# **Status of the Proton Radius Puzzle**

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\* Supported by NSF PHY-1436680, PHY-1505934, and DOE DE-SC0012589 and DE-SC0013941

### **PSI muonic hydrogen measurements**

• 2010: R. Pohl et al., Nature 466, 09259 (2010): 2S $\Rightarrow$ 2P Lamb shift  $\Delta E(meV) = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \Rightarrow r_p = 0.84184 \pm 0.00067 \text{ fm}$ 

Possible issues: atomic theory & proton structure

 2013: A. Antognini et al., Science 339, 417 (2013): 2S⇔2P Lamb + 2S-HFS ΔE<sub>L</sub>(meV) = 206.0336(15) - 5.2275(10)r<sub>p</sub><sup>2</sup> + 0.0332(20)<sub>TPE</sub> ⇔r<sub>p</sub> = 0.84087±0.00039 fm



#### R. Pohl et al., Nature 466, 09259 (2010)

# Buly 2010 www.sature.com/nature 510 THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE

OIL SPILLS There's more to come PLAGIARISM It's worse than

you think CHIMPANZEES The battle for survival

#### SHRINKING THE PROTON New value from exotic atom

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#### **April 2013** ASSOCIATION OF ASIA PACIFIC PHYSICAL SOCIETIES 8 July 2010 | www.nature.com/nature | \$10 Volume 23 Number 2 APRIL 2013 Bulletin **Proton Size Puzzle Reinforced OIL SPILLS** From being lars There's more to come PLAGIARISM It's worse than you think Overether the CHIMPANZEES The battle for Title ow tax survival TOBA amplifiar Banda Isla 155M0210 2203 Feature Articles **Activities and Research News** Institutes in Asia Pacific Neutrino Oscillation and Proton Size Puzzle Reinforced \* Department of Physics' Mixing Yonsei University Asia Pacific School/Workshop: \* Status and Prospect on Gravitation and Cosmology \* Elepartment of Physics NATURE of Telescope Array 2013 at Korea University hers for hire Experiment

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#### July 2013

INSIDE THE NEANDERTHAL BRAIN First hints of how their minds differed from ours ASS 8 July 2010 | www.nature.com/nature | \$10 ewScientist II. WEEKEY July 20 - 26, 2013 Vol **OIL SPILLS** There's more to come PLAGIARISM It's worse than you think CHIMPANZEES The battle for survival CAR HACKING Could cyberattackers arrange a crash? No2935 UESS.95 CANSI.95 LONG STORY How the Diplodocus got its neck EVOLUT Feature Articles. Acti WINDS OF CHANGE It works differently if you're small Neutrino Oscillation and · Pro Gale-force warnings Mixing + 651 from Antarctica id technology news www.newscientist.com US jobs in science Status and Prospect. **D**D NATURE of Telescope Array 20 thers for hire Experiment THE REPORT OF THE REPORT OF THE

January 2014





# The proton radius puzzle

- >7σ (4%) discrepancy between muonic and electronic measurements
- High-profile articles in Nature, NYTimes, etc.
- Puzzle unresolved, possibly New Physics





#### The proton radius puzzle in 2013

The proton rms charge radius measured with electrons:  $0.8770 \pm 0.0045$  fm (CODATA2010+Zhan et al.) muons:  $0.8409 \pm 0.0004$  fm



## **Possible resolutions to the puzzle**

- The ep (scattering) results are wrong
   Fit procedures not good enough
   Q<sup>2</sup> not low enough, structures in the form factors
- The ep (spectroscopy) results are wrong Accuracy of individual Lamb shift measurements? Rydberg constant could be off by 5 sigma
- The µp (spectroscopy) result is wrong Discussion about theory and proton structure for extracting the proton radius from muonic Lamb shift measurement
- Proton structure issues in theory

Off-shell proton in two-photon exchange leading to enhanced effects differing between  $\mu$  and e Hadronic effects different for  $\mu p$  and ep: e.g. proton polarizability (*effect*  $\propto m_l^4$ )

 Physics beyond Standard Model differentiating µ and e Lepton universality violation, light massive gauge boson Constraints on new physics e.g. from kaon decays

#### New measurements are on their way

#### Additional measurements needed / in preparation / done

- Spectroscopy with  $\mu$ D,  $\mu$ He, and regular H; Rydberg constant
- ep-, ed-scattering (PRad at Jlab, ISR-ep and ed elastic at MAMI; MESA)
- µ±p- and e±p-scattering in direct comparison at PSI (MUSE)
- Searches for lepton universality violating light bosons (e.g. kaon decays such as TREK/E36 at J-PARC)

r <sub>p</sub> (fm)	ер	μρ	
Spectroscopy	0.8758 ± 0.077	0.84087 ± 0.00039	
Scattering	0.8770 ± 0.060 ???		

Need more precision for extraction from scattering More insights from comparison of ep and µp scattering

#### Workshop series: Trento 2012+2016; Mainz 2014



Castello di Trento ("Trint"), watercolor 19.8 x 27.7, painted by A. Dürer on his way back from Venice (1495). British Museum, London

#### The proton radius puzzle

Trento, June 20 - 24, 2016

#### **Main Topics**

The proton radius puzzle and beyond: Structure of the lightest nuclei, Laser spectroscopy of light muonic atoms and ions Precision spectroscopy of regular atoms, Electron scattering, Nuclear polarizability, two-photon exchange Beyond-Standard-Model solutions of the proton radius puzzle

#### Speakers

Jan C. Bernauer, (MIT, USA), Carl E. Carlson, (William & Mary, USA), Kjeld S.E. Eikema, (LaserLAB Amsterdam, The Netherlands), Eric A. Hessels, (York University; Toronto, Canada), Michael Kohl, (Hampion U. J. Jeffston Lab, USA), Krzyztof Pachukak, (University of Warsaw, Poland), Gil Paz, (Wayne State University, USA), Ingo Sick, (University of Based, Switzerland), Vladimir A. Yerokhin, (Center for Advances Studies, St. Petersburg, Russia)

#### Organizers

Carlos Bertulani (*Texas A&M University-Commerce*) carlos.bertulani@tamuc.edu Guillaume Blanchon (*CEA - DAM - DIF*) guillaume.blanchon@cca.fr Gregory Potel (*Lawrence Livermore National Laboratory*) potel@nscl.msu.edu Vittorio Soma (*CEA Saclay*) vittorio.soma@cca.fr



Director of the ECT\*: Professor Jochen Wambach (ECT\*)

The ECT\* is sponsored by the "Fondazione Bruno Kessler" in collaboration with the "Assessorato alla Cultura" (Provincia Autonoma di Trento), funding agencies of EU Member and Associated States and has the support of the Department of Physics of the University of Trento.

For local organization please contact: Gianmaria Ziglio - ECT\* Secretariat - Villa Tambosi - Strada delle Tabarelle 286 - 38123 Villazzano (Trento) - Italy Tel.:(+39-0461) 314721 Fax:(+39-0461) 314750, E-mail: ect@ectstar.eu or visit http://www.ectstar.eu



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# Trento workshop June 20-24, 2016

#### 2nd ECT\* Workshop on the Proton Radius Puzzle

June 19-25, 2016 Trento, Italy Version 2

Sunday, June 19, 20:00: Pizza Dinner

Time	Monday June 20	Tuesday June 21	Wednesday June 22	Thursday June 23	Friday June 24	
9:00 - 10:30	(9:30) Ron, Jerry, Randolf (10) Welcome	<b>Gerald A. Miller</b> (35+10) Electrophobic Scalar Boson and Muonic Puzzles	<b>Eric A. Hessels</b> (35+10) Determining the Proton Charge Ra- dius from Electron-Proton Scat- tering and from Hydrogen Spec- troscopy	Marc Diepold (35+10) News from muonic Helium: Theory status and results	Toshimi Suda $(35+10)$ $e+p$ project at ultra-low $Q^2$ inJapan	
	Julian Krauth (35+10) Muonic deuterium	John Ralston (35+10) The Muon Experimental Anomalies Are Explained by a New Interaction Proportional to Charge	<b>Kjeld S.E. Eikema</b> $(35+10)$ Precision deepUV Ramsey-comb spectroscopy of $H_2$ and prospects for 1S-2S excitation of He-ions	<b>Chen Ji</b> (35+10) Nuclear Structure Contributions to Lamb shift in Light Muonic Atoms	Ashot Gasparian (35+10) The PRad Experiment at Jefferson Lab	
10:30 - 11:00	coffee break					
11:00 - 12:30	<b>M. Mihoviloviĉ</b> (35+10) The Initial state radiation experi- ment at MAMI	<b>Krzysztof Pachucki</b> (35+10) Toward the absolute nuclear charge radius determination from the spec- tra of light atomic and molecular systems	Joan M. Dreiling (35+10) Progress Towards Generating Ryd- berg State, One-Electron Ions	<b>Carl E. Carlson</b> (35+10) Two-photon exchange corrections to the Lamb shift in muonic helium	<b>Randolf Pohl</b> (35+10) CREMA++: Future experiments with muons, and more	
	Ingo Sick (35+10) Proton rms-radius: recent determi- nations from (e,e)	<b>V.A. Yerokhin</b> (35+10) Nuclear recoil effect in the Lamb shift of hydrogen and light hydrogen-like ions	<b>Lothar Maisenbacher</b> (35+10) Precision spectroscopy of the 2S-4P transition in atomic hydrogen	<b>Antonio Pineda</b> (35+10) The Lamb shift in muonic hydrogen and the proton radius from effective field theories		
12:30 - 14:30	lunch break					
14:30 - 16:00	<b>Jan C. Bernauer</b> (35+10) Why I believe that proton scattering gives a big radius	<b>Excursion</b> Ferrari Spumante Cellars	Michael Kohl (35+10) TREK/E36 @ J-PARC: Investigat- ing lepton universality with stopped kaon decays	Gil Paz (35+10) Addressing the Proton Radius Puz- zle Using QED-NRQED Effective Field Theory		
	<b>Douglas Higinbotham</b> (35+10) Statistical Modeling of Electron Scattering Data		<b>Andrea Vacchi</b> (35+10) Muonic hydrogen ground state hy- perfine splitting - towards the high precision measuremen	<b>Franziska Hagelstein</b> (35+10) Proton Structure in the Hyperfine Splitting of Muonic Hydrogen		
16:00 - 16:30	) coffee break					
16:30 - 18:00	<b>Evangeline Downie</b> (35+10) <i>MUSE Overview</i>		Savely Karshenboim (35+10) t.b.a	Discussions		
	Discussions		Discussions			

## The proton radius puzzle in 2016

The proton rms charge radius measured with electrons: 0.8751 ± 0.0061 fm (CODATA2014) muons: 0.8409 ± 0.0004 fm



Lorenz, Hammer, Meissner EPJ A 48, 151 (2012)



# There is a deuteron radius puzzle: 7.5 $\sigma$ between r<sub>d</sub> (µD) and CODATA-2010

### **Muonic Helium-4**



Muonic Helium-4 results constrain parameter space of new physics and (un)conventional hadronic physics (Muonic Helium-3 theory (polarizability) still being developed)

#### **Atomic hydrogen spectroscopy (2016)**



#### Mainz ep scattering at low Q<sup>2</sup>



# **Proton radius from Mainz A1 data**



- Low Q<sup>2</sup> J. Bernauer et al., PRL105 (2010) 242001; PRC90, 015206 (2014)
- Left: world + Mainz fit; Middle: Mainz raw data; Right rebinned GE
- Large difference in slope between r = 0.84 and 0.88 fm
- Floating normalization, higher-order Q<sup>2</sup> terms present
- Controversies about radius extraction dependence on fit model
- Need yet higher precision

# **Controversy about scattering results**

- Recently, radius extractions from same scattering data have been controversial
- Group 1: Bernauer, Distler, Sick: large radius ~0.88 fm J.C. Bernauer and M. Distler, arXiv:1606.02159v1 [nucl-th]
   I. Sick, Progress in Particle and Nuclear Physics 67, 473 (2012)
  - Importance of corrections Q<sup>4</sup> and Q<sup>6</sup> even at low Q<sup>2</sup> ~ 10<sup>-3</sup> (GeV/c)<sup>2</sup> which affect cross section at the 15% level
  - Linear fits (like all polynomial or Taylor expansions) give biased result
  - Need large Q<sup>2</sup> range to determine higher order terms, these affect low-Q<sup>2</sup>
- Group 2: Griffioen, Carlson, Higinbotham: small radius ~0.84 fm D.W. Higinbotham et al., Phys. Rev. C93, 055207 (2016), arXiv:1510.01293 [nucl-ex] K. Griffioen, C. Carlson, and S. Maddox, arXiv:1509.06676 [nucl-ex]
  - reduced Q<sup>2</sup> range and order of fit function
  - justifying significance with F-tests etc.

 Horbatsch & Hessels: can produce any radius 0.84-0.88 fm depending on fit function and range. Get small radius even over full Q<sup>2</sup> range fit, however fit function is biased
 M. Horbatsch and E. A. Hessels, Phys. Rev. C93, 015204 (2016), arXiv:1509.05644 [nucl-ex]

- VMD fits are biased, too (small radius)
   I.T. Lorenz, U.-G. Meißner, H.W. Hammer, and Y.B. Dong, Phys. Rev. D 91, 014023 (2015)
- Perhaps most realistic is the z-expansion with realistic physics constraints for convergence (= large radius!)
   R.J. Hill and G. Paz, Phys. Rev. D 82, 113005 (2010)
   G. Lee, J.R. Arrington, and R.J. Hill, Phys. Rev. D 92, 013013 (2015)

# The PRad proton radius proposal (JLAB)





- Low intensity beam in Hall B @ Jlab into windowless gas target
- Scattered ep and Moller electrons into HYCAL at 0°
- Lower Q<sup>2</sup> than Mainz. Very forward angle, insensitive to 2γ, G<sub>M</sub>
- Conditionally approved by PAC38 (Aug 2011): "Testing of this result is among the most timely and important measurements in physics."
- Approved by PAC39 (June 2012), graded "A"
- Running in Hall B in May-June 2016 (completed)

# Initial state radiation (ISR) at MAMI

Radiative tail dominated by coherent sum of two Bethe-Heitler diagrams



- In data ISR can not be distinguished from FSR
- Combining data and simulation, ISR and form factor can be extracted
- Q<sup>2</sup> (Reconstructed) > Q<sup>2</sup> (Vertex for ISR)
- Idea behind new MAMI experiment to extract G<sub>E</sub><sup>p</sup> at lowest Q<sup>2</sup> ~ 10<sup>-4</sup> (GeV/c)<sup>2</sup>
- Method tested at higher Q<sup>2</sup>

Data taken in 2014, under analysis, bgd. systematics limited, new ISR planned

# A light boson and the proton radius puzzle

#### Jaeckel, Roy (arXiv:1008.3536)

 Hidden U(1) photon can decrease charge radius for muonic hydrogen, however even more so for regular hydrogen

#### Tucker-Smith, Yavin (arXiv:1011.4922) can solve proton radius puzzle

 MeV particle coupling to p and µ (not e) consistent with g<sub>µ</sub>-2

#### Batell, McKeen, Pospelov (arXiv:1103.0721): can solve proton radius puzzle

- new e/µ differentiating force consistent with gµ-2
- <100 MeV vector or scalar gauge boson V (poss. dark photon)</p>
- resulting in large PV µp scattering

#### Carlson, Rislow (arXiv:1310.2786): can solve proton radius puzzle

- new e/µ differentiating force consistent with gµ-2
- Two fine-tuned scalar/pseudoscalar or vector/axial gauge bosons

#### Liu, McKeen, Miller (arXiv:1605. 04612): can solve proton radius puzzle

• Electrophobic scalar boson consistent with  $g_{\mu}$ -2

#### Barger, Chiang, Keung, Marfatia (arXiv:1109.6652):

- Light bosons constrained by  $K \to \mu \nu$  decay



# Search for a new particle in $K^+ \rightarrow \mu^+ v e^+ e^-$



(universality-violating, fine tuned);  $\Gamma(K^+ \rightarrow \mu^+ v A') \sim 10^{-6} - 10^{-5}$ 

#### HUGE signals predicted, J-PARC TREK/E36 stringent test

# Motivation for µp scattering



# Lepton scattering and charge radius



Sachs form factors:

$$G_E(Q^2) = F_1(Q^2) - \tau F_2(Q^2)$$
  

$$G_M(Q^2) = F_1(Q^2) + F_2(Q^2)$$

Fourier transform (in the Breit frame) gives spatial charge and magnetization distributions

#### Derivative in $Q^2 \rightarrow 0$ limit:

$$\begin{split} \left| \left\langle r_E^2 \right\rangle &= \left. -6 \frac{dG_E^p(Q^2)}{dQ^2} \right|_{Q^2 \to 0} \\ \left\langle r_M^2 \right\rangle &= \left. -6 \frac{dG_M^p(Q^2)/\mu_p}{dQ^2} \right|_{Q^2 \to 0} \end{split}$$

#### Expect identical result for ep and µp scattering

#### Lepton scattering and charge radius



Expect identical result for ep and µp scattering

# **MUon Scattering Experiment (MUSE) at PSI**

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Use the world's most powerful low-energy separated  $e/\pi/\mu$  beam for a direct test if  $\mu p$  and ep scattering are different:

- to higher precision than previously
- in the low Q<sup>2</sup> region, similar to Mainz (Bernauer) and JLab (Zhan) for sensitivity to radius

measure both µ<sup>±</sup>p and e<sup>±</sup>p for direct comparison and robust, convincing result
depending on the results, 2nd generation experiments (lower Q<sup>2</sup>, µ<sup>±</sup>n,D,He, higher Q<sup>2</sup>, ...) might be desirable

# **MUon Scattering Experiment (MUSE) at PSI**

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Use the world's most powerful low-energy separated  $e/\pi/\mu$  beam for a direct test if  $\mu p$  and ep scattering are different:

- Simultaneous, separated beam of  $(e^{+}/\pi^{+}/\mu^{+})$  or  $(e^{-}/\pi^{-}/\mu^{-})$  on liquid H<sub>2</sub> target
- $\rightarrow$  Separation by time of flight
- $\rightarrow$  Measure absolute cross sections for ep and µp
- $\rightarrow$  If radii differ by 4%, then form factor slope by 8%, x-section slope by 16%
- $\rightarrow$  Measure e+/µ+, e-/µ- ratios to cancel certain systematics
- Directly disentangle effects from two-photon exchange (TPE) in e+/e-, μ+/μ-
- Multiple beam momenta 115-210 MeV/c to separate G<sub>E</sub> and G<sub>M</sub> (Rosenbluth)

#### **πM1 / MUSE beamline**



- πM1: 100-500 MeV/c Momentum selective RF+TOF separated π, μ, e
- Limited beam flux (5 MHz)
   → Large angle, non-magnetic
  - detectors to detect leptons
- Secondary beam
  - $\rightarrow$  Tracking of beam particles to target
- Mixed beam
  - → Identification of beam particle in trigger

# **MUSE experiment layout**

- Beam particle tracking
- Liquid hydrogen target
- Scattered lepton detection

Measure e<sup>±</sup>p and µ<sup>±</sup>p elastic scattering p = 115, 153, 210 MeV/c  $\Theta$  = 20° to 100° Q<sup>2</sup> = 0.002 - 0.07 (GeV/c)<sup>2</sup>  $\epsilon$  = 0.256 - 0.94

- Challenges
- Secondary beam with π background
- Non-magnetic spectrometer
- Background from Møller scattering and muon decay in flight



#### **Mechanical assembly**



12 MUSE Test Runs to characterize piM1 beam to test detector prototypes (scintillators, Cerenkov, straw tubes) to study and optimize GEM performance •Oct 2012 May 2013 July 2013 Oct 2013 (Cosmics) Dec 2013 June 2014 Dec 2014 Feb 2015 (Cosmics) June-July 2015 Dec 2015 May 2016 June-July 2016 **Representation from 13 institutions** 

#### **First beam tests**



#### Beam spot with GEM – May 23, 2013





# **Projected sensitivity for MUSE**

- Cross sections to <1% stat. for backward μ, <<1% for e and forward μ Absolute 2%, point-to-point relative uncertainties few x10<sup>-3</sup>
- Individual radius extractions from e<sup>±</sup>, µ<sup>±</sup> each to 0.01 fm
- Compare e<sup>±</sup> xsecs and µ<sup>±</sup> xsecs for TPE. Charge-average to eliminate TPE.
- From e/μ xsec ratios: extract e-μ radius difference with minimal truncation error to 0.0045 fm or ~8σ (1st-order fits)
- If no difference, extract radius to 0.007 fm (2nd-order fit)



# **Projected sensitivity for MUSE**

- Charge radius extraction limited by systematics, fit uncertainties
- Many uncertainties are common to all extractions in the experiments: Cancel in e+/e-, μ+/μ-, and μ/e comparisons
- $R_e R_\mu = 0.034 \pm 0.006$  fm (5.6 $\sigma$ ), MUSE:  $\delta r = 0.0045$  fm (7.6 $\sigma$ )

**MUSE** suited to verify 5.6σ effect (CODATA2014) with even higher significance



# **MUon Scattering Experiment – MUSE**

#### 55 MUSE collaborators from 24 institutions in 5 countries:

A. Afanasev, A. Akmal, J. Arrington, H. Atac, C. Ayerbe-Gayoso, F. Benmokhtar,
N. Benmouna, J. Bernauer, A. Blomberg, E. Brash, W.J. Briscoe, E. Cline, D. Cohen,
E.O. Cohen, K. Deiters, J. Diefenbach, B. Dongwi, E.J. Downie, L. El Fassi, S. Gilad,
R. Gilman, K. Gnanvo, R. Gothe, D. Higinbotham, Y. Ilieva, L. Li, M. Jones, N. Kalantarians,
M. Kohl, G. Kumbartzki, J. Lichtenstadt, W. Lin, A. Liyanage, N. Liyanage, Z.-E. Meziani,
P. Monaghan, K.E. Mesick, P. Moran, J. Nazeer, C. Perdrisat, E. Piasetzsky, V. Punjabi,
R. Ransome, D. Reggiani, P.E. Reimer, A. Richter, G. Ron, T. Rostomyan, A. Sarty,
Y. Shamai, N. Sparveris, S. Strauch, V. Sulkosky, A.S. Tadepalli, M. Taragin, and L. Weinstein



George Washington University, Montgomery College, Argonne National Lab, Temple University, College of William & Mary, Duquesne University, Massachusetts Institute of Technology, Christopher Newport University, Rutgers University, Hebrew University of Jerusalem,, Tel Aviv University, Paul Scherrer Institut, Johannes Gutenberg-Universität, Hampton University, University of Virginia, University of South Carolina, Jefferson Lab, Los Alamos National Laboratory, Norfolk State University, Technical University of Darmstadt, St. Mary's University, Soreq Nuclear Research Center, Ieizmann Institute, Old Dominion University

# **MUon Scattering Experiment – MUSE**

- Proton Radius Puzzle still unresolved ~6 years later
- MUSE Experiment at PSI
  - Measure  $\mu p$  and ep scattering and compare  $\mu$ +/e+ and  $\mu$ -/e- directly
  - Measure e+/e- and µ+/µ- to study/constrain TPE effects

#### Technical Challenges

PID, timing, background rejection, momentum and flux determination

#### Timeline

- Initial proposal February 2012
- Technical review July 2012
- First beam tests in fall 2012
- PAC-approved in January 2013
- Further beam tests 2x yearly in summer and fall 2013–2016
  - Funding & construction 2016–2017
- Production running 2018–2019 (2x 6 months)

### **Summary and outlook**

- Proton Radius Puzzle still unresolved ~6 years later
- Substantial theoretical and experimental activity
- Numerous additional, high-quality experimental data expected in the next few years
   PRad, ISR, MUSE, TREK/E36, muonic atoms, regular hydrogen

"Until the difference between the ep and µp values is understood, it does not make sense to average the values together. For the present, we give both values. It is up to workers in this field to solve this puzzle." K.A. Olive et al. [Particle Data Group], Chin. Physics C 38, 090001 (2014)

 R<sub>P</sub> = 0.84087 ± 0.00026 ± 0.00029 fm
 [Muonic Hydrogen]

 A. Antognini et al., Science 339, 417 (2013)

 $R_P = 0.8775 \pm 0.0051 \, \text{fm}$ [CODATA2010]P.J. Mohr, B.N. Taylor, and D.B. Newell, Rev. Mod. Phys. 84, 1527 (2012) $R_P = 0.8751 \pm 0.0061 \, \text{fm}$ [CODATA2014]P.J. Mohr, D.B. Newell, and B.N. Taylor, arXiv:1507.07956v1 (2015)

# Backup