

2021. 12. 10

# **Gamma-ray Spectroscopy of Hypernuclei**

**Department of Physics, Tohoku University  
Advanced Science Research Center, JAEA**

**H. Tamura**

# Contents

**Introduction / Present status**

**Future experiments**

**$\Lambda\Sigma$  mixing and CSB**

**Baryon modification in nuclear medium**

**Medium/heavy hypernuclei for hyperon puzzle**

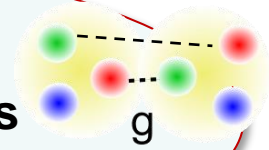
**Introduction /  
Present Status of  
 $\gamma$ -ray spectroscopy**

# Motivations of hypernuclear studies

**Hypernuclei** → **Scattering exp. for free YN int.**  
**Hypernuclei for YN int. in nuclear matter**

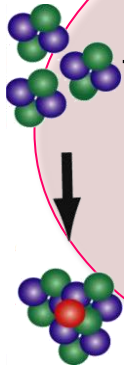
## BB interactions

Unified understanding of BB forces by  $u, d \rightarrow u, d, s$   
particularly short-range forces by quark pictures  
Test lattice QCD calculations



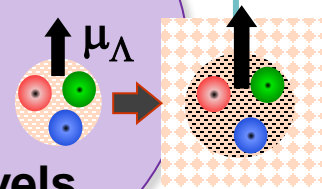
## Impurity effect in nuclear structure

Changes of size,  
deformation, clustering,  
Appearing new symmetry,  
...



## Properties and behavior of baryons in nuclei

$\mu_\Lambda$  in a nucleus  
 $\Lambda$ 's single particle levels  
Weak decays of  $\Lambda$  in nuclei

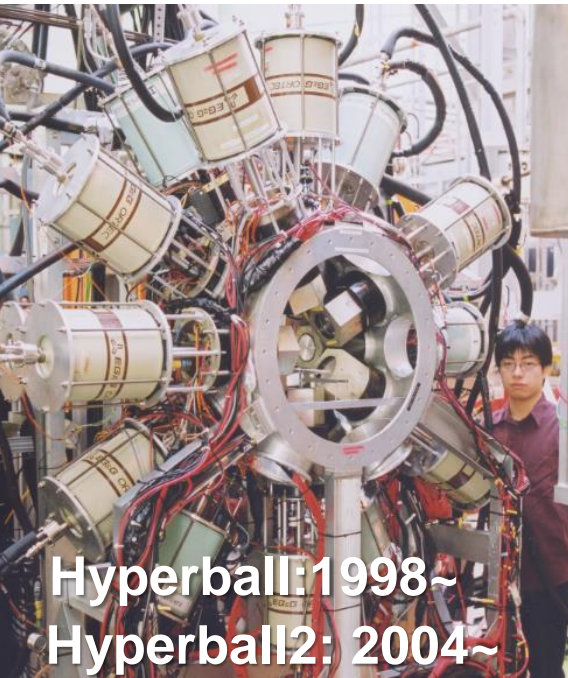


Clues to understand  
hadrons and nuclei  
from quarks

Cold and dense  
nuclear matter  
with strangeness

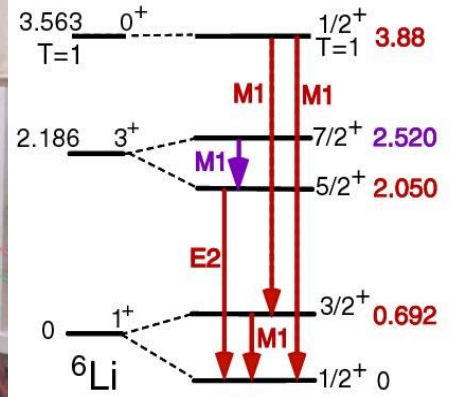


# Hypernuclear $\gamma$ -ray data (2015)



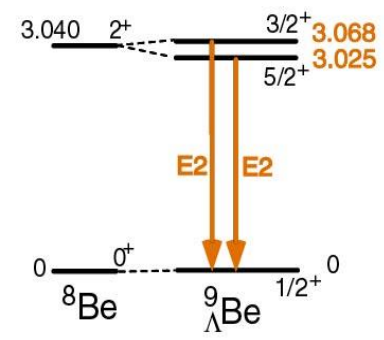
Hyperball: 1998~  
Hyperball2: 2004~

${}^7\text{Li} (\pi^+, K^+\gamma)$  KEK E419



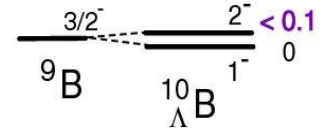
${}^7\text{Li}$  PRL 84 (2000) 5963  
PRL 86 (2001) 1982  
PLB 579 (2004) 258  
PRC 73 (2006) 012501

${}^9\text{Be} (K^-, \pi^-\gamma)$  BNL E930('98)



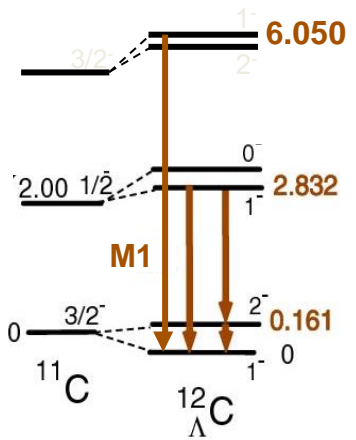
PRL 88 (2002) 082501  
NPA 754 (2005) 58c

${}^{10}\text{B} (K^-, \pi^-\gamma)$  BNL E930('01)



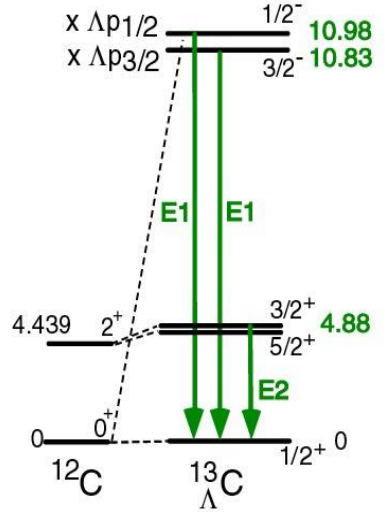
NPA 754 (2005) 58c

${}^{12}\text{C} (\pi^+, K^+\gamma)$  KEK E566



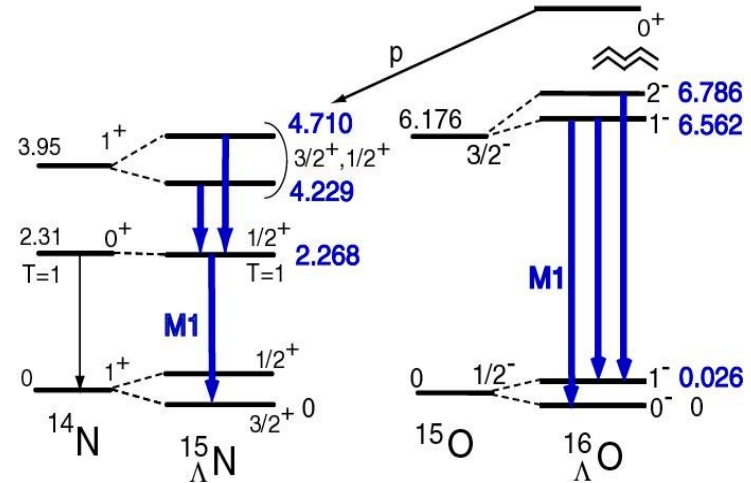
EPJ A33 (2007) 243  
PTEP (2015) 081D01

${}^{13}\text{C} (K^-, \pi^-\gamma)$  BNL E929 (NaI)



PRL 86 (2001) 4255  
PRC 65 (2002) 034607

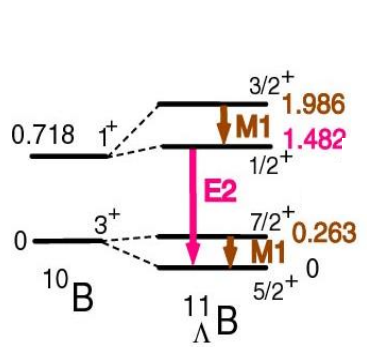
${}^{16}\text{O} (K^-, \pi^-\gamma)$  BNL E930('01)



PRC 77 (2008) 054315

PRL 93 (2004) 232501  
EPJ A33 (2007) 247

${}^{11}\text{B} (\pi^+, K^+\gamma)$  KEK E518



NPA 754 (2005) 58c

# Hypernuclear $\gamma$ -ray data (2015)

${}^7\text{Li} (\pi^+, K^+\gamma)$  KEK E419

${}^9\text{Be} (K^-, \pi^+\gamma)$  BNL E930('98)

${}^{10}\text{B} (K^-, \pi^+\gamma)$  BNL E930('01)

**$\Lambda\text{N}$  spin-dependent interaction strengths determined:**

$$V_{\Lambda\text{N}}^{\text{eff}} = V_0(r) + \underset{\Delta}{V_{\sigma}(r) \vec{s}_{\Lambda} \vec{s}_N} + \underset{S_{\Lambda}}{V_{\Lambda}(r) \vec{l}_{\Lambda\text{N}} \vec{s}_{\Lambda}} + \underset{S_N}{V_N(r) \vec{l}_{\Lambda\text{N}} \vec{s}_N} + \underset{T}{V_T(r) S_{12}}$$

$$\Delta = 0.33 (A > 10), 0.42 (A < 10), S_{\Lambda} = -0.01, S_N = -0.4, T = 0.03 \text{ MeV}$$

- Almost all p-shell levels are reproduced within a few 10 keV by this parameter set. (D.J. Millener)
- Feedback to BB interaction models. Nijmegen ESC08 model is almost OK for  $\Lambda\text{N}$ .
- Next step

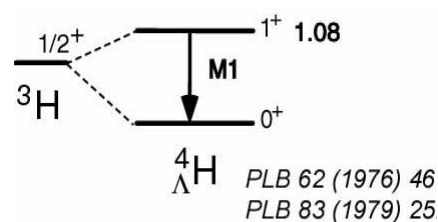
$\Lambda\text{N}$ - $\Sigma\text{N}$  force and CSB not understood  $\Rightarrow$  s-shell hypernuclei

$\Lambda\text{N}$  force in dense nuclear matter?  $\Rightarrow$  sd-shell (heavier) hypernuclei

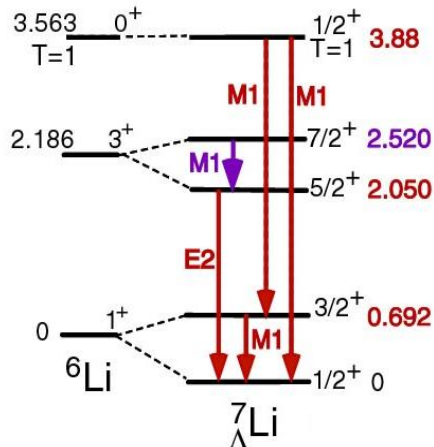


# Hypernuclear $\gamma$ -ray data (2019)

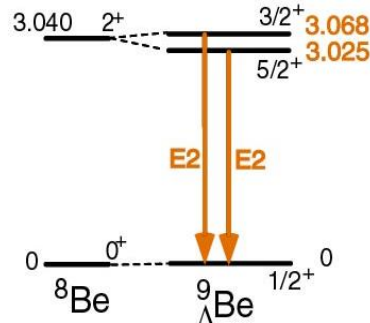
${}^7\text{Li}$  etc. ( $K^{\text{stop}}, \gamma \pi^-$ )



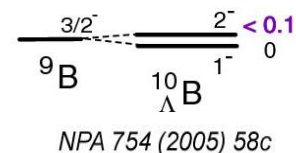
${}^7\text{Li}$  ( $\pi^+, K^+\gamma$ ) KEK E419



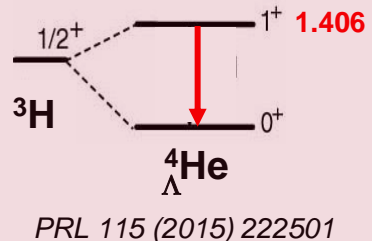
${}^9\text{Be}$  ( $K^-, \pi^-\gamma$ ) BNL E930('98)



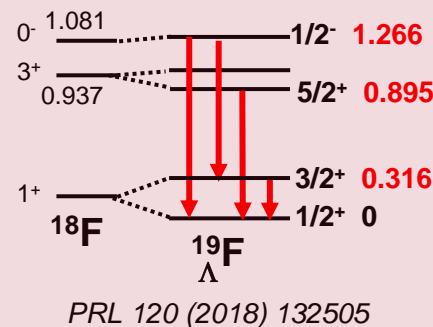
${}^{10}\text{B}$  ( $K^-, \pi^-\gamma$ ) BNL E930('01)



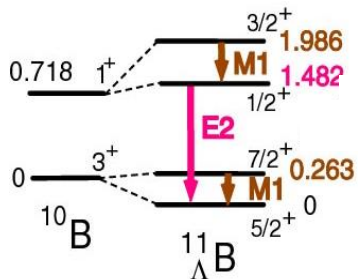
${}^4\text{He}$  ( $K^-, \pi^-\gamma$ ) J-PARC E13



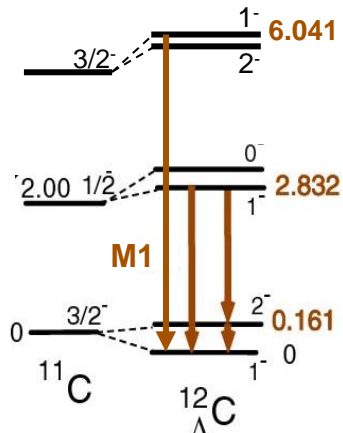
${}^{19}\text{F}$  ( $K^-, \pi^-\gamma$ ) J-PARC E13



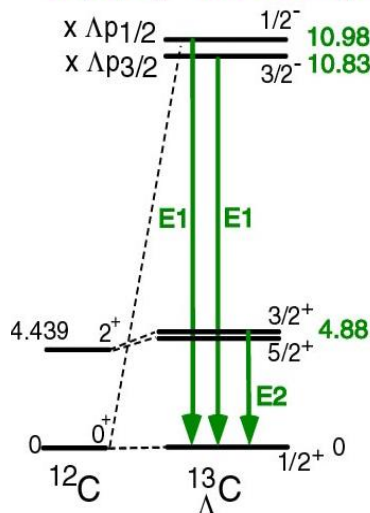
${}^{11}\text{B}$  ( $\pi^+, K^+\gamma$ ) KEK E518



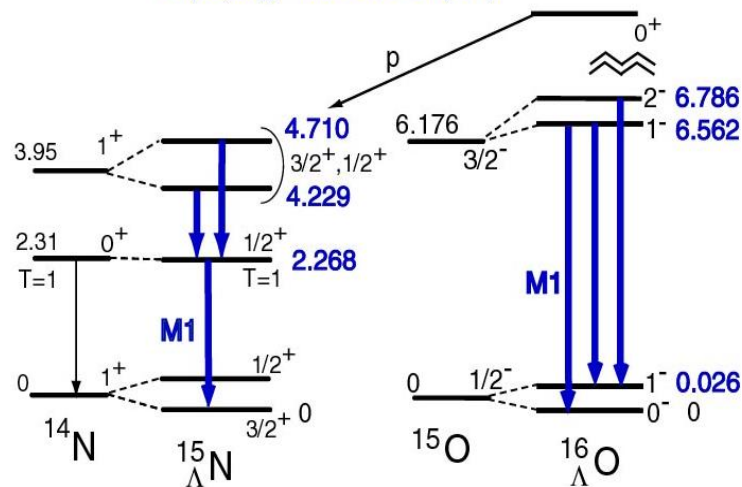
${}^{12}\text{C}$  ( $\pi^+, K^+\gamma$ ) KEK E566



${}^{13}\text{C}$  ( $K^-, \pi^-\gamma$ ) BNL E929 (NaI)



${}^{16}\text{O}$  ( $K^-, \pi^-\gamma$ ) BNL E930('01)



NPA835 (2010) 422

PTEP (2015) 081D01

PRL 86 (2001) 4255  
PRC 65 (2002) 034607

PRC 77 (2008) 054315

PRL 93 (2004) 232501  
EPJ A33 (2007) 247

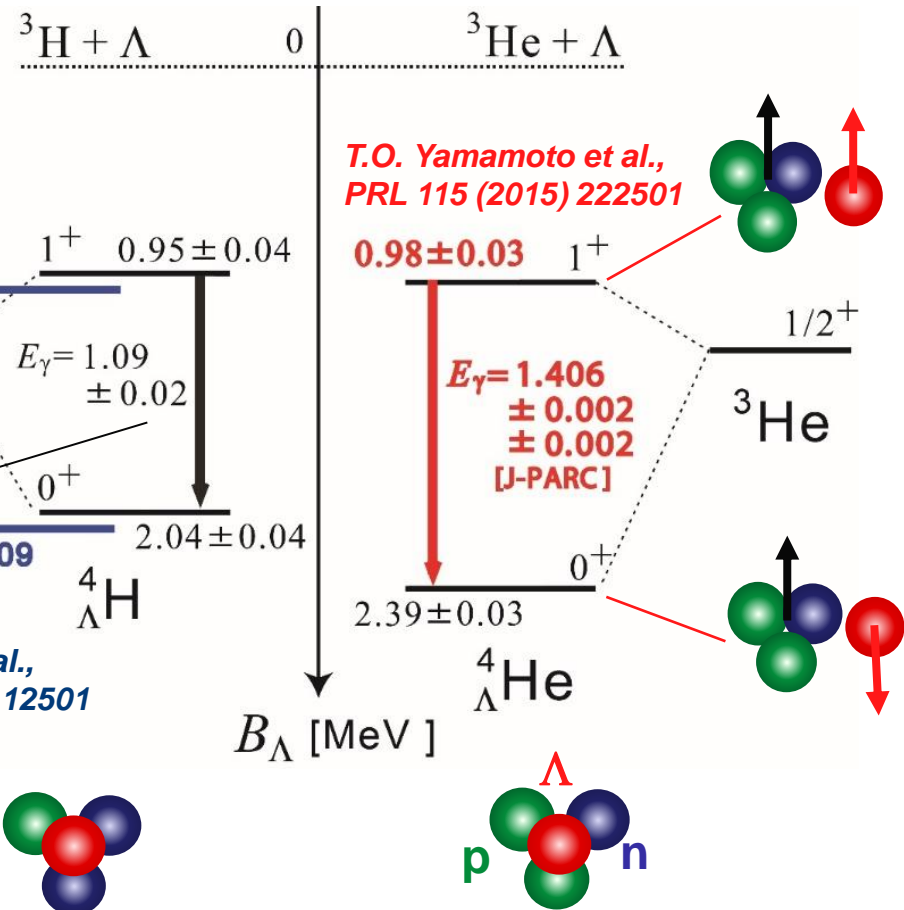
# Plans of $\gamma$ spectroscopy experiments

- Further study of CSB
    - Re-measure  ${}^4_{\Lambda}\text{H}(1^{+}\rightarrow 0^{+})$
    - p-shell hypernuclei via  $(\pi^{-}, \text{K}^0)$  reaction
  - Search for  ${}^3_{\Lambda}\text{H}$   $\gamma$ -rays
  - B(M1) measurement for  $g_{\Lambda}$  of a  $\Lambda$  in medium
  - Medium to heavy hypernuclei
    - E1( $p_{\Lambda}\rightarrow s_{\Lambda}$ ) for density dependent  $\Lambda\text{N}$  interaction and origin of spin-orbit splitting
    - Impurity effects in deformed hypernuclei
- E63 (approved)**
-



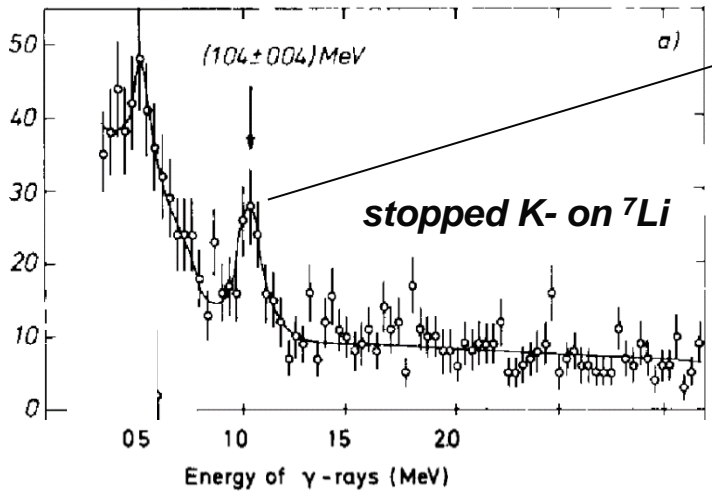
# $\Lambda\Sigma$ mixing and CSB

# Energy levels of A=4 mirror hypernuclei



**M. Bedjidian et al.**  
**Phys. Lett. B 83, 252 (1979).**

NaI counters (bad resolution)  
 a large Doppler broadening



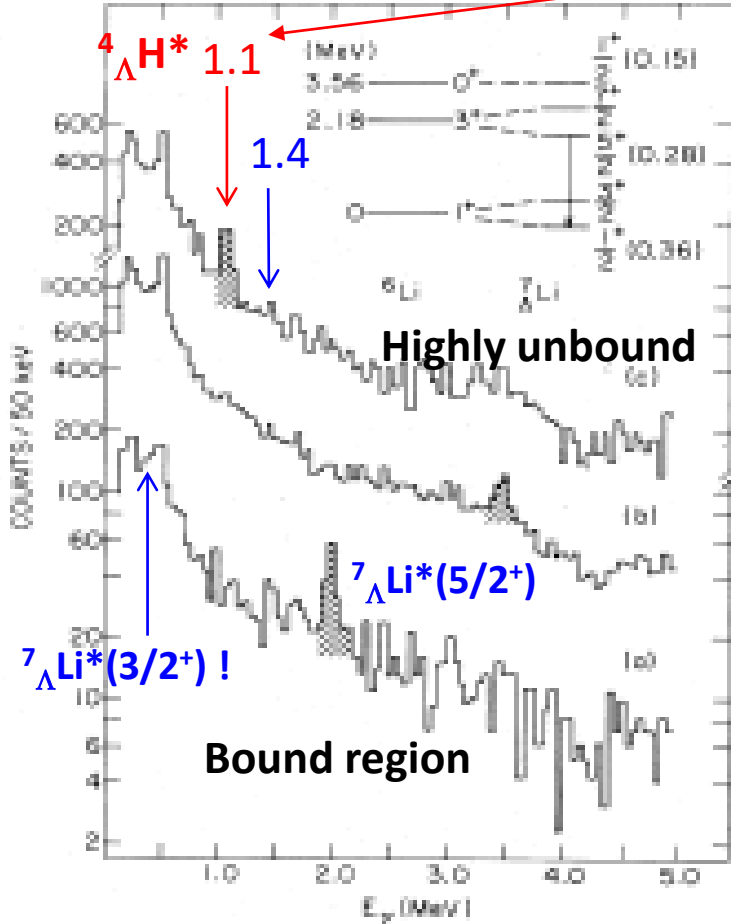
${}^4_{\Lambda}\text{H}$   $\gamma$ -ray should be precisely measured (E63).

# Production of ${}^4_{\Lambda}\text{H}^*$ and ${}^3_{\Lambda}\text{H}^*$ via in-flight ${}^7\text{Li} (K^-, \pi^-)$

M. Ukai

Gating highly unbound region of the missing mass  
 -> a peak at  $1.108 \pm 0.010 \text{ MeV}$  with systematic error  
 It should be  ${}^4_{\Lambda}\text{H} \gamma$ -ray

M. May, PRL 51(1983)2085



Possible reaction process  $Ex({}^7_{\Lambda}\text{Li}^*) > 19.3 \text{ MeV}$

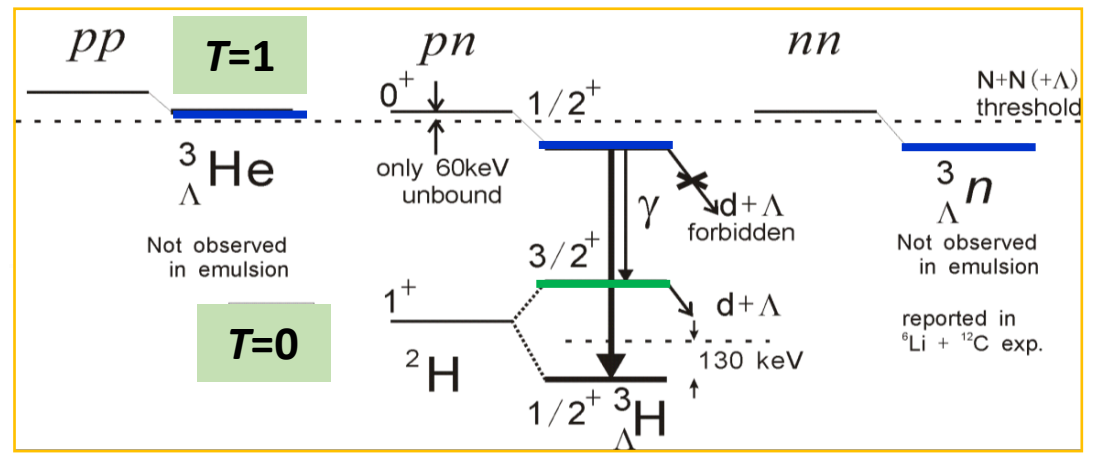
$$K^- + \alpha + t \rightarrow \Lambda + {}^3\text{He} + \pi^- + t$$

$\Lambda + {}^3\text{He} \rightarrow {}^4_{\Lambda}\text{He}$  ( $0^+$  only non-spin-flip)  
 $\Lambda + t \rightarrow {}^4_{\Lambda}\text{H}$  (Both  $0^+/1^+$  ratio = 1:3 expected)

Byproduct  ${}^7_{\Lambda}\text{Li}^*(p_n p_{\Lambda} \text{ substitutional state})$   
 $Ex({}^7_{\Lambda}\text{Li}^*) = 12 \text{ MeV}$

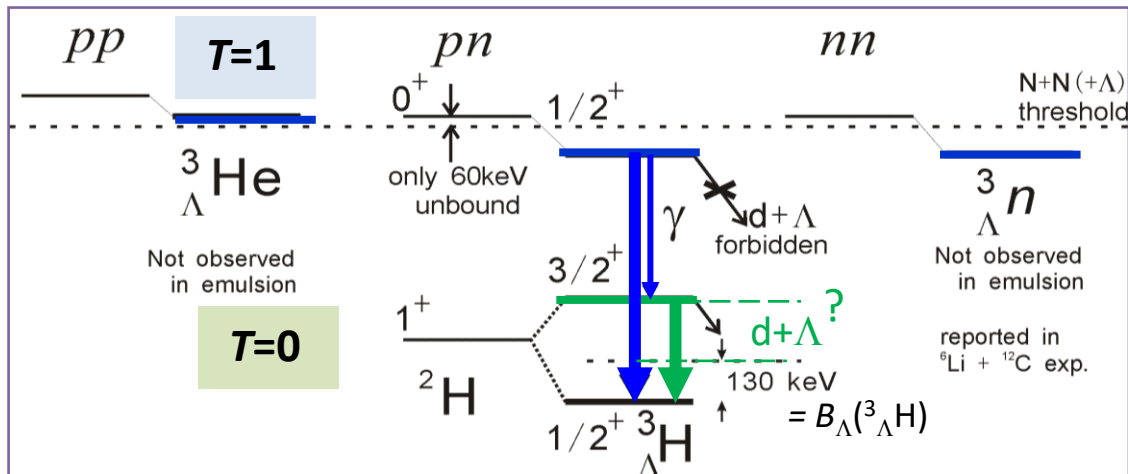
$$K^- + \alpha + t \rightarrow \alpha + {}^3_{\Lambda}\text{H}^* + \pi^-$$

NaI: 74 keV (FWHM) at 1 MeV





# Physics Motivation



**$T=1$  level**  $\gamma$  transitions from  ${}^3\Lambda\text{H}^*(T=1, 1/2^+)$  -> Precise energy for  $\Lambda n n$  ( $T=1$ ) interaction

**$T=0$  level**  $\gamma$  transitions from  ${}^3\Lambda\text{H}^*(T=0, 3/2^+)$

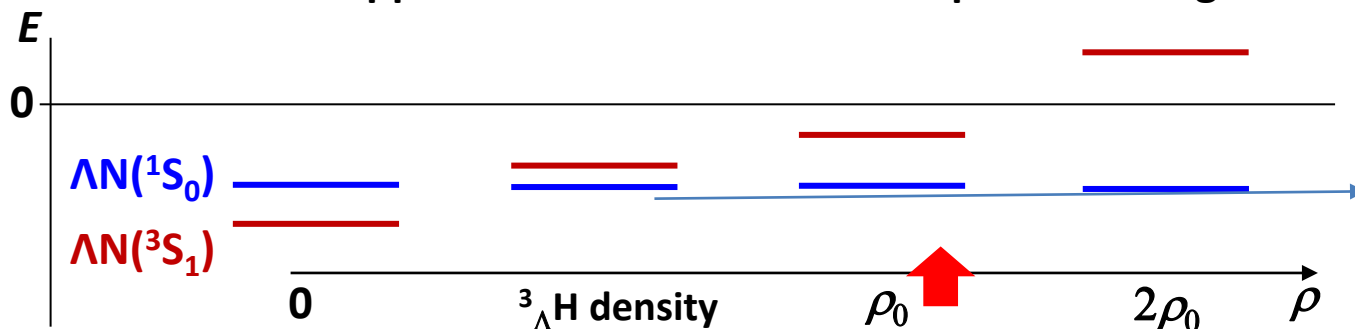
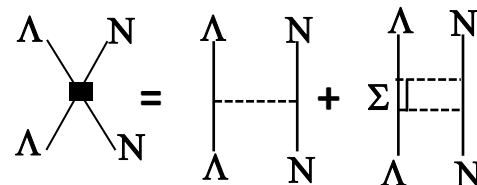
-> Attractive effect of  $\Lambda N$ - $\Sigma N$  in  $\Lambda N({}^3S_1)$

NLO13, HALQCD predict a large attraction in  $\Lambda N({}^3S_1)$  due to  $\Lambda N$ - $\Sigma N$

->  ${}^3S_1$  is less attractive than  ${}^1S_0$  in nuclear matter due to Pauli effect

-> Suppression of  $\Lambda N$ - $\Sigma N$  makes repulsion at high density

-> solution of hyperon puzzle ?



${}^3\Lambda\text{H}$  ( $3/2, 1/2$ ) splitting can be smaller than  $B_\Lambda$

Emulsion:  $0.13 \pm 0.05$  MeV  
STAR:  $0.41 \pm 0.12$  MeV

we know this only

# Range counters for E63

F. Oura

## J-PARC E63 実験を計画中 [1]

beam line: J-PARC K1.1

reaction:  ${}^7\text{Li}(K^-, \pi^-)$  反応の後,

生成される  ${}^7_\Lambda\text{Li}^*$  が,

${}^4_\Lambda\text{H}$  や  ${}^3_\Lambda\text{H}$  などのハイパー核に崩壊

[1] H. Tamura, J-PARC E63 proposal.

E63実験 physics motivations

- 核内での $\Lambda$ のg因子の変化
- 4体系ハイパー核( ${}^4_\Lambda\text{H}$ ,  ${}^4_\Lambda\text{He}$ )のCSB
- ${}^3_\Lambda\text{H}$ のエネルギー構造

ガンマ線測定 (Ge検出器群: Hyperball-J)

+

核種を完全に決定するために,

二体弱崩壊 $\pi$ の飛程測定 (Range counter)

$\gamma$ -weak coincidence!

${}^4_\Lambda\text{H} \rightarrow {}^4\text{He} + \pi^-$  (133 MeV/c, range in pla.scinti.=99.5 mm)

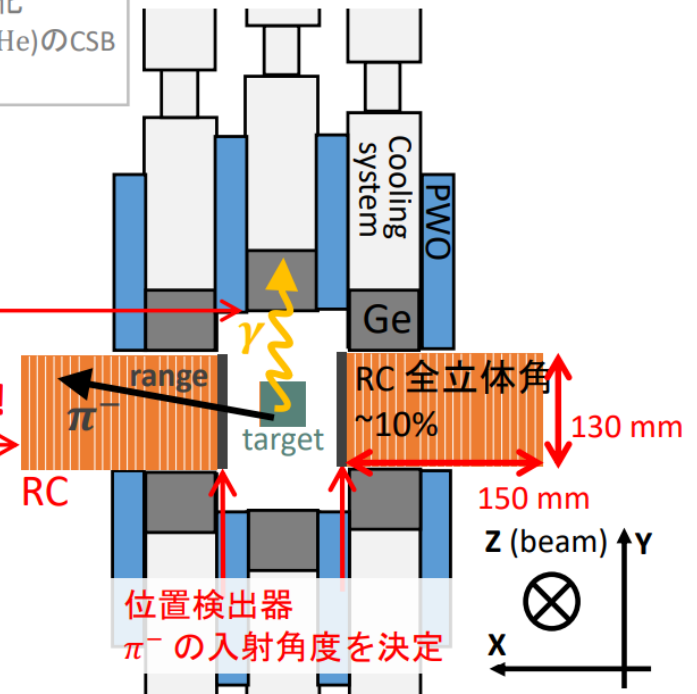
${}^3_\Lambda\text{H} \rightarrow {}^3\text{He} + \pi^-$  (114 MeV/c, range = 64.6 mm)

(要求)  $\rightarrow$  これらの  $\pi^-$  をRCで識別したい。

$\leftrightarrow$  これらの  $\pi^-$  (range差: 34.9 mm) を  $3\sigma$  で分けたい。

Target周りのsetup

Hyperball-J



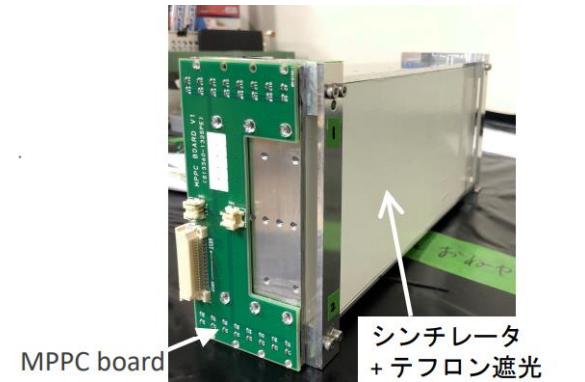
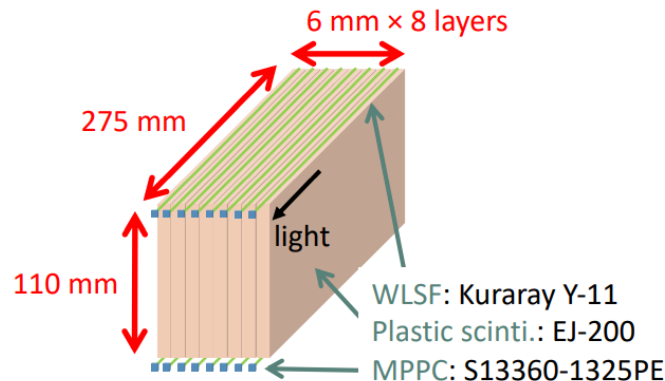
位置検出器

$\pi^-$  の入射角度を決定

9/16/2021

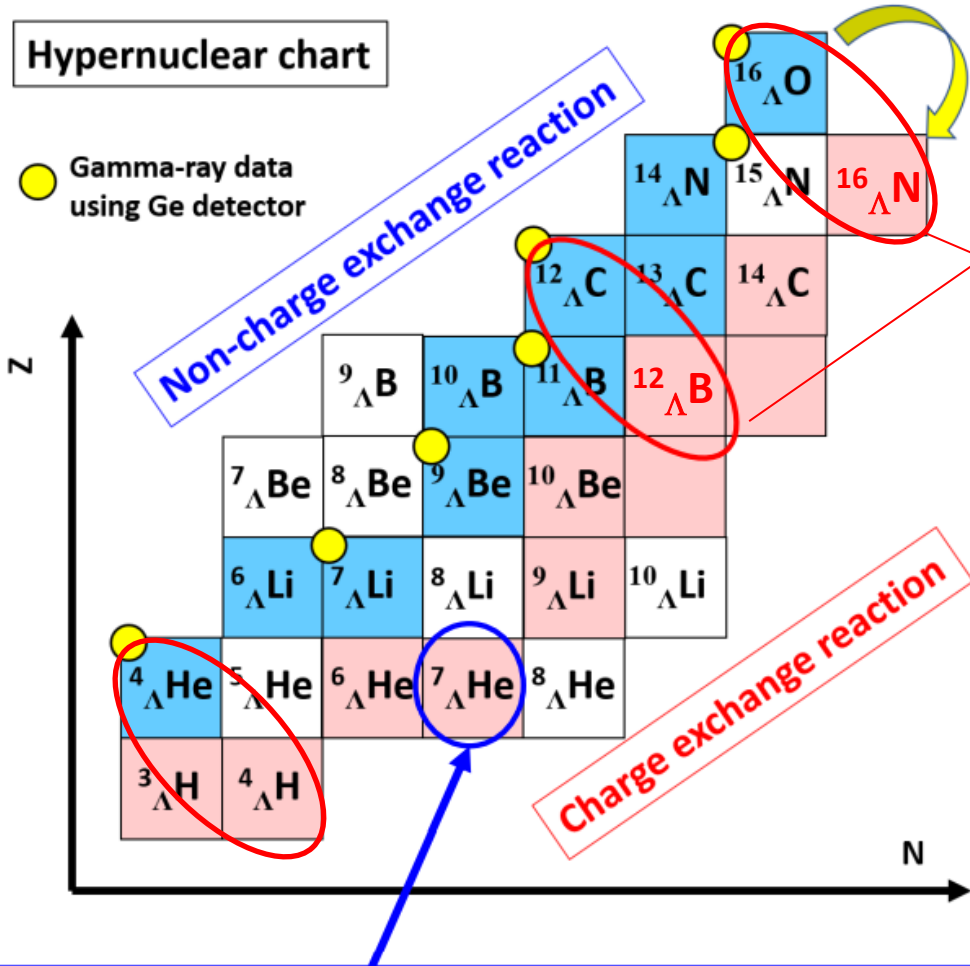
日本物理学会 2021年秋季大会 大浦 文也(東北大)

3



# CSB and n-rich p-shell hypernuclei

T.O. Yamamoto



How strongly CSB effect appears for A>4 hypernuclei?  
 -> may help to understand the origin

We only have precise data for proton rich hypernuclei produced by "n→Λ reaction"



Need to approach mirror pair (neutron rich) hypernuclei by introducing "p→Λ reaction"

Other neutron rich hypernuclei can be accessed  
 → ΛΣ mixing effect  
 Shrinkage (Drastic change of B(E2))



# **Baryon modification in nuclear medium**

# $g_\Lambda$ in a nucleus

## B(M1) of $\Lambda$ -spin-flip M1 transition

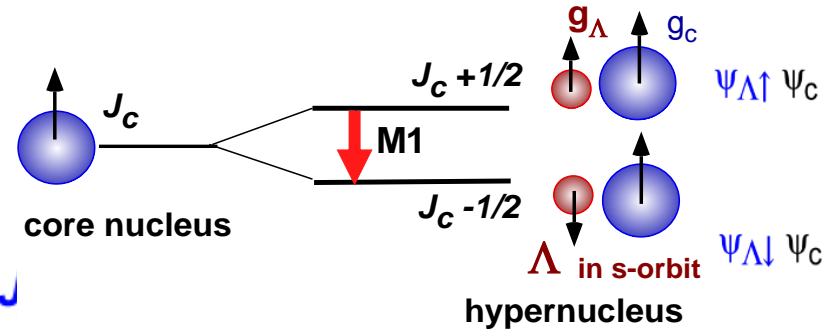
$$B(M1) = (2J_{up} + 1)^{-1} |\langle \Psi_{low} \| \mu \| \Psi_{up} \rangle|^2$$

$$= (2J_{up} + 1)^{-1} |\langle \Psi_{\Lambda\downarrow} \Psi_c \| \mu \| \Psi_{\Lambda\uparrow} \Psi_c \rangle|^2$$

$$\mu = g_c J_c + g_\Lambda J_\Lambda = g_c J + (g_\Lambda - g_c) J_\Lambda$$

$$= \frac{3}{8\pi} \frac{2J_{low} + 1}{2J_c + 1} (g_\Lambda - g_c)^2 \quad [\mu_N^2]$$

R.H. Dalitz and A. Gal, *Annals of Phys.* 116 (1978) 167.



: assuming “weak coupling”  
between a  $\Lambda$  and the core.

${}^7_\Lambda\text{Li}$  ~100% **Doppler Shift Attenuation Method:** eg) B(E2): Tanida et al.

$$\Gamma = BR / \tau = \frac{16\pi}{9} E_\gamma^3 B(M1)$$

*PRL* 86 (2001) 1982

## Modification of $g_\Lambda$ in nuclear medium?

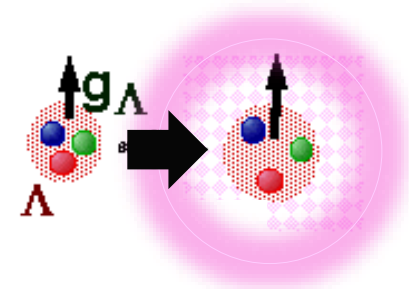
■  $\Lambda$ - $\Sigma$  mixing: C.B. Dover, H. Feshbach, A. Gal, *PRC* 51 (1995) 541.

+2--5 % for  ${}^4_\Lambda\text{He}$ , small for T=0 hypernuclei

■ K,  $2\pi$  exchange current: K. Saito, M. Oka, T. Suzuki, *NPA* 625 (1997) 95.

-7% for  ${}^7_\Lambda\text{Li}$

■ “Quark exchange current” in QCM T. Takeuchi, K. Shimizu, K. Yazaki, *NPA* 481 (1988) 693.



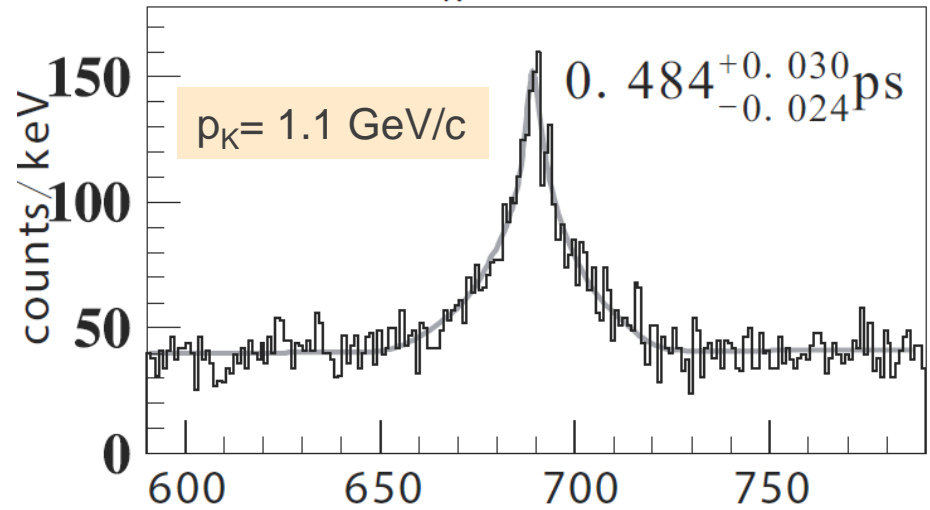
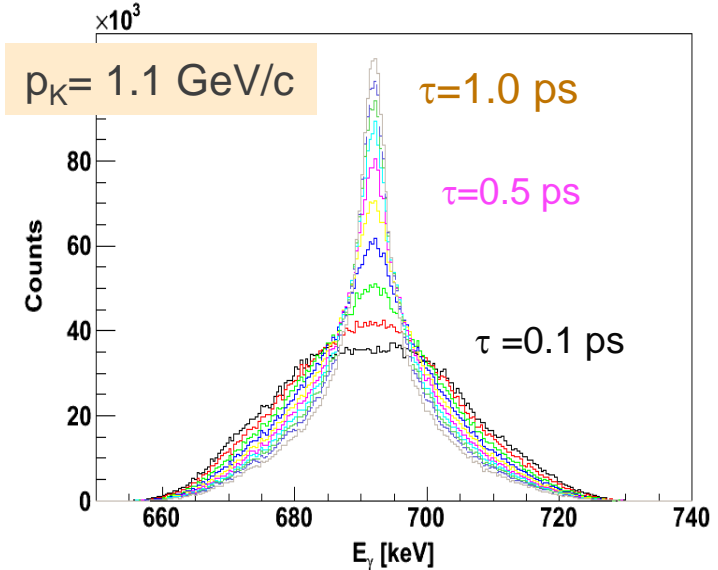
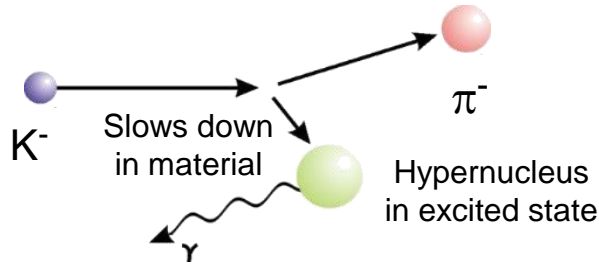
# Experiment at J-PARC

Approved as E13 -> E63

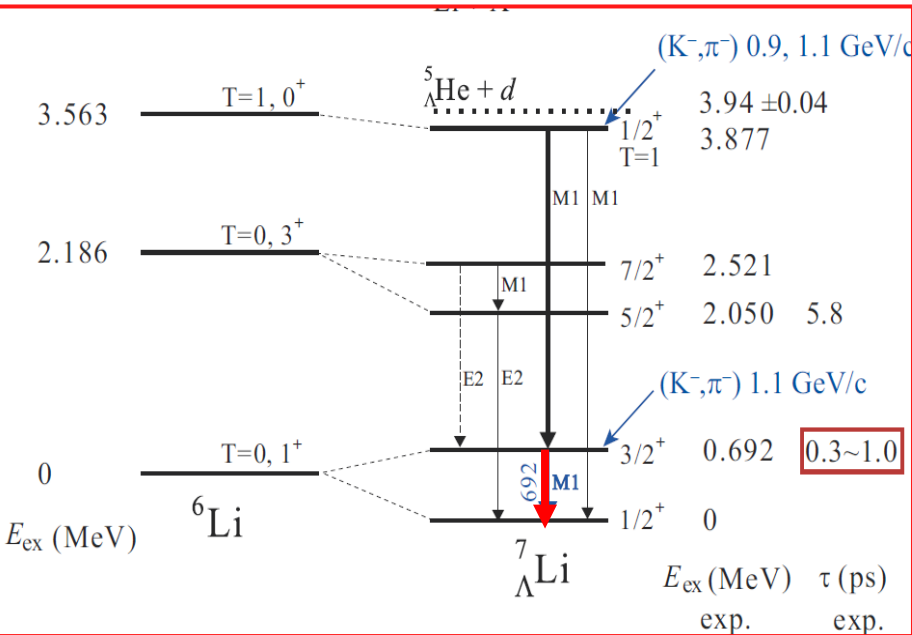
DSAM (Doppler Shift Attenuation Method)

$\tau \sim 0.5 \text{ ps}$   
 $t_{\text{stop}} \sim 2 \text{ ps}$

in  $\text{Li}_2\text{O}$  ( $2.01 \text{ g/cm}^3$ )



H. Tamura et al., Nucl.Phys. A881 (2012) 310



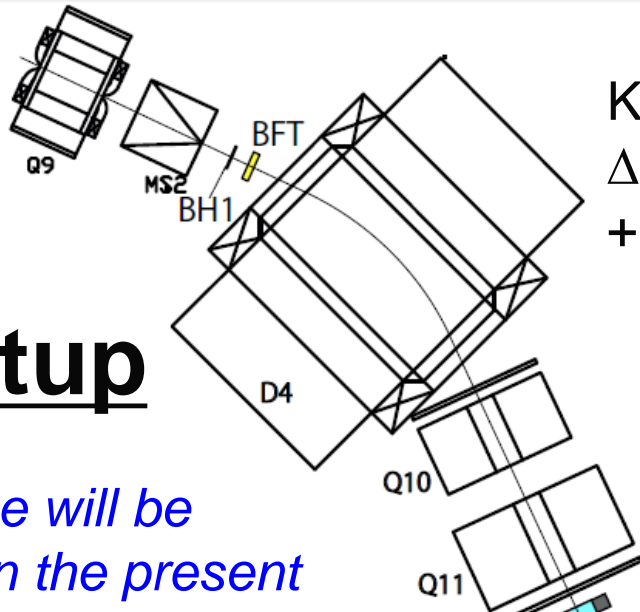
For 35 days for 50kW

Assuming 56k  $K^-$ /spill for 0.9 GeV/c

176k  $K^-$ /spill for 1.1 GeV/c

Stat. error  $\Delta\tau/\tau = 6\%$   $\Rightarrow \frac{\Delta|g_\Lambda - g_c|}{|g_\Lambda - g_c|} \sim 3\%$

# K1.1

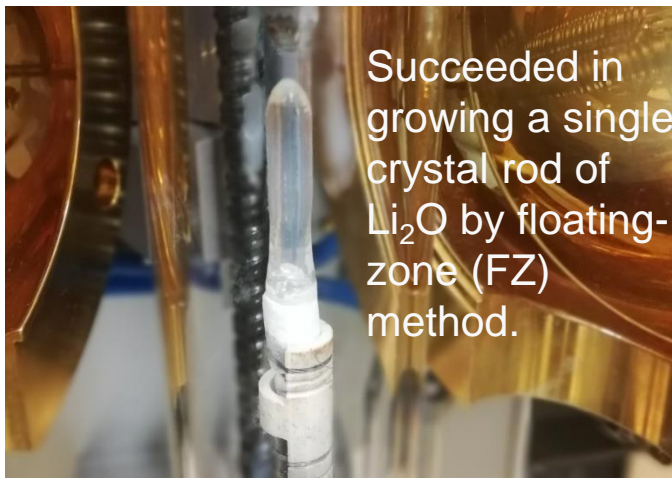


K1.1 Beam spectrometer  
 $\Delta p/p = 0.042\%$  (FWHM) @1.1 GeV/c  
 + multiple scat. effect

## E63 setup

*K1.1 beamline will be constructed in the present hadron hall.*

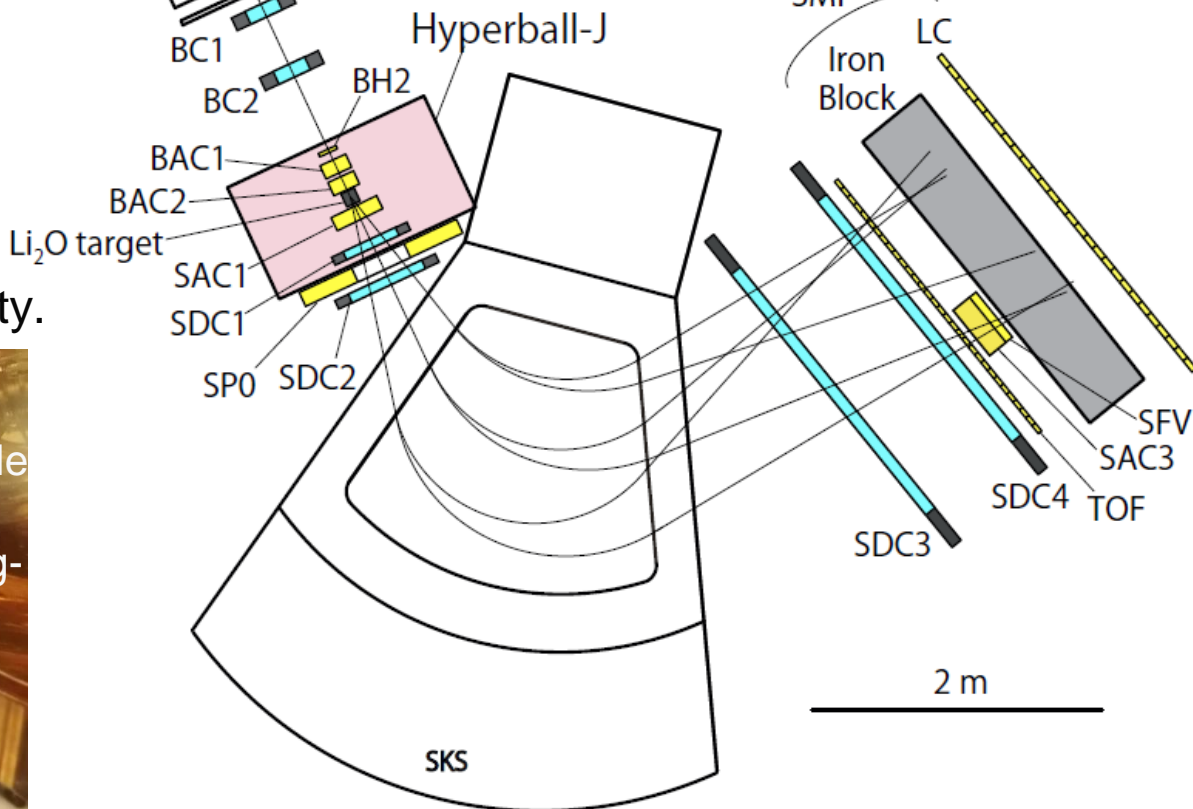
For the Li target, we need single-crystal  $\text{Li}_2\text{O}$  with a microscopically uniform density.



Succeeded in growing a single crystal rod of  $\text{Li}_2\text{O}$  by floating-zone (FZ) method.

K1.1 area

*Detectors are the same as E13  
 Almost all of them are ready.*



# B(M1) value expected in “ordinary” nuclear physics

Experimental values:

$${}^6\text{Li}: g_c = 0.822047 \mu_N$$

$$\Lambda: g_\Lambda (\text{free}) = -1.226 \pm 0.008 \mu_N$$

=> If weak coupling is OK,

$${}^7_\Lambda\text{Li} \text{ B(M1)}$$

$$= 0.334 \pm 0.003 \mu_N^2$$

## Calculations

	$J_i, T_i \rightarrow J_j, T_f$	$B(M1) (\mu_N^2)$	
${}^7_\Lambda\text{Li}$	$3/2^+, 0 \rightarrow 1/2^+, 0$	0.322	${}^5_\Lambda\text{He} + p + n$ cluster (Hiyama et al.) <sup>a</sup>
		0.352	${}^4\text{He} + d + \Lambda$ cluster (Motoba-Bando-Ikeda) <sup>b</sup>
		0.364	Shell model (Dalitz-Gal) <sup>c</sup>

-3.5% from weak coupling

<+5.5% from weak coupling

<sup>a</sup> H. Hiyama et al., PRC 59 (1999) 2351.

<sup>b</sup> T. Motoba, H. Bando, K. Ikeda, T. Yamada, PTP Suppl. 81 (1985) 42.

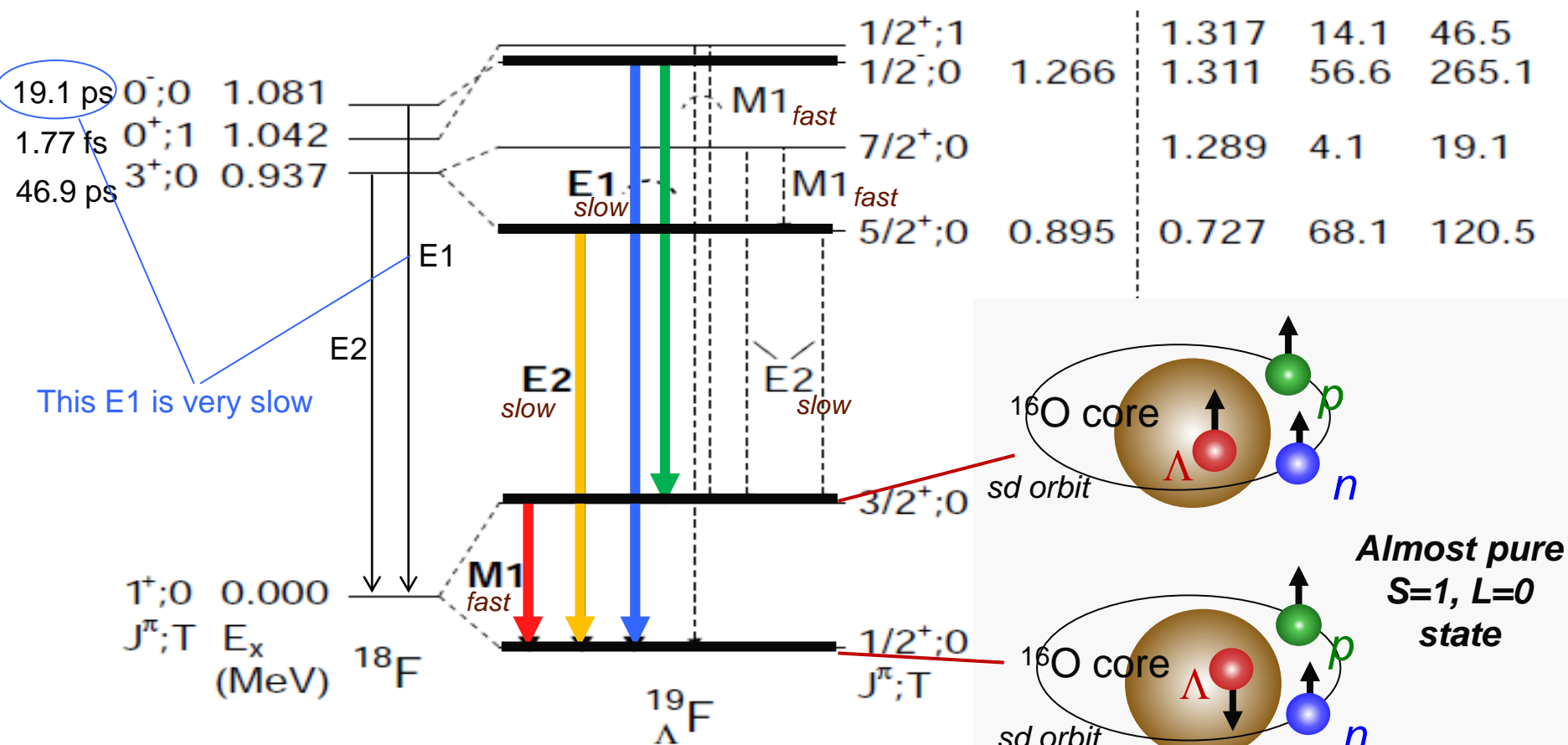
<sup>c</sup> R.H. Dalitz and A. Gal, Annals of Phys. 116 (1978) 167.

- Suggesting that the weak coupling hypothesis holds well.
- Better calculation by Hiyama is going on.
  - [\${}^4\text{He} + p + n + \Lambda\$  cluster model with and without  \$\Lambda - \Sigma\$  coupling](#)
- Ab-initio 7-body calculations in future (after the measurement is done)

# **Medium/heavy hypernuclei and the hyperon puzzle**

# Recent result: Level scheme of $^{19}_{\Lambda}F$

Assigned from the peak width (Doppler broadening or not) and the expected yield.



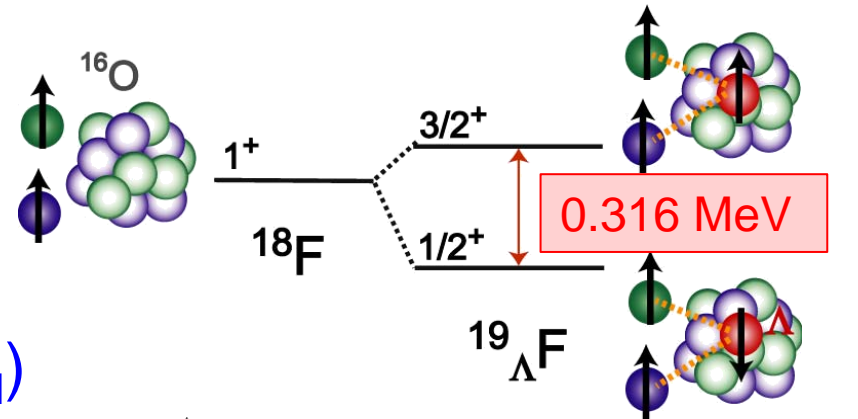
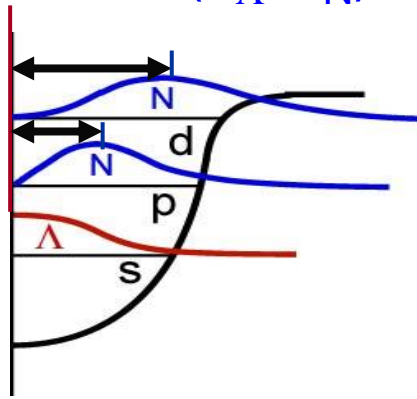
fast: Doppler broadening ( $< 1$  ps)  
 slow: No Doppler broadening ( $> 1$  ps)

\* A. Umeya and T. Motoba, Nucl. Phys. A954 (2016) 242.  
 Shell model calculation with NSC97f interaction

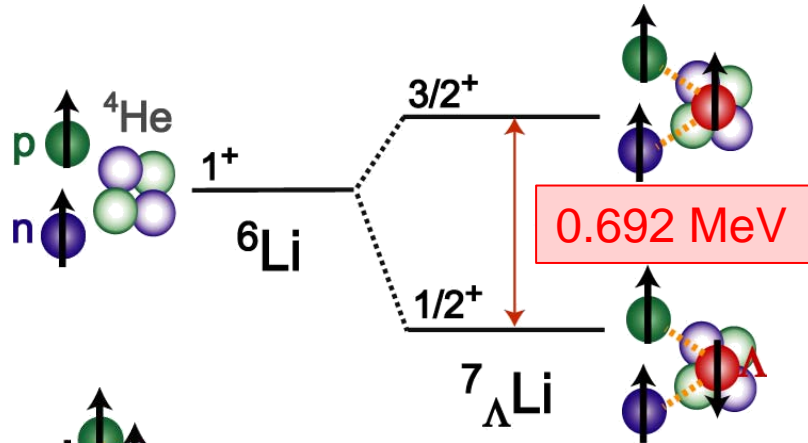


# A-dependence of $\Lambda N$ interaction strength

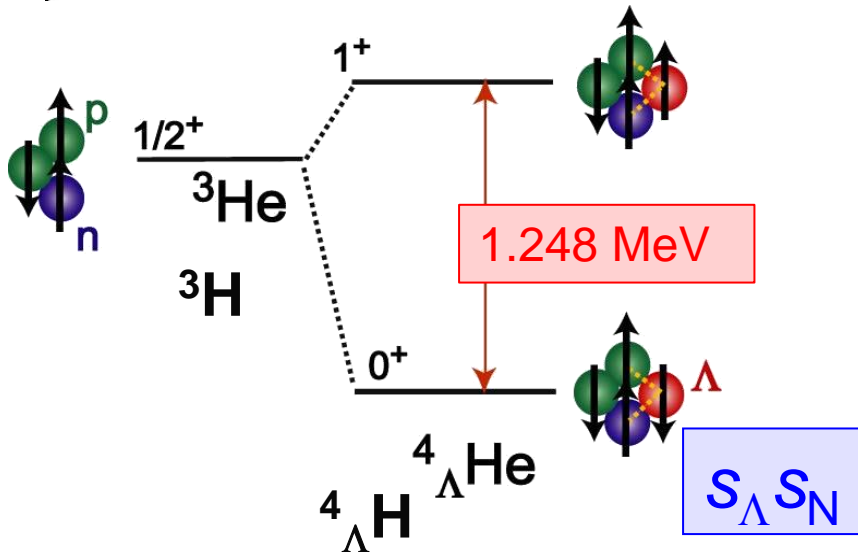
$$\bar{r}(s_\Lambda - d_N) > \bar{r}(s_\Lambda - p_N) > \bar{r}(s_\Lambda - s_N)$$



$s_\Lambda d_N$



$s_\Lambda p_N$



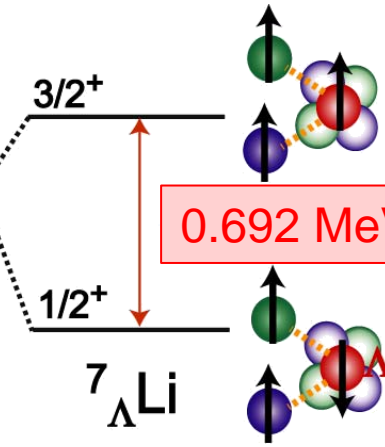
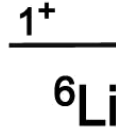
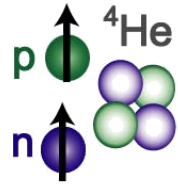
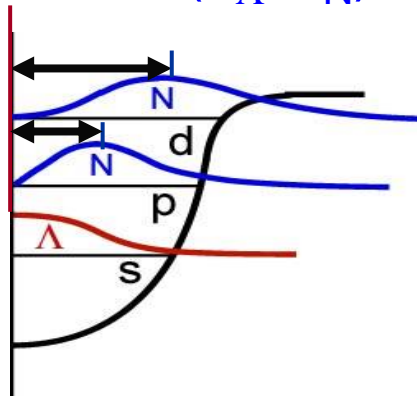
$s_\Lambda s_N$

Effective interaction between two baryons in different shells is consistently understood by theories

⇒ Level structure of hypernuclei in a wide range of A can be reproduced.  
 ⇒ Density dependence of  $\Lambda N$  int. may be able to be studied

# A-dependence of $\Lambda N$ interaction strength

$$\bar{r}(s_\Lambda - d_N) > \bar{r}(s_\Lambda - p_N) > \bar{r}(s_\Lambda - s_N)$$

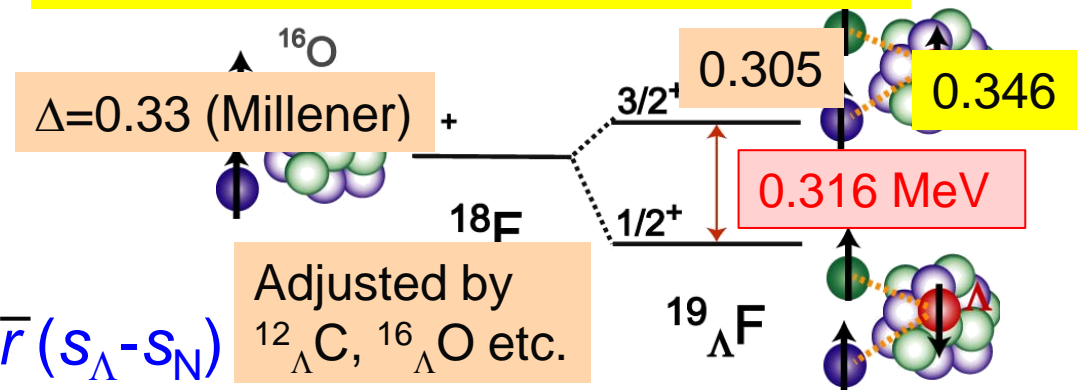


$\leq 0.629$

$s_\Lambda p_N$

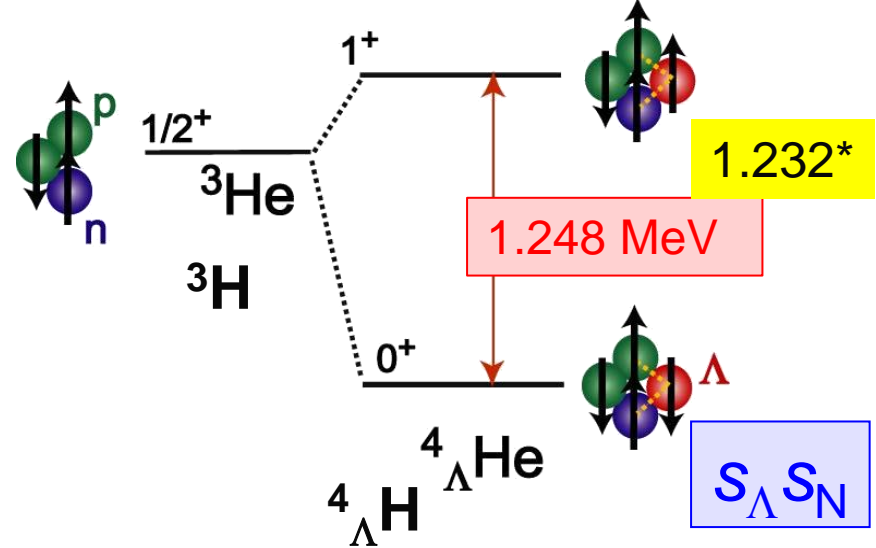
$s_\Lambda d_N$

NSC97e+f (Motoba, Umeya, Akaishi\*)



Adjusted by  ${}^{12}_\Lambda\text{C}$ ,  ${}^{16}_\Lambda\text{O}$  etc.

$\Delta=0.33$  (Millener) +



$s_\Lambda s_N$

Effective interaction between two baryons in different shells is consistently understood by theories

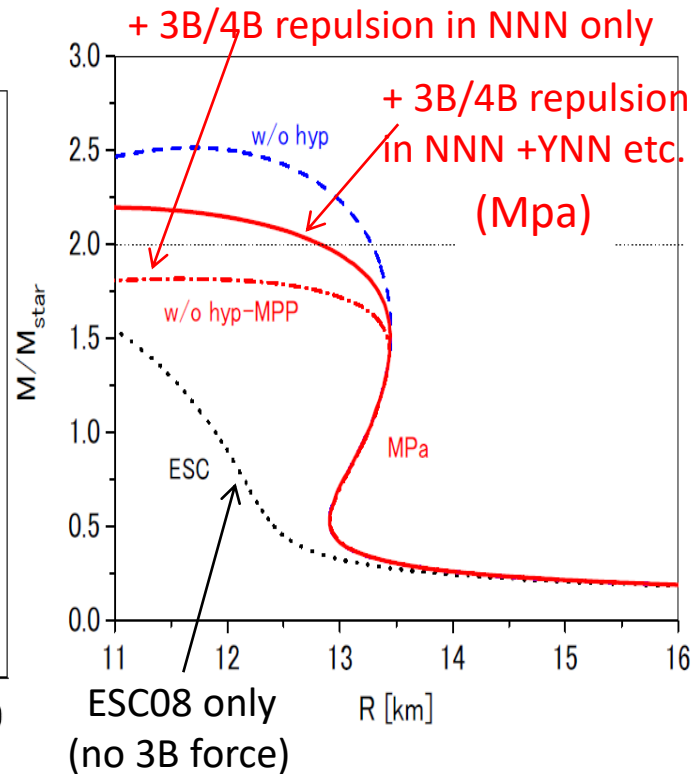
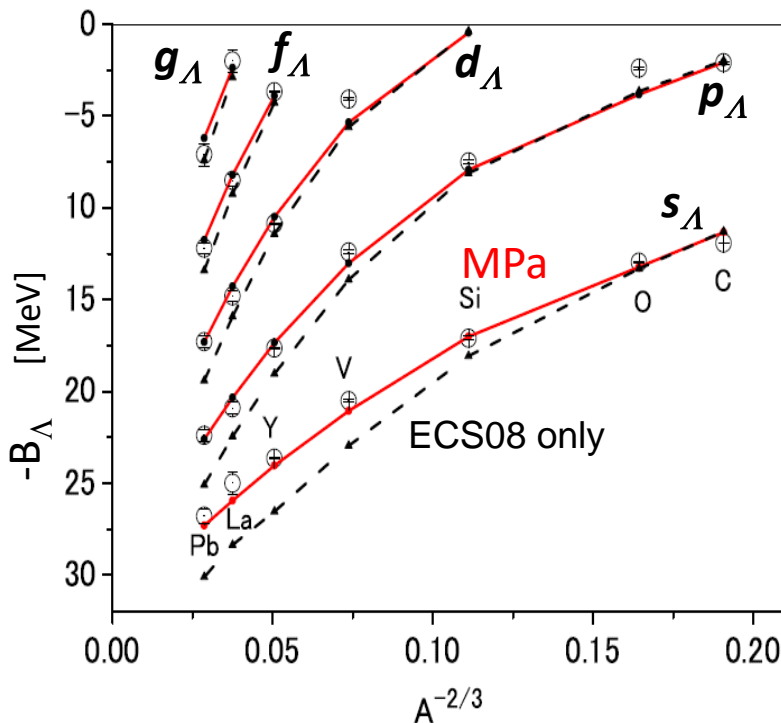
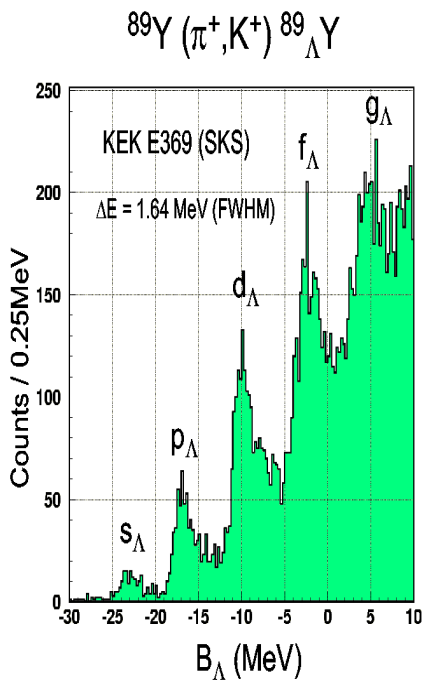
$\Rightarrow$  Level structure of hypernuclei in a wide range of A can be reproduced.  
 $\Rightarrow$  Density dependence of  $\Lambda N$  int. may be able to be studied

# How to study density dependence of $\Lambda N$ interaction in matter?

Ab-initio calc. of nuclear masses from NN force => NNN repulsion necessary  
 Similar YNN (YYN, YYY) repulsive forces?  
 --- Lack of precise YN scattering /hypernuclear data!

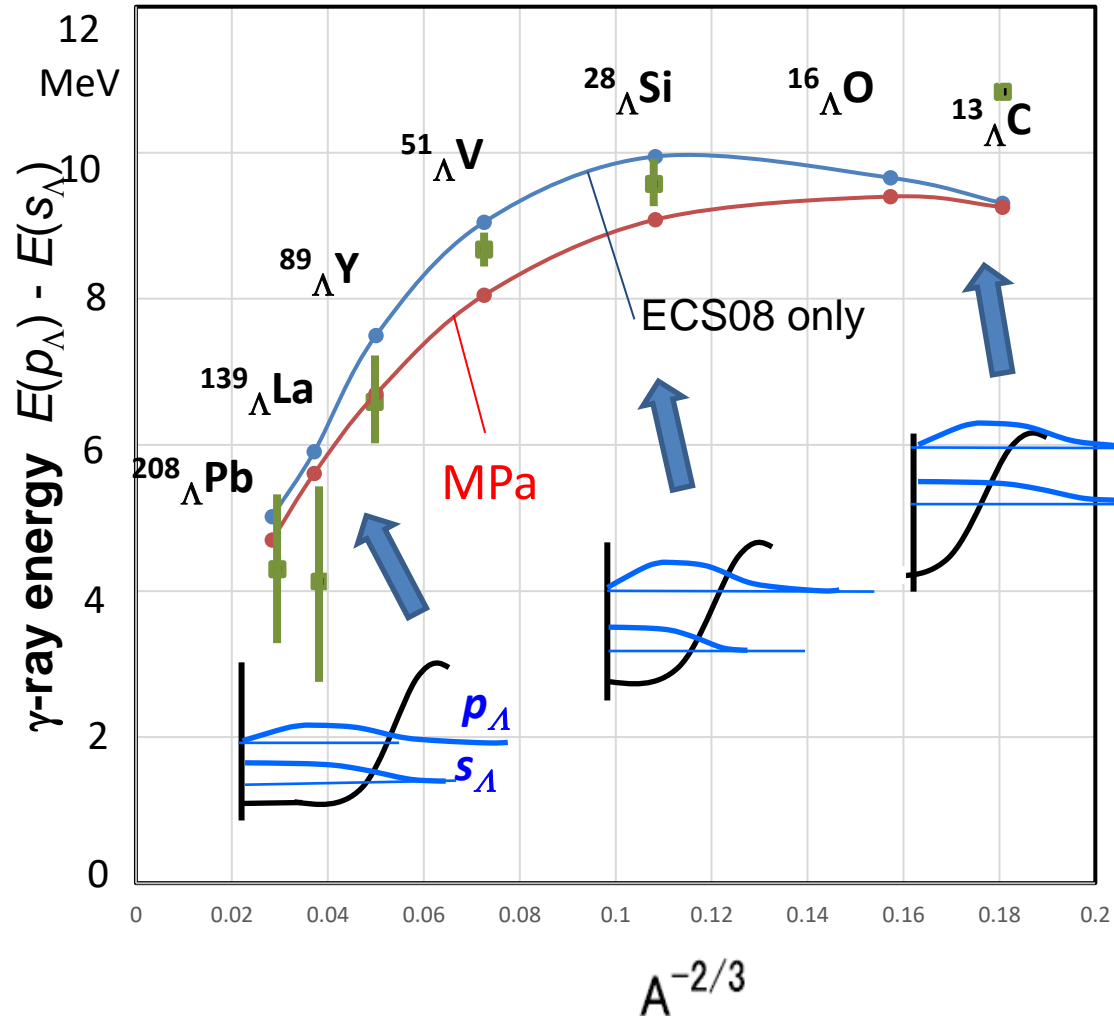
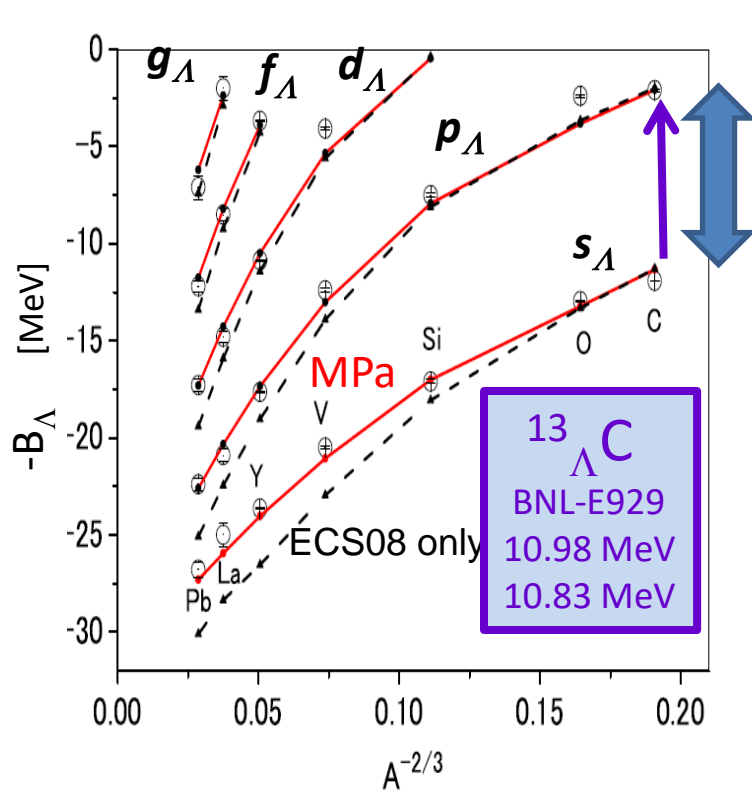
**Precise  $B_\Lambda$  data for wide A of  $\Lambda$  hypernuclei**  
**in  $< 0.1$  MeV accuracy is necessary**  
 => **HIHR at Ext-HD**

*Yamamoto, Furumoto, Rijken et al.*  
 PRC88 (2013) 2, 022801 NNN determined  
 PRC90 (2014) 045805 from HI collision data



# Another approach using $\gamma$ -rays

$p_\Lambda$ - $s_\Lambda$  spacing is affected by density dep. of  $\Lambda N$  interaction  
 It can be precisely ( $\sim$ keV) measured with E1  $\gamma$ -transitions.

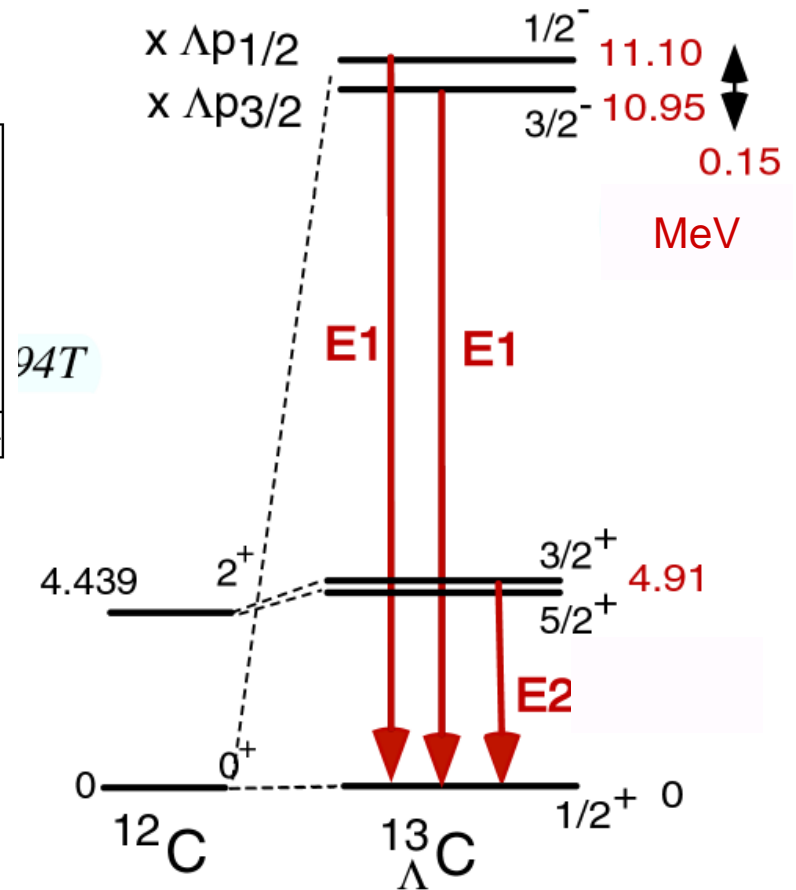
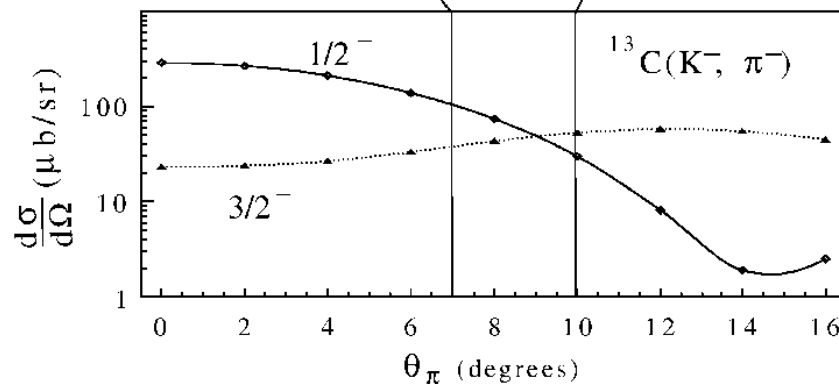
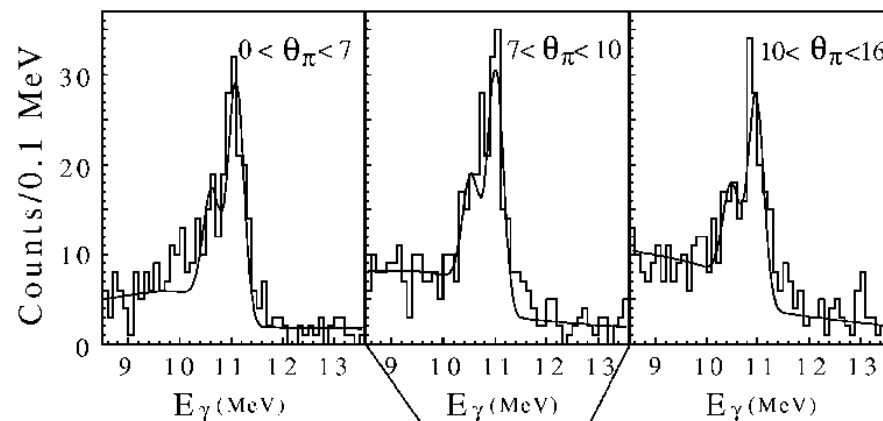


# $\Lambda$ spin-orbit splitting in $^{13}_{\Lambda}\text{C}$

$^{13}\text{C} (\text{K}^-, \pi^- \gamma)$   
BNL E929  
w/ NaI array

$p_{1/2}, p_{3/2}$  single-particle level splitting

$$E(1/2^-) - E(3/2^-) = 152 \pm 54 \pm 36 \text{ keV}$$



*Ajimura et al., PRL 86 (2001) 4255*

FIG. 2.  $\gamma$  ray spectra taken in coincidence with scattered  $\pi^-$ 's (upper panel) and differential cross section of  $1/2^-$  and  $3/2^-$  states calculated by Motoba [18] (lower panel) are shown.

# E1 ( $p_{\Lambda} \rightarrow s_{\Lambda}$ ) measurement for a wide A range

$^{29}_{\Lambda}\text{Si}$ ,  $^{52}_{\Lambda}\text{Cr}$ ,  $^{89}_{\Lambda}\text{Y}$ ,  $^{135}_{\Lambda}\text{La}$ ,  $^{208}_{\Lambda}\text{Pb}$

	$^{13}_{\Lambda}\text{C}$	$^{16}_{\Lambda}\text{O}$	$^{28}_{\Lambda}\text{Si}$	$^{29}_{\Lambda}\text{Si}$	$^{40}_{\Lambda}\text{Ca}$	$^{51}_{\Lambda}\text{V}$	$^{52}_{\Lambda}\text{Cr}$	$^{89}_{\Lambda}\text{Y}$	$^{139}_{\Lambda}\text{La}$	$^{208}_{\Lambda}\text{Pb}$
$\Delta E (p_{\Lambda}-s_{\Lambda})$	11.10 10.95	10.6	9.6	~9	~9	8.8 (8.1)	~8	6.6 (6.0)	4.1	4.4
Sp (core)	16.0	7.3	7.5	11.6	5.8	7.9	9.5	6.7	6.1	7.5
Sn (core)	18.7	13.2	13.3	17.2	13.3	9.3	9.3	9.4	7.5	6.7
Target (%)	$^{13}\text{C}$ 1.1%	$^{16}\text{O}$ 100%	$^{28}\text{Si}$ 92%	$^{29}\text{Si}$ 4.7%	$^{40}\text{Ca}$ 97%	$^{51}\text{V}$ 100%	$^{52}\text{Cr}$ 84%	$^{89}\text{Y}$ 100%	$^{139}\text{La}$ 100%	$^{208}\text{Pb}$ 52%

**( $K^-, \pi$ ) 1.1 GeV/c @K1.1 line, 100 kW, Total ~ 7 weeks**

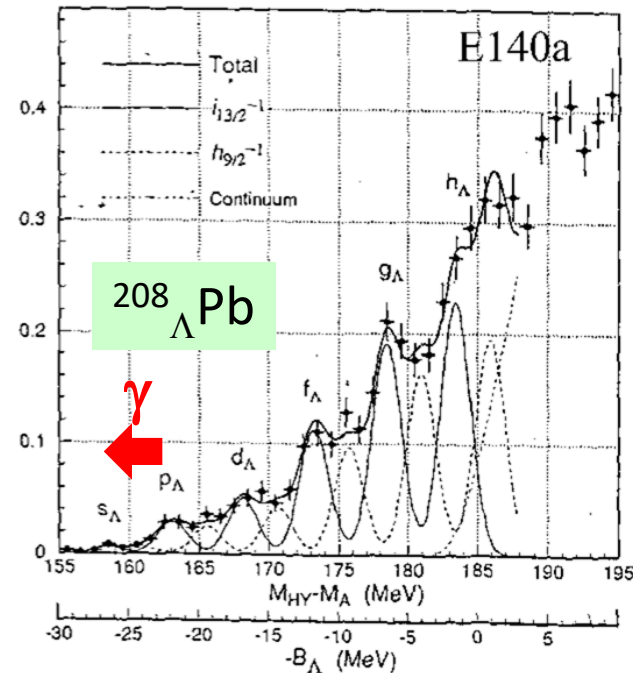
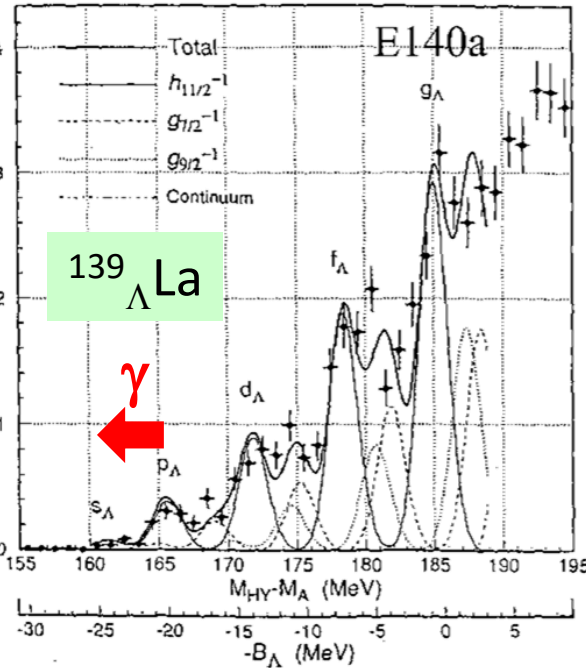
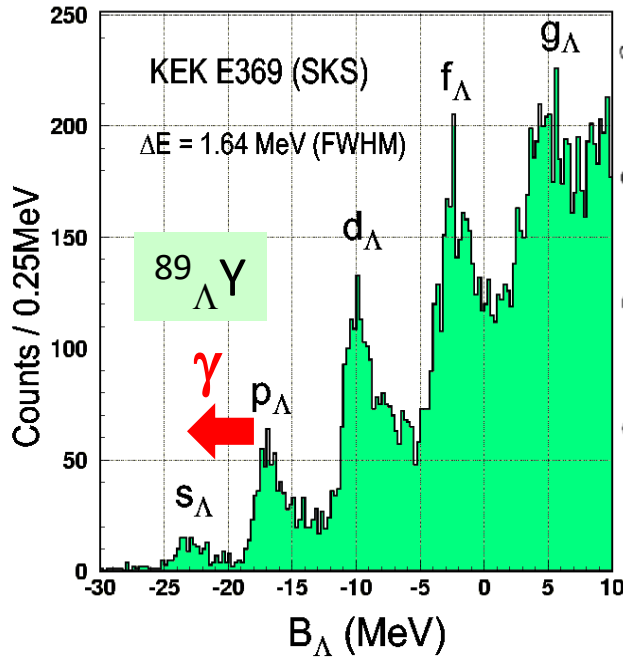
- **Density dependence of  $\Lambda N$  interaction**
- **Origin of nuclear LS splitting -> “Nuclear structure without pion”**
  - 2-body LS force ---Very small due to cancellation between a large SLS and a large ALS
  - Tensor force ---No one pion exchange -> small, no isospin dependence.
  - Many-body correlation ---No one pion exchange ->Small ?

# Heavy hypernuclei

$^{89}\text{Y}(\pi^+, K^+) ^{89}_{\Lambda}\text{Y}$

$^{139}\text{La}(\pi^+, K^+)_{\Lambda}^{139}\text{La}$ ,  $p_{\pi} = 1.06 \text{ GeV}/c$

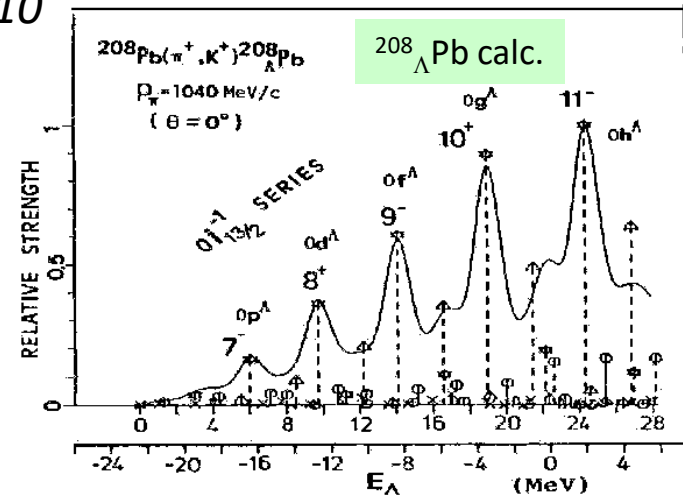
$^{208}\text{Pb}(\pi^+, K^+)_{\Lambda}^{208}\text{Pb}$ ,  $p_{\pi} = 1.06 \text{ GeV}/c$



Hasegawa et al., PRC 53 (1996) 1210

$(\pi^+, K^+)$  reaction

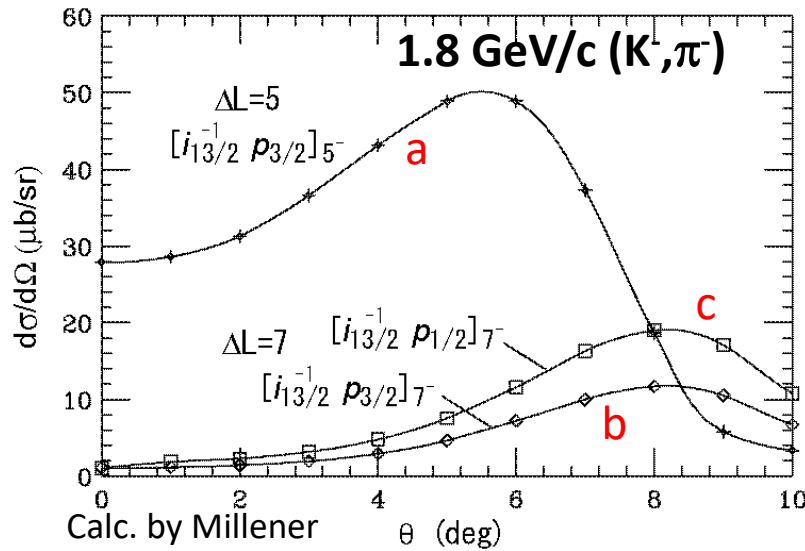
KEK E140a, K6+SKS





# $\gamma$ -spectroscopy of $^{208}_{\Lambda}\text{Pb}$

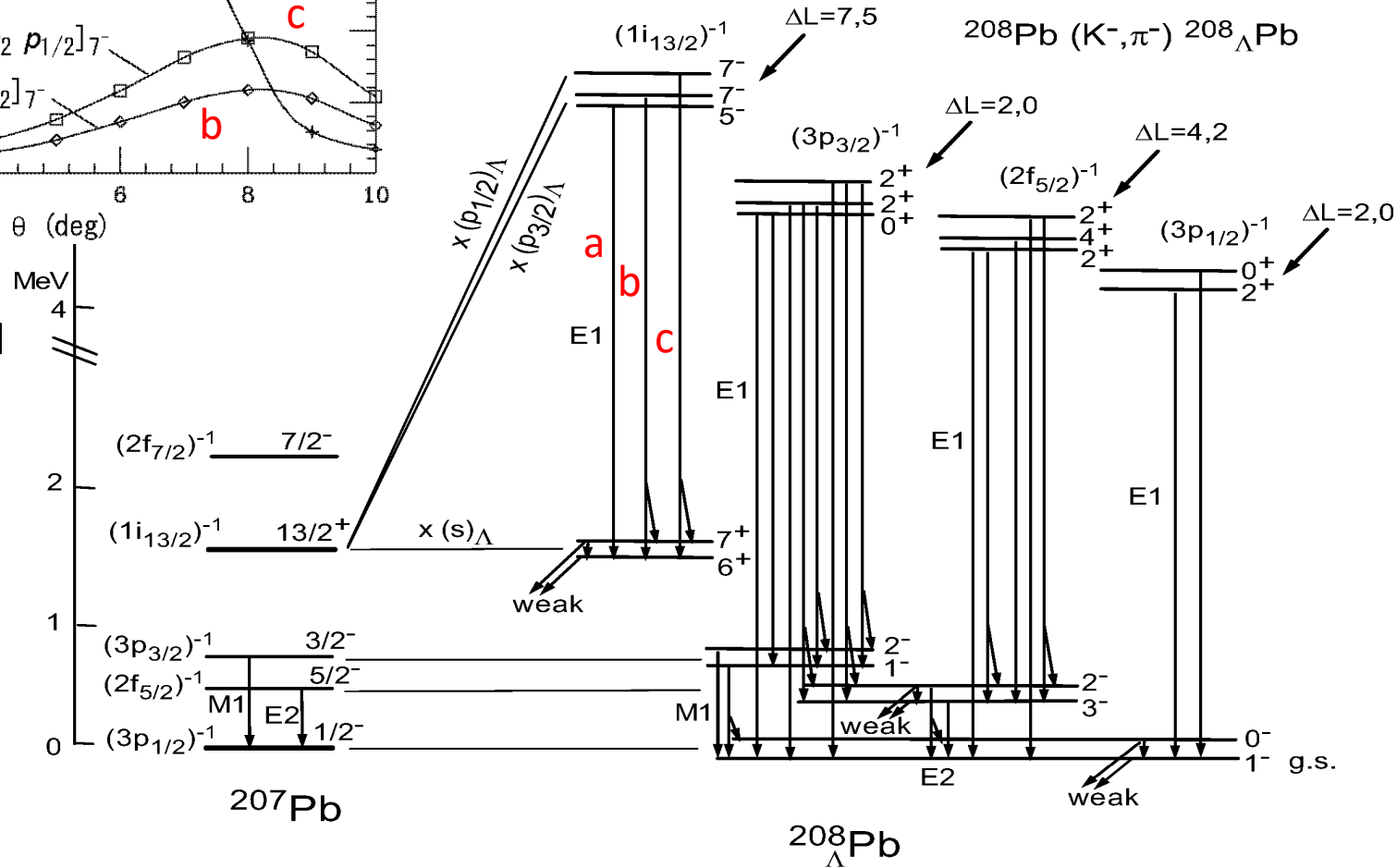
Split into several transitions



from J-PARC LOI

15 days at K1.1  
@120 kW

a: ~300 ev  
b: ~200 ev  
c: ~700 ev



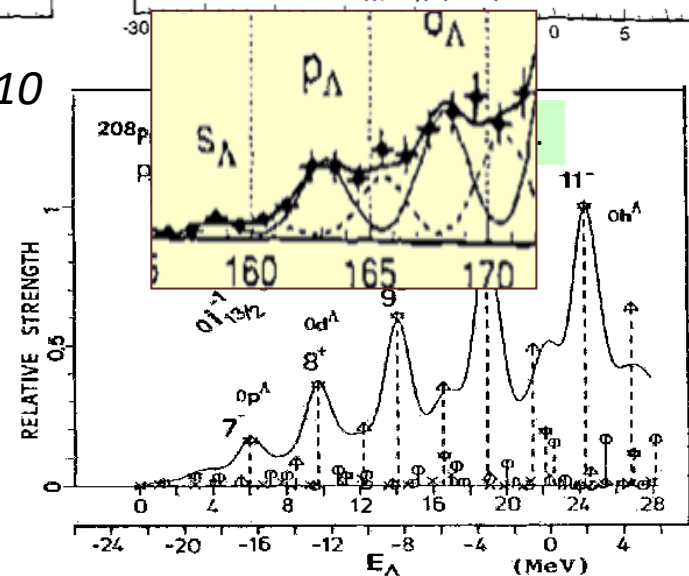
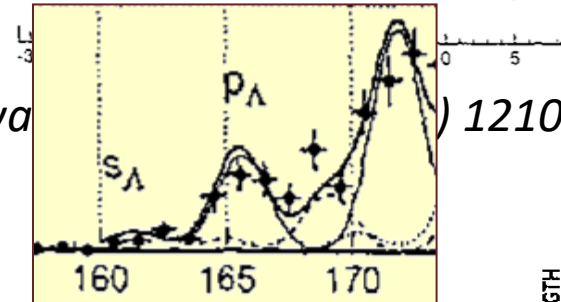
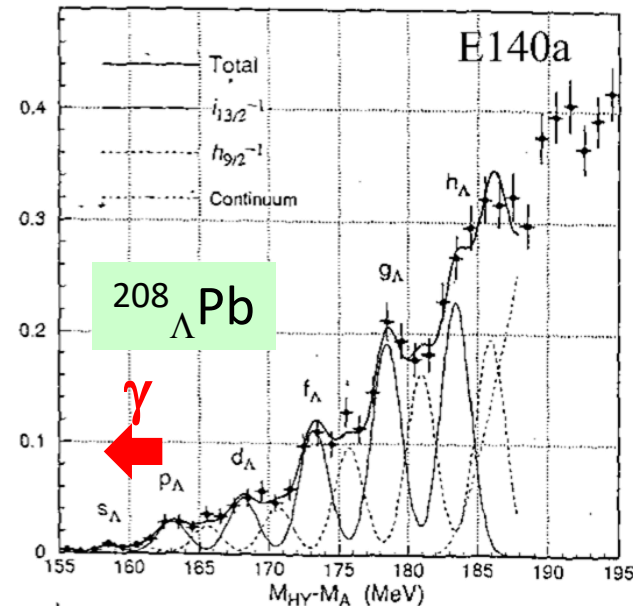
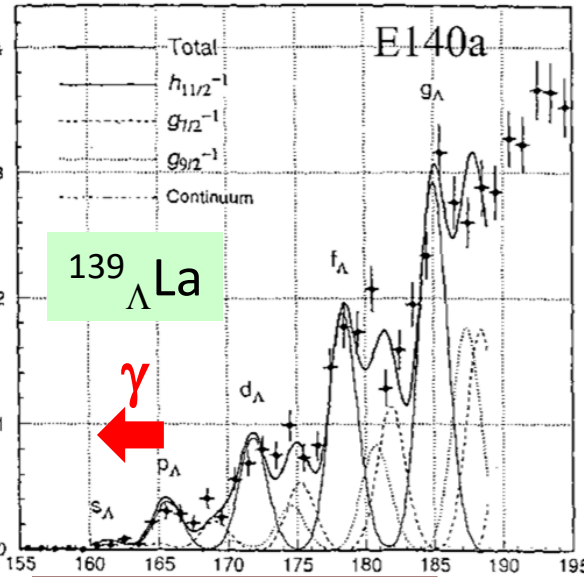
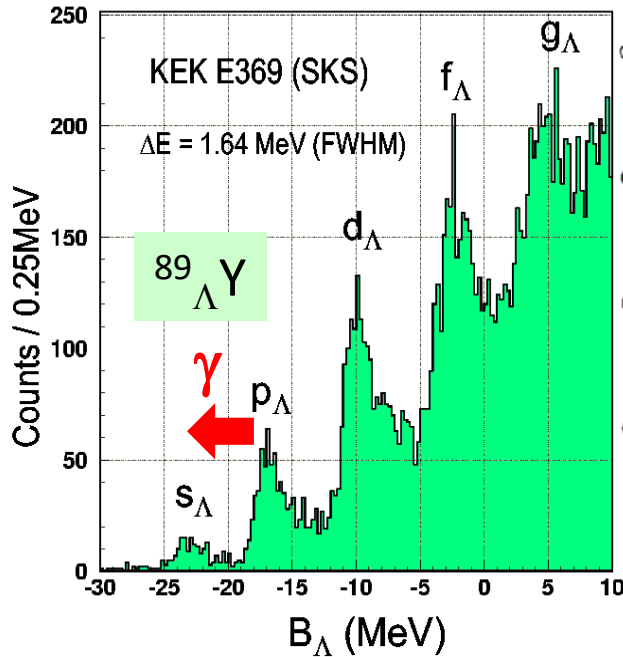
Probably, we can clearly assign transitions, even when several peaks are observed, from angular distribution and intensity combined with reliable calculations of hypernuclear structure and reactions.

# Heavy hypernuclei

$^{89}\text{Y}(\pi^+, K^+) ^{89}_{\Lambda}\text{Y}$

$^{139}\text{La}(\pi^+, K^+)_{\Lambda}^{139}\text{La}$ ,  $p_{\pi} = 1.06 \text{ GeV}/c$

$^{208}\text{Pb}(\pi^+, K^+)_{\Lambda}^{208}\text{Pb}$ ,  $p_{\pi} = 1.06 \text{ GeV}/c$



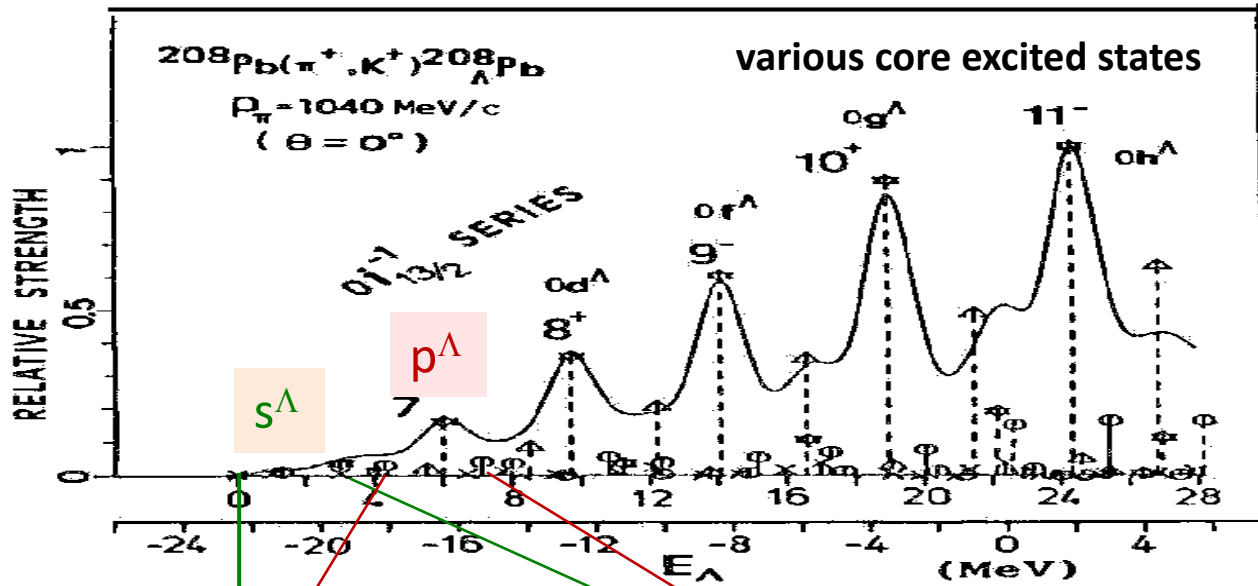
Hasegawa

$(\pi^+, K^+)$  reaction

KEK E140a, K6+SKS

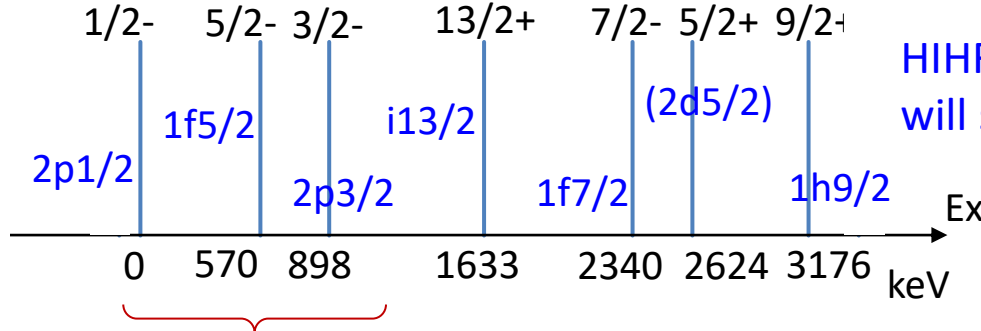
**Detailed low-lying level schemes are important for measurement of  $\Lambda$ 's single particle energies with HIHR.**

# In the case of $^{208}_{\Lambda}\text{Pb}$



core state  
 $^{207}\text{Pb}$

hole state



HIHR (300 keV resolution)  
 will separate these peaks.

**Gamma-ray data is desired to decompose the doublet and assign these low-lying levels**

# What to be studied for a proposal

- K1.1(SKS) or K1.8(S-2S)?  
1.8 GeV/c (K-,pi-) may be better for higher momentum transfer
- Realistic estimates of gamma-ray yields

## Request to the theorists

- How reliably the density dependence of  $\Lambda N$  force ( $\Lambda NN$  force) can be derived from  $p_{\Lambda}$ - $s_{\Lambda}$  spacings?  
Effects of nuclear deformation and level structure?
- What we can extract from spin-orbit splitting of various heavy  $\Lambda$  hypernuclei?
- Realistic calculations of level schemes and cross sections of medium/heavy hypernuclei necessary.