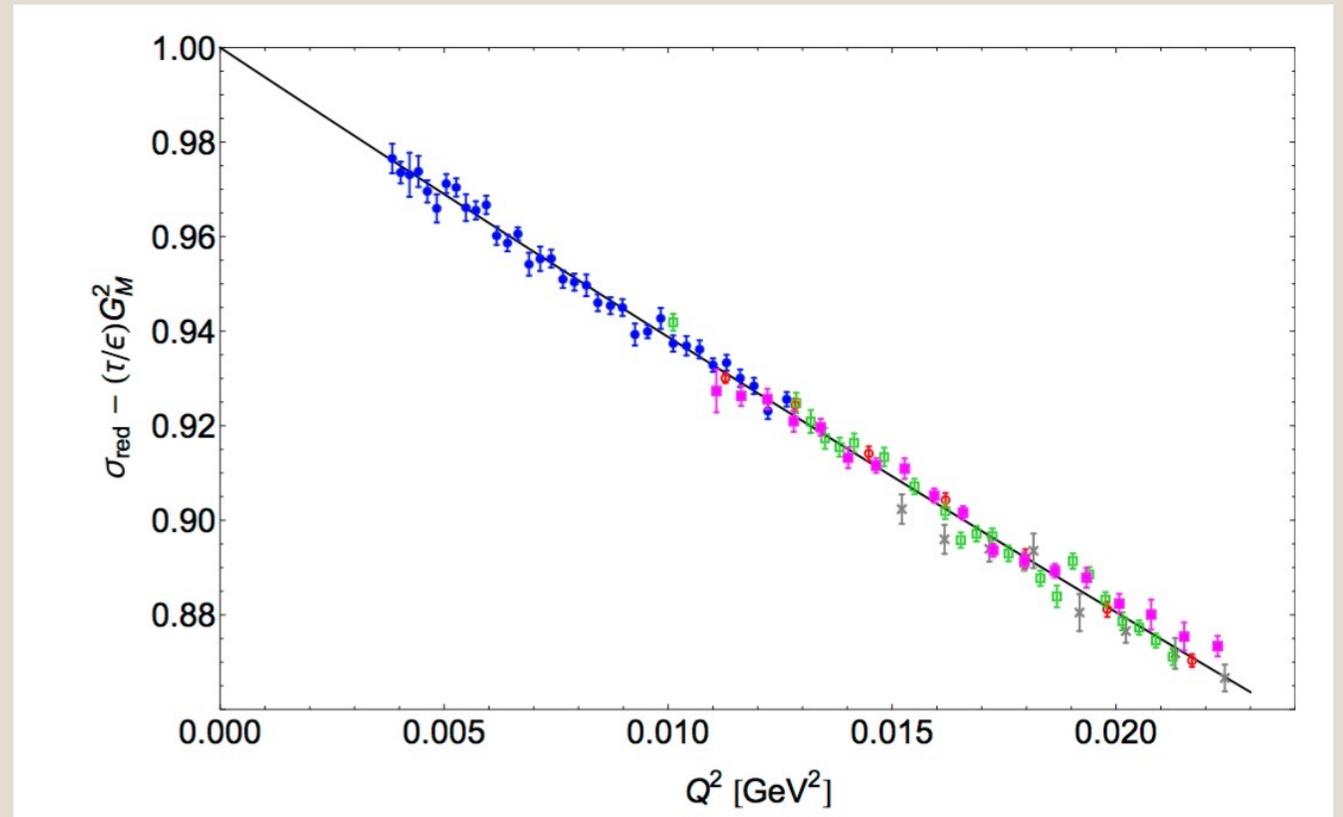
180 MeV: blue, red, green

315 MeV: magenta

450 MeV: gray (Rosenbluth method?)  
(270/1422 MAMI data)

For  $R_p$  we need the slope at  $Q^2=0$  !

Big question: are the predicted  $\chi$ PT moments (incl. uncertainties) reasonable?



# What do we get when using less vs more data?

Blue band: statistical  
 Pink: syst.:  $\langle r^2 \rangle_M$   
 Green syst. Higher

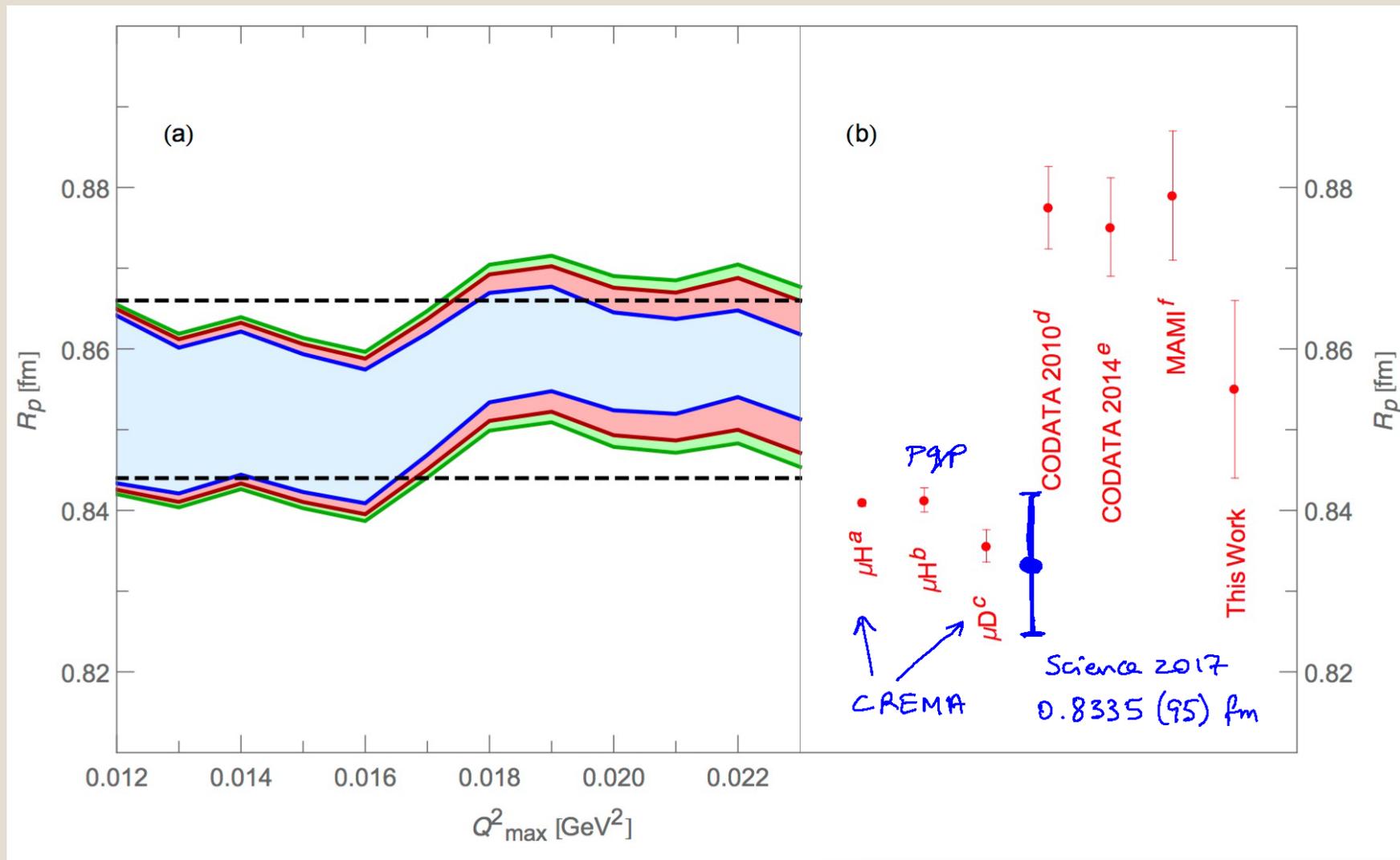
Note:  
 We are far from the  
 branch cut ( $0.078 \text{ GeV}^2$ )

$\chi$ PT bound in  $\text{fm}^2$ :

$$0.28 < \langle r^2 \rangle_M < 0.60$$

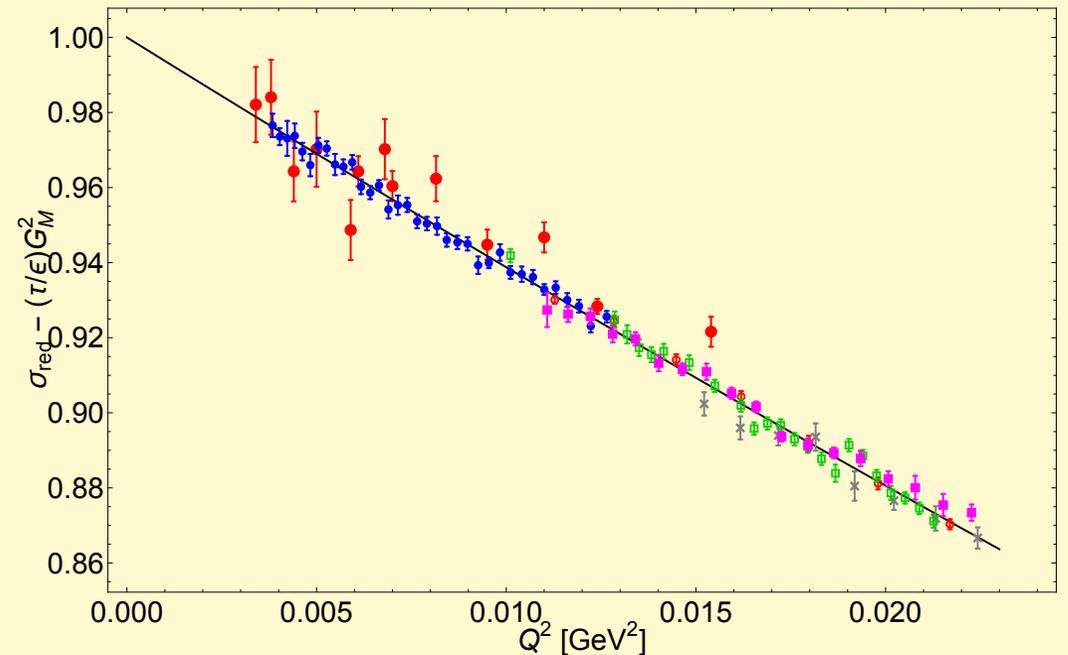
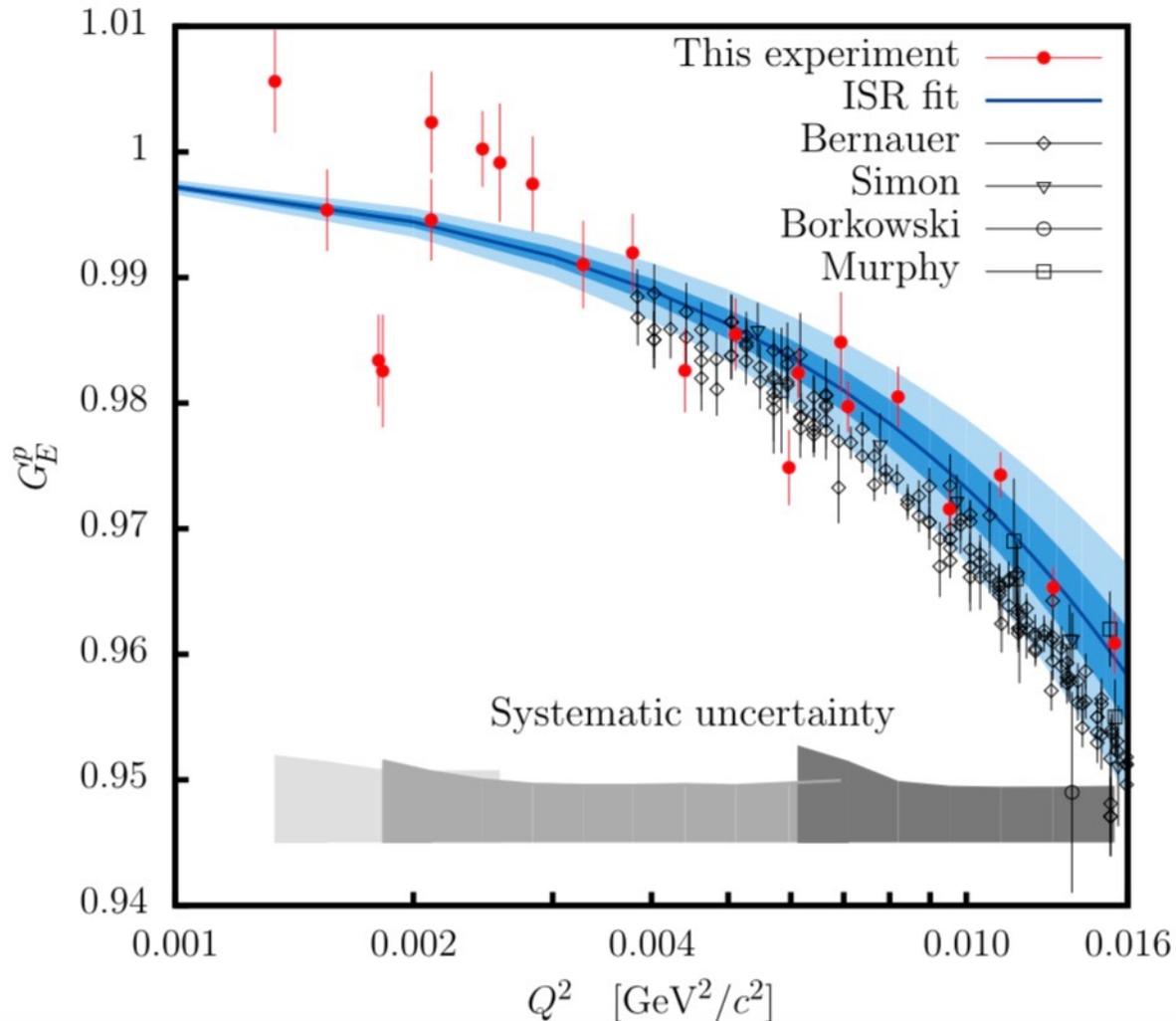
Current  $R_M = 0.8 \text{ fm}$   
 ( $\chi$ PT marginal ?)

Main reason why we stop  
 at  $0.023 \text{ GeV}^2$ , but  $\langle r^4 \rangle_E$  is  
 also 'small'.



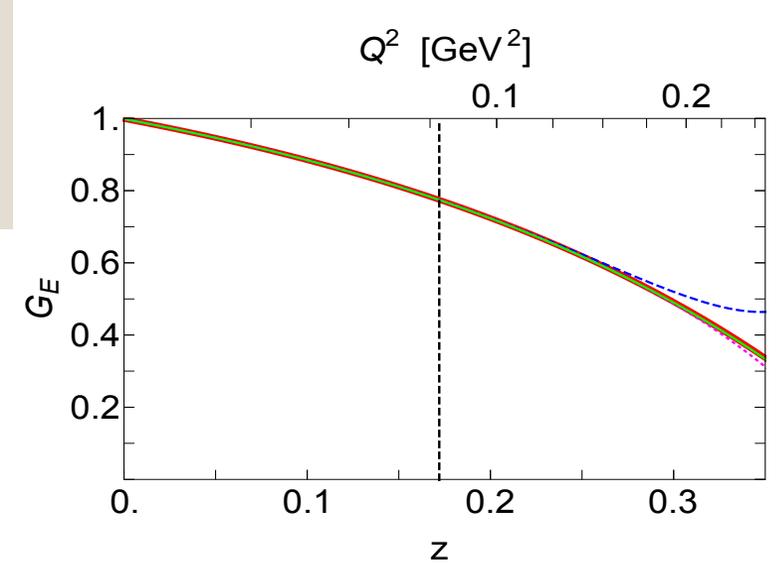
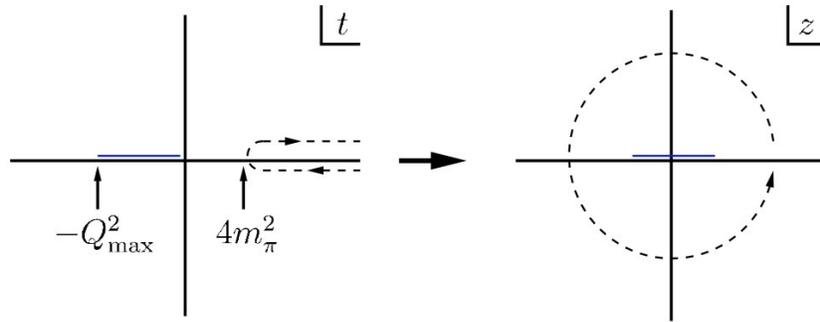
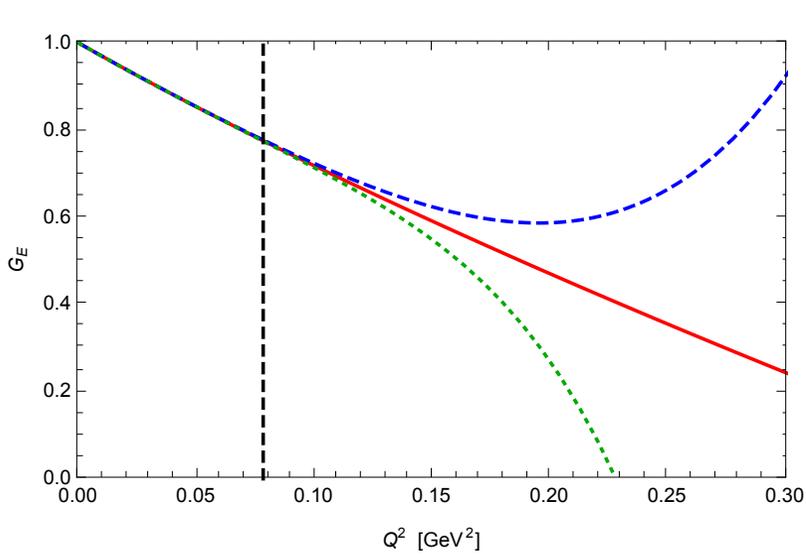
# New MAMI on the horizon (PRad competition?)

- Initial-state radiation, Phys Lett B771,194 (2017), arXiv1612.06707



$R_p$  small, after all ?

# $G_E$ and $G_M$ from effective theory (Peset and Pineda)



R.J. Hill and G. Paz re-introduce this (forgotten?) method!

$$z = \frac{\sqrt{t_c - t} - \sqrt{t_c}}{\sqrt{t_c - t} + \sqrt{t_c}}$$

Moment expansion in  $Q^2$  fails beyond 0.078 due to branch cut (charged pions) at  $Q^2 = -0.078 = -t_c$

$\gamma$ -p scattering, dispersion relations

Note: we had to put in  $R_p^2 = \langle r^2 \rangle_E$  (here  $R_p = 0.85$  fm)!

But:

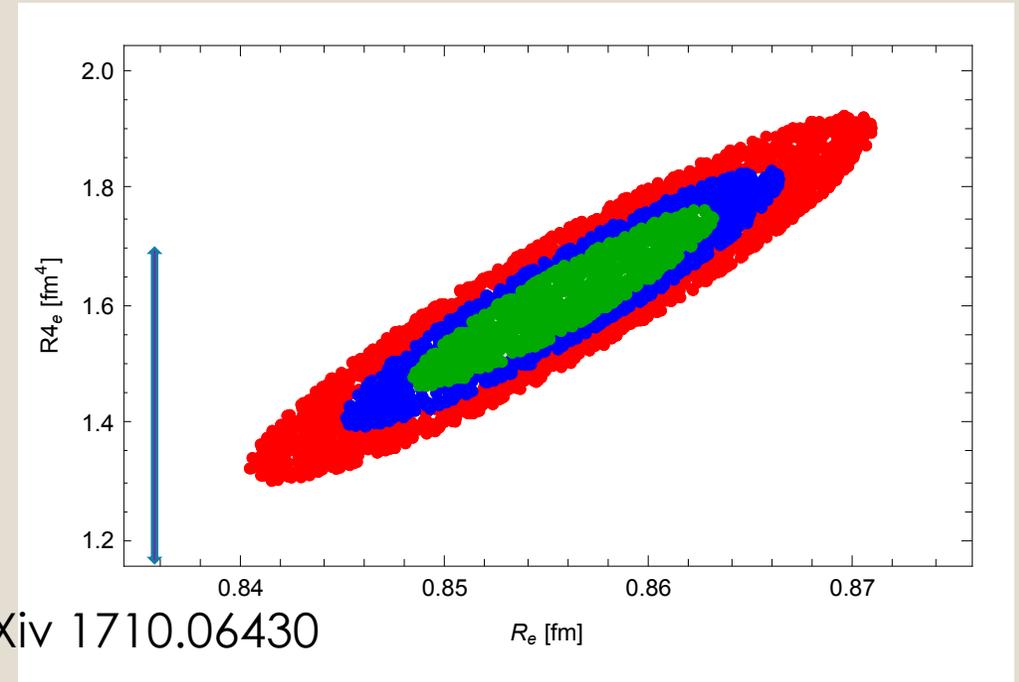
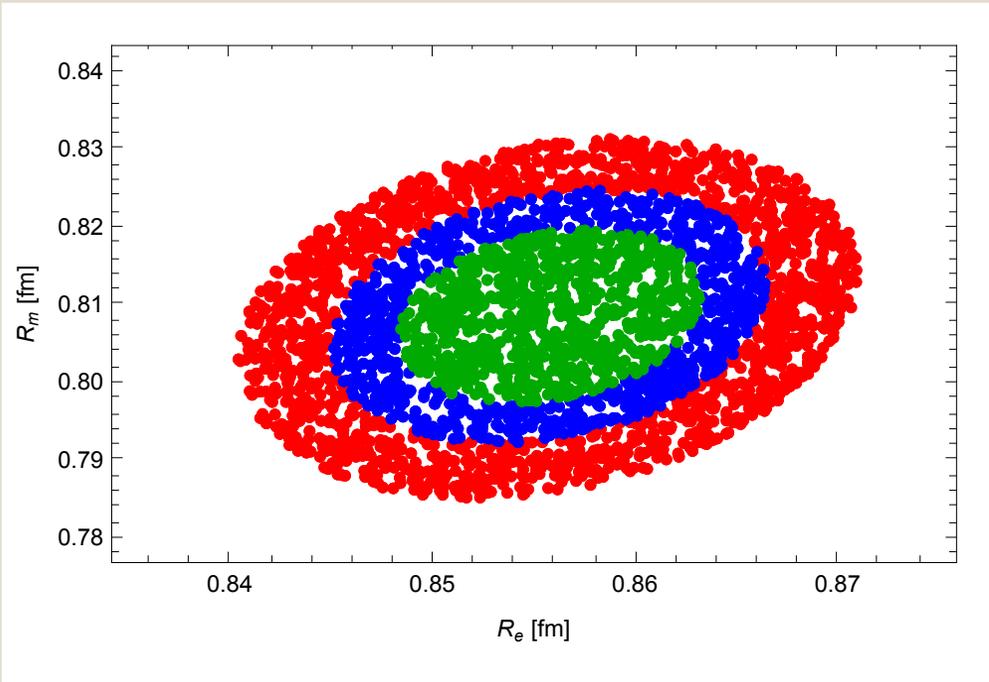
We can fix that using conformal mapping

Moment expansion equals semi-analytic answer to high accuracy out to reasonable  $Q^2 = -t$ !

# Testing fits up to moderate $Q^2_{\max}$

- Situation: Effective theory predictions: nothing useful on charge radius, rather small quartic moment, smallish magnetic radius.
- Thus: attempt fits where  $R_p=R_e$  and  $R_m$  float, as well as  $\langle r^4 \rangle_e$  with sampling of  $\langle r^6 \rangle_e$  and  $\langle r^4 \rangle_m$  in an extended range compared to predictions. Show reduced chi-squared for three-parameter fits with chosen  $\langle r^6 \rangle_e$  and  $\langle r^4 \rangle_m$  and observe correlations.
- If we went for the minimum chi-squared in these, then we'd do a total 5-parameter fit
- Higher moments up to order 20 are used as the central-value predictions. Without that, no reasonable function out to  $Q^2_{\max} = 0.2 \text{ GeV}^2$ .
- Note: we are forced to expand beyond the predictions for  $\langle r^6 \rangle_e$  and  $\langle r^4 \rangle_m$ , but not by too much.
- We use heavy-baryon effective theory including as degrees:  $\pi$ ,  $p$ , and the  $\Delta$ . (by C. Peset and A. Pineda)

$(Q_{\max}^2 = 0.2 \text{ GeV}^2) \chi_{\text{red}}^2$  : green < 1.08, blue < 1.10, red < 1.14



J.A & C.W arXiv 1710.06430

Is lowest reduced chi-squared  $\chi_{\text{red}}^2$  the answer?

If not, why not?

Are there systematic problems with the MAMI data?

Clearly: P&P prediction  $0.6(3) = \text{No Go}$

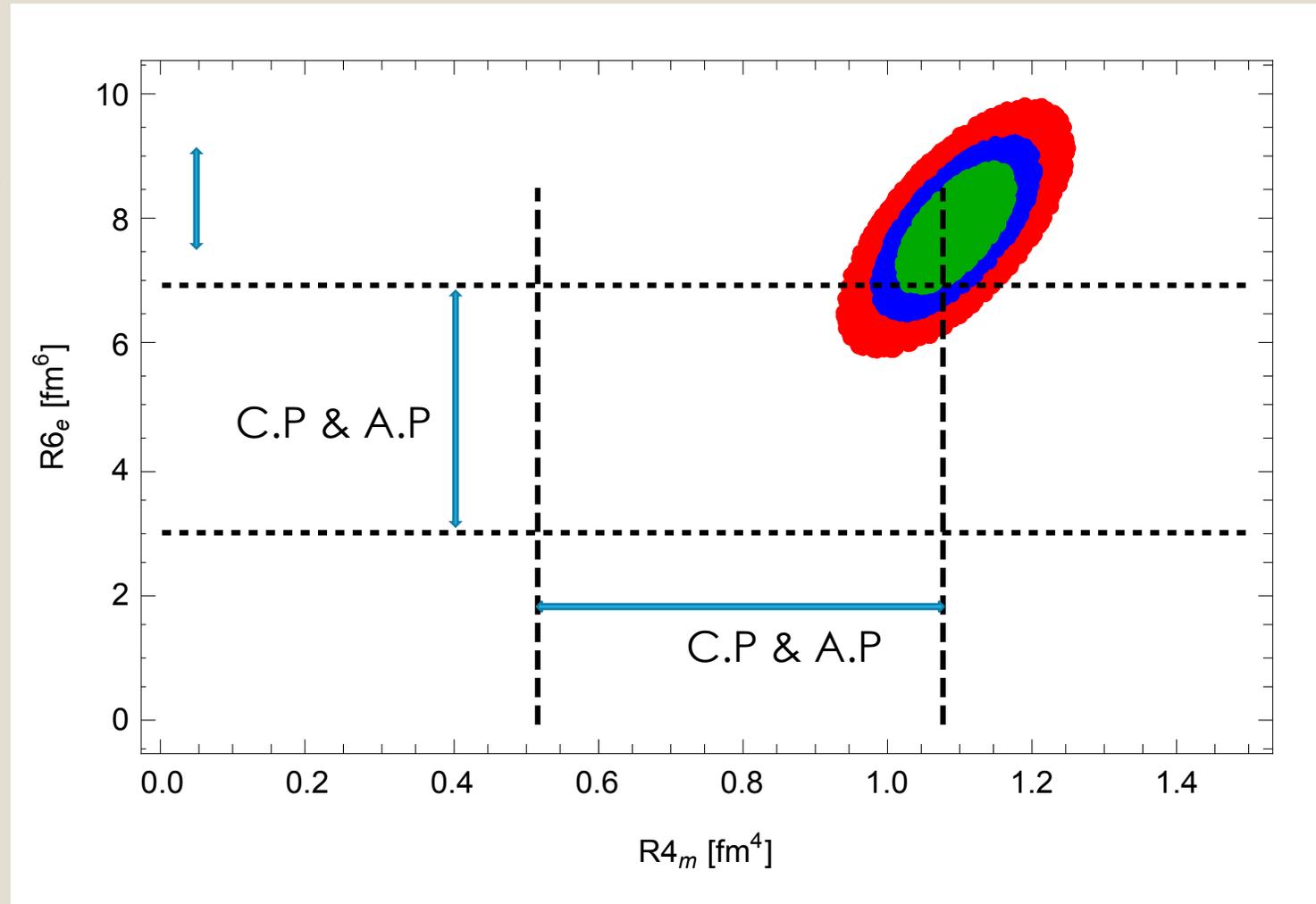
I. Sick & D. Trautmann:  $2.01(5)$  PRC 2017

M. Distler:  $2.6 \text{ fm}^4$

Note the  $R_e$  vs  $\langle r^4 \rangle_e$  correlation !!

Is it consistent for the higher moments ?

J.A & C.W arXiv 1710.06430



# Strategy: use 'χPT+' (J.Alarcón & C.Weiss) with a trick:

- Turn moment expansions into fit functions:

here is how:

Given a max.  $Q^2$  (here 0.2, dashed line):  
Spread the data in the conformal range  
Power series about  $\zeta=0$ .  $\zeta$  = generalized  $z$ .

Use predicted moments (up to 10<sup>th</sup> order in  $\zeta$ )

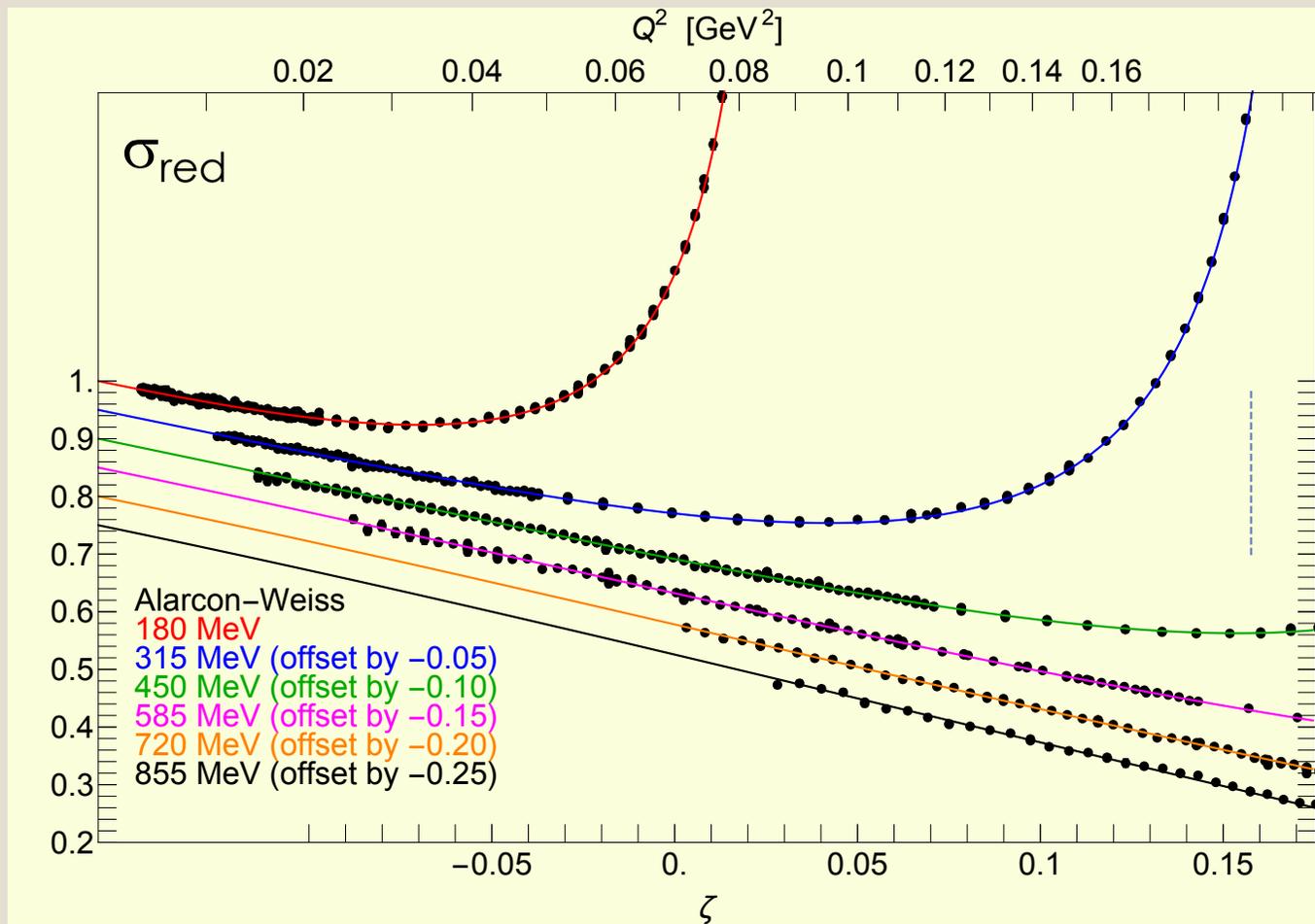
Replace the lowest-order moments by fit parameters (here a 4-parameter fit)

Fit works for some range above max.  $Q^2$ .

Reduced chi-squared of 1.08 here

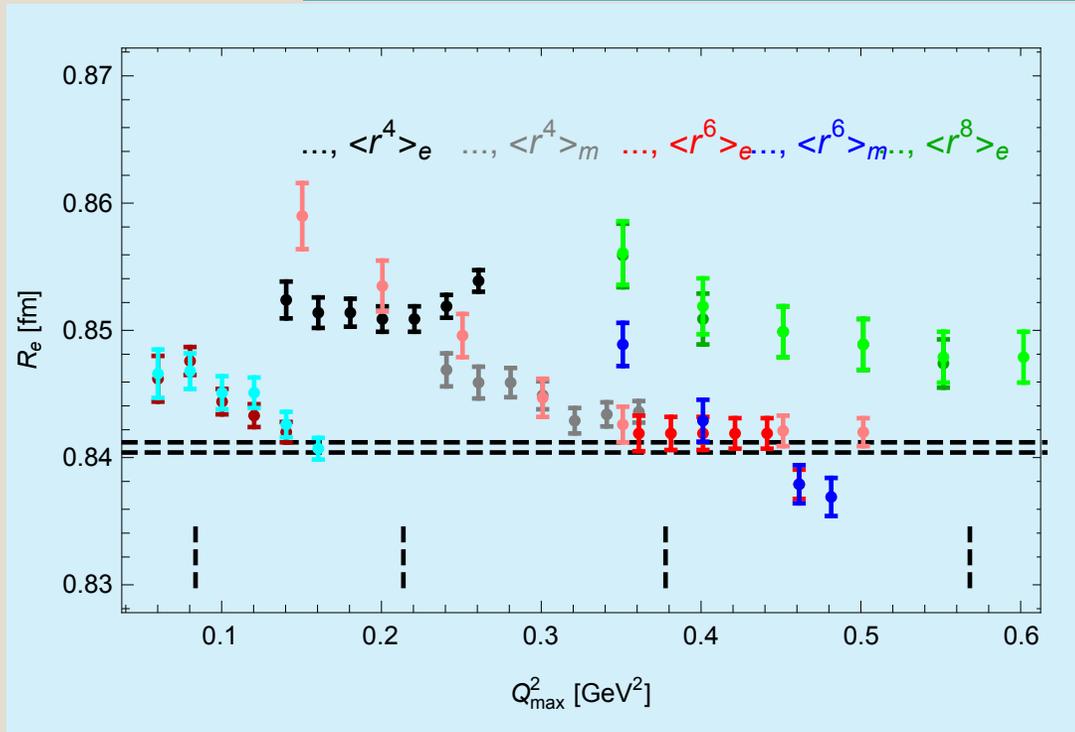
Good sensitivity to magnetic effects. Why?

To go to higher max.  $Q^2$  we need more predictions replaced by fit parameters

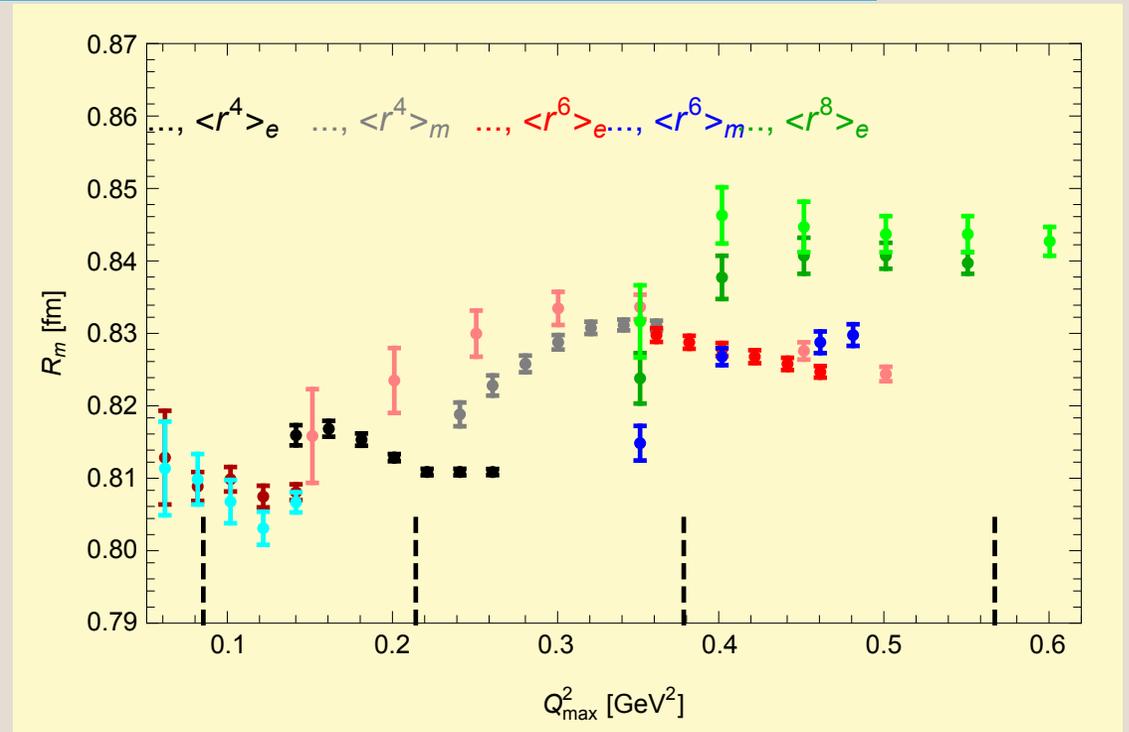


# Fits with 2, 3, 4, 5, 6, 7 parameters (& up to 31 norms)

Electric Radius:



Magnetic Radius:

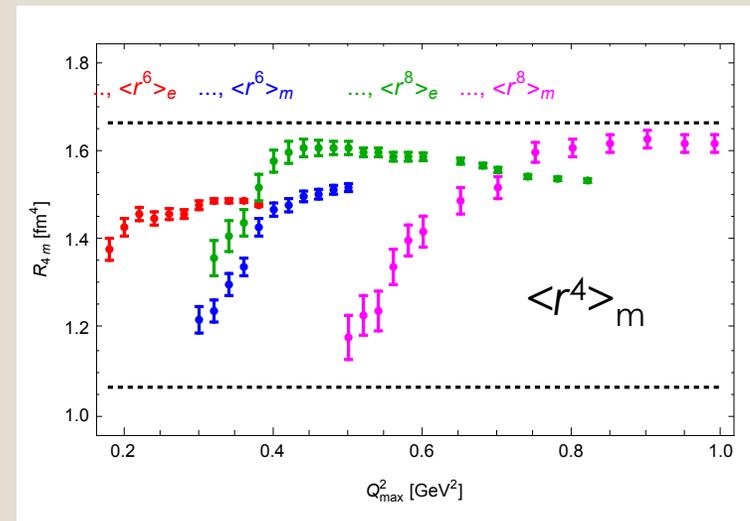
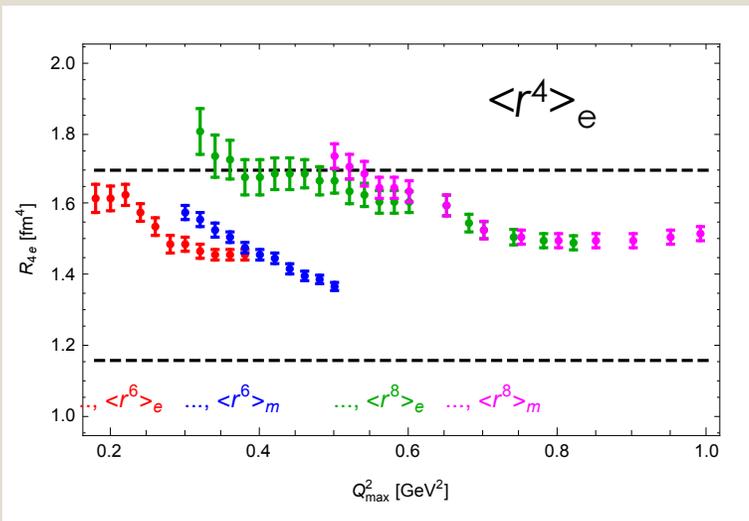


Errors shown are statistical (fit) errors; systematic errors due to predicted moment uncertainties can be inferred from the jump in value when a relevant parameter is added (electric vs magnetic)

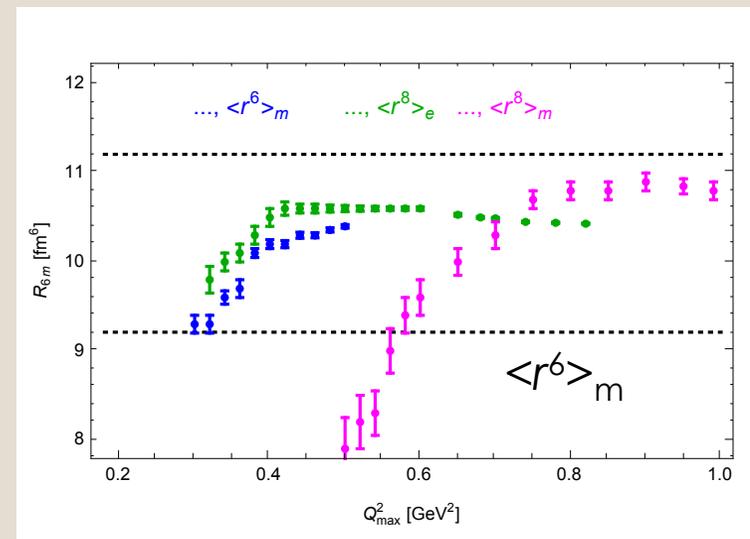
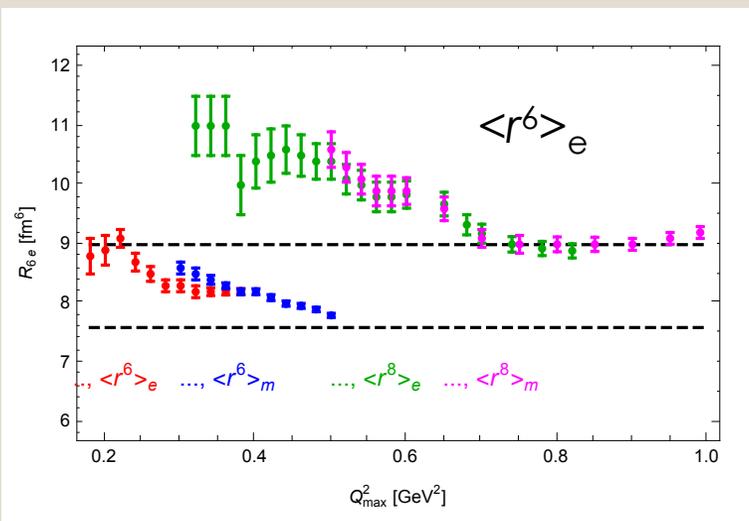
Fits tend towards **small** ( $\mu$ H) radius value when the dust settles! (blue? – no gain in fit quality)

Magnetic radius of  $\sim 0.82(1)$  fm is **higher** than the MAM analysis of  $0.80(2)$  fm (2014 with TPE)

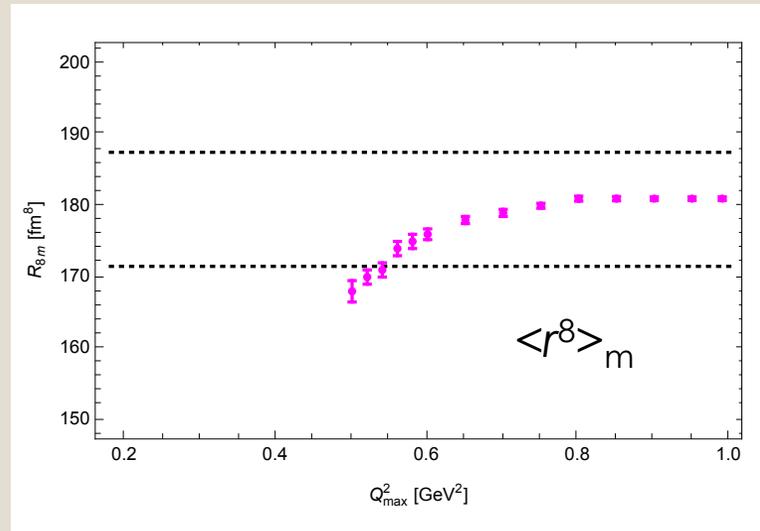
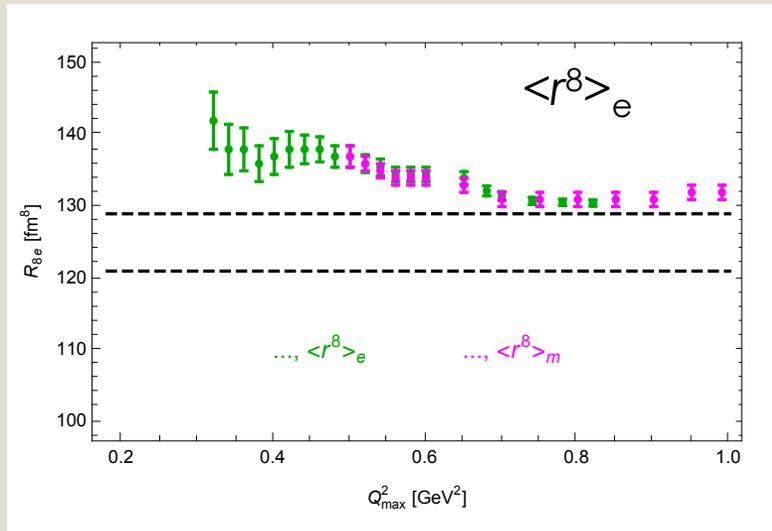
# Electric moments (arXiv 1710.06430), magnetic (private c., with uncertainties assumed $\geq$ to electric by MH)



Consistency between predicted ranges and fit findings?



# The highest 'determined' moments



What have we done ?

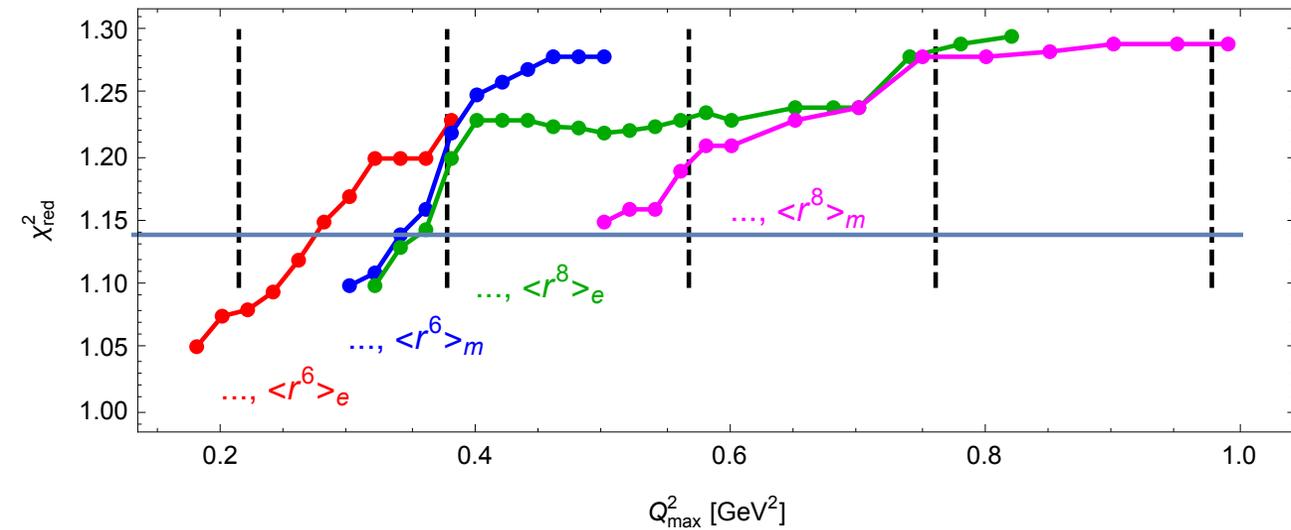
Used theory to yield constraints on the large- $Q^2$  behavior of the form factors.

Used the only parameters relevant in the given  $Q^2$  range.

Used a physics constraint ( $\pi$ - $\pi$  threshold in analytic continuation of the FFs).

So, is there any **bad news** ?

# Reduced chi-squared is – perhaps - the bad news!



The MAMI fitters are told to stay below 1.14 - line.

This 1.14 is an admission of problems,  
For 1422 data points it shouldn't happen.

Now, what if the MAMI troubles are systematic?

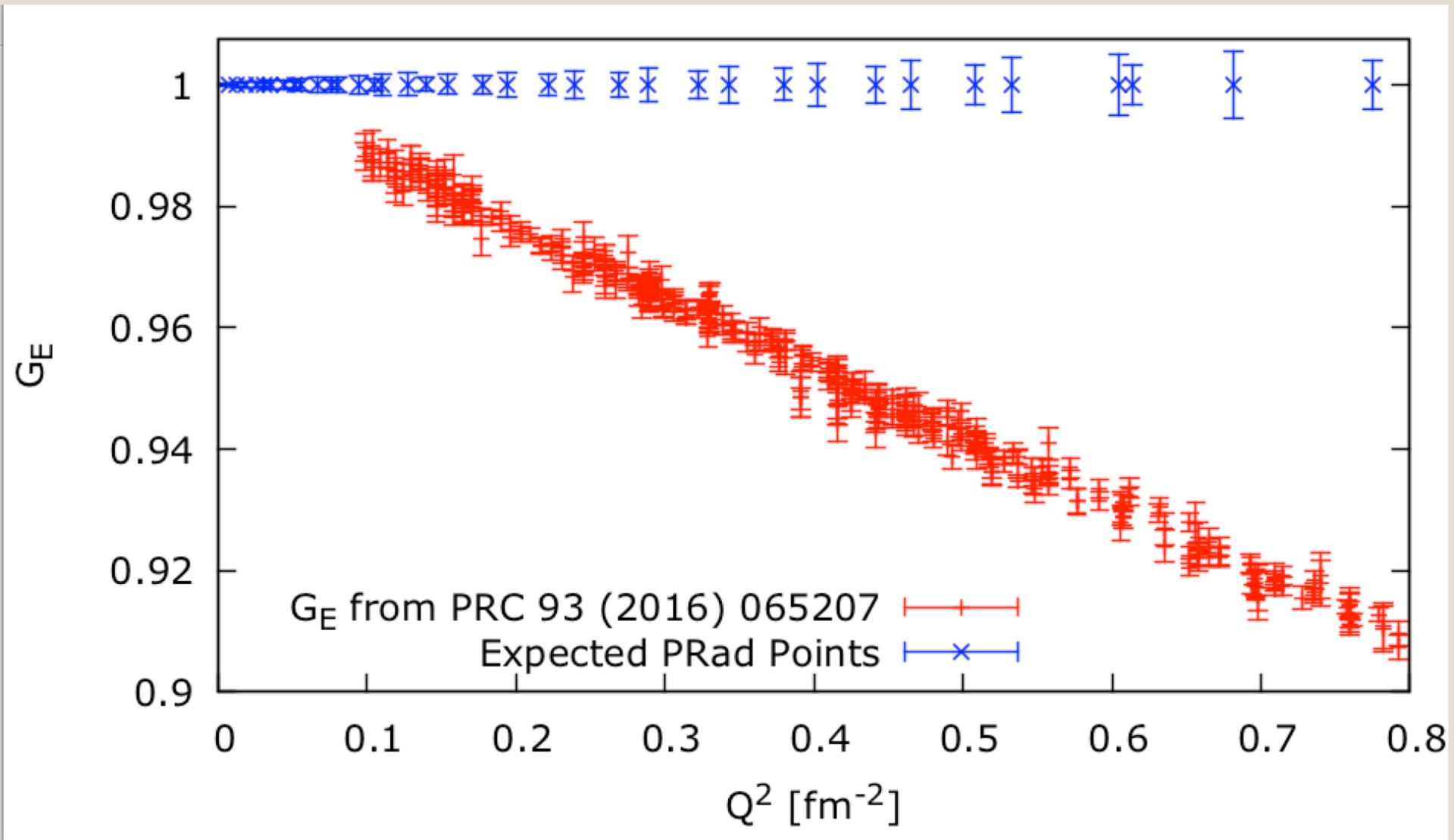
Our analysis: a value of 1.23 for  $Q^2_{\max} < 0.74$  is OK.  
The blue curve is worse (last 6 points, i.e., reject).  
Is  $\chi^2$  a  $1/\varepsilon$  problem??

The MAMI fitters (including ourselves in the past) have managed to achieve 1.14 over the entire data set by using 12 parameters per form factor = 24 parameters. Are these fits just fighting some systematic errors when  $\varepsilon$  goes small? (at the dashed lines)

7% error vs 14% (Jan's vs our guess)

The future will tell. The weaving is in the MAMI data (from Rosenbluth separations!),  $G_e$  and  $G_m$  swing a couple of times - is this physics? If so, what physics?

# Expected Precision of PRad Data



At this point, the community is split.

0.84 fm

0.88 fm



**New electron scattering (PRAD), muon-electron scattering (MUSE), and atomic experiments coming!**

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