

Oh The Humanity! What Have You Done To The MLU!?

MLU Functions in the Tritium Cycle

Evan McClellan

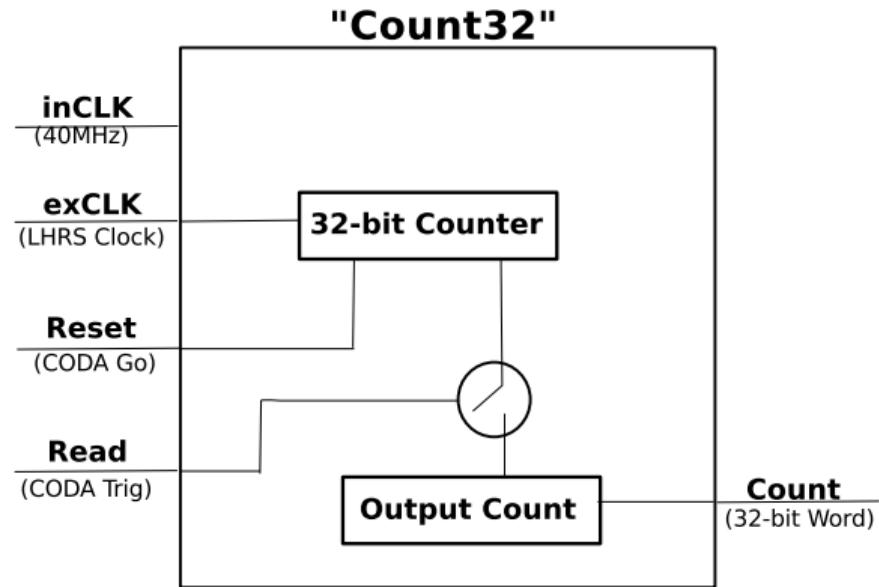
February 2, 2018

Fast Clock Counter

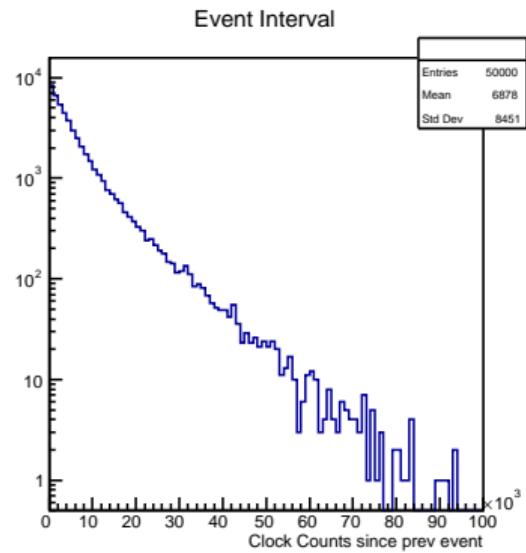
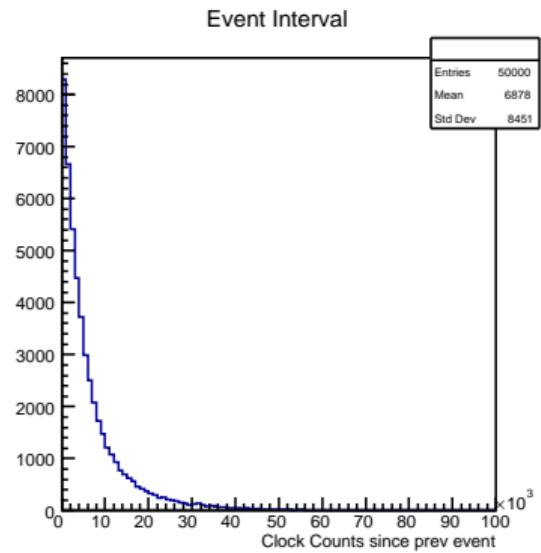
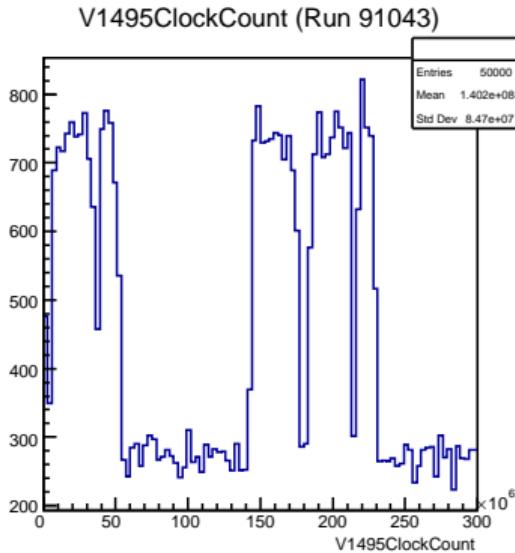
- Count LHRS clocks since start of run
- Read-out every physics event
- LHRS clock frequency = 103 kHz
- Two-Arm event syncing, inter-event duration, etc.

Register Size

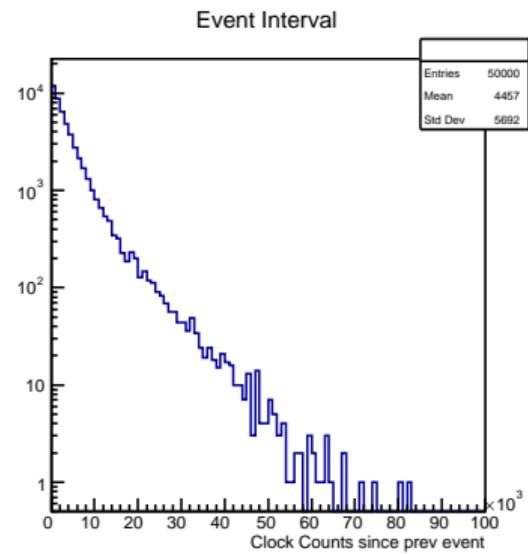
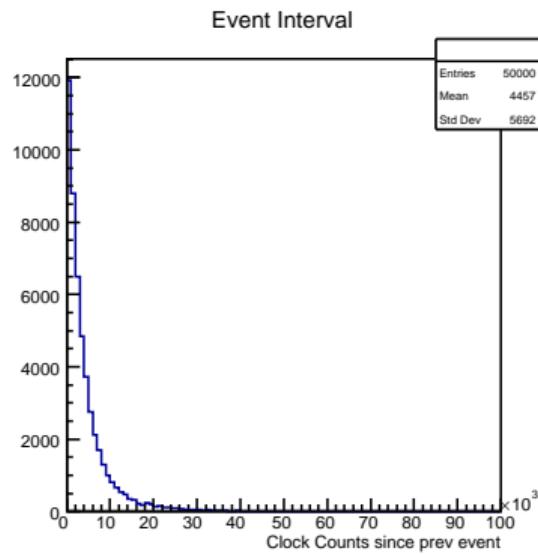
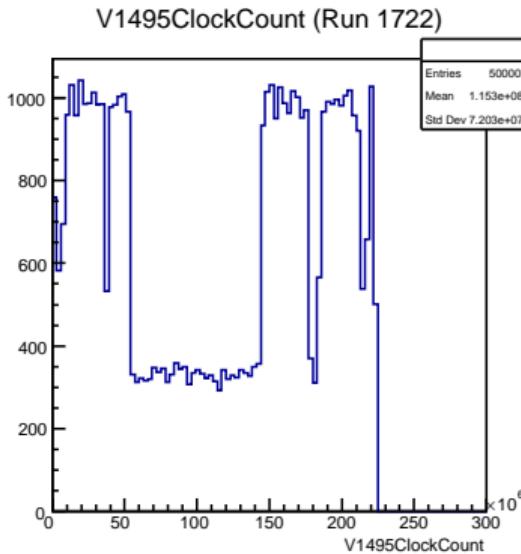
nbits	Period
16	0.64 s
32	11.6 hr
48	86.7 yr
64	5.68 Myr



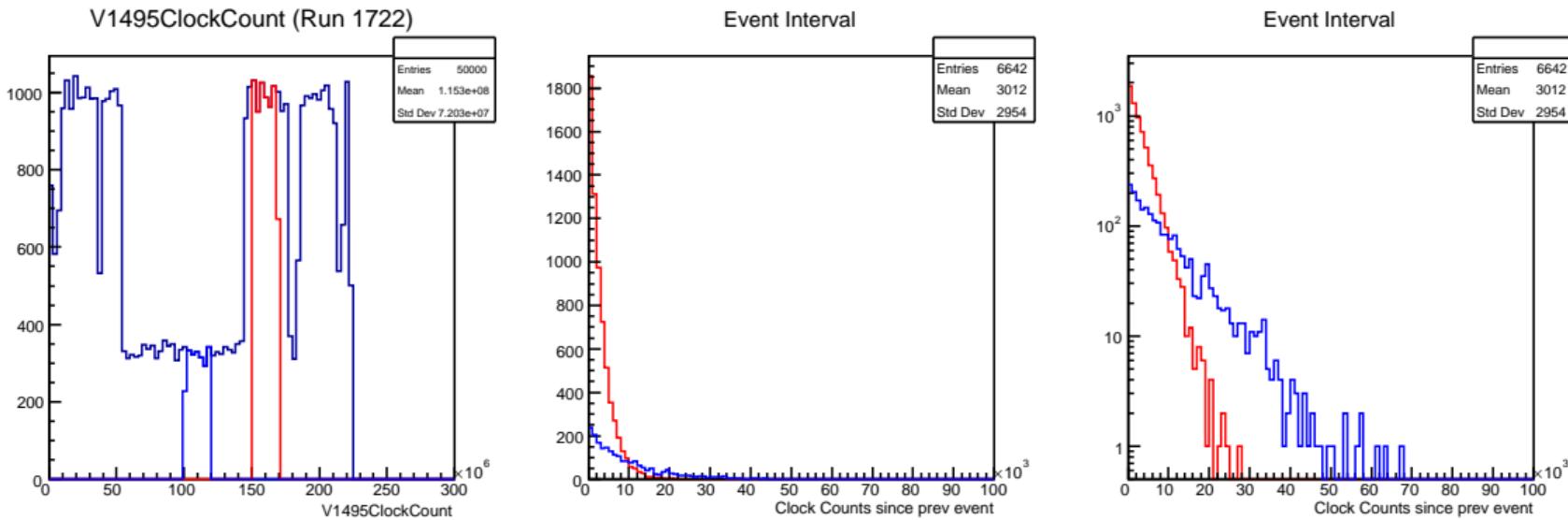
Clock Counter Data (RHRHS)



Clock Counter Data (LHRS)



Clock Counter Data (LHRS): Beam vs Cosmics



A Random Pulser in Programmable Logic

Linear Feedback Shift Registers, Inverse Transform Sampling, and Rational Function Fitting,
Oh My!

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Why make a Fast Random Trigger?

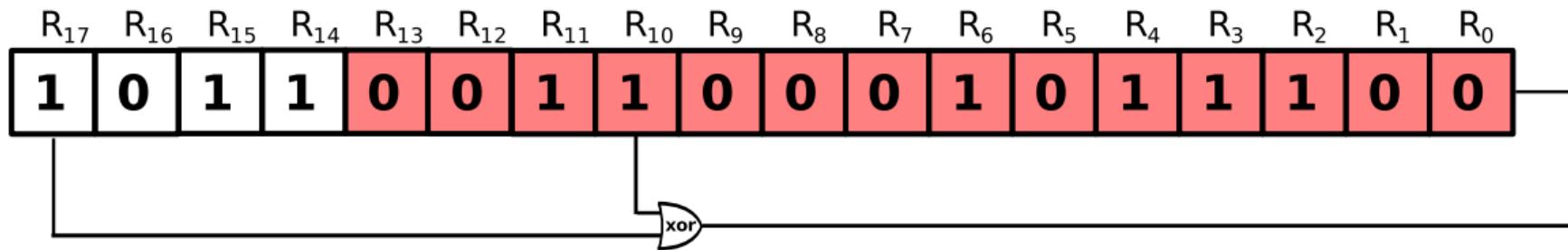
Accurate deadtime vs rate mapping without beam
(less accurate if read-out is zero-suppressed)

What is a Linear-Feedback Shift Register?

Pseudo-random number generator.

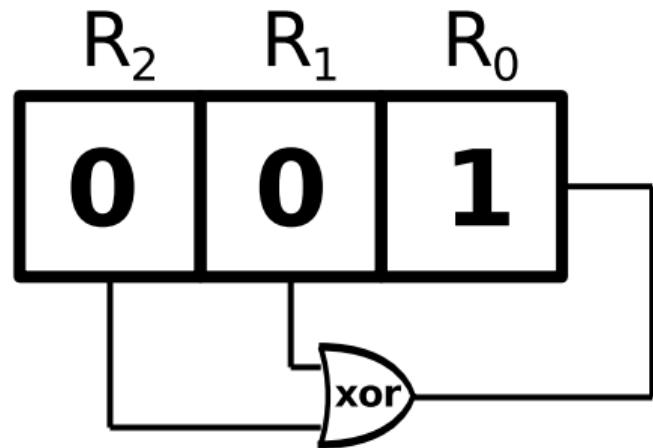
Easy to implement in hardware (programmable logic)

Used for security in GSM phones.



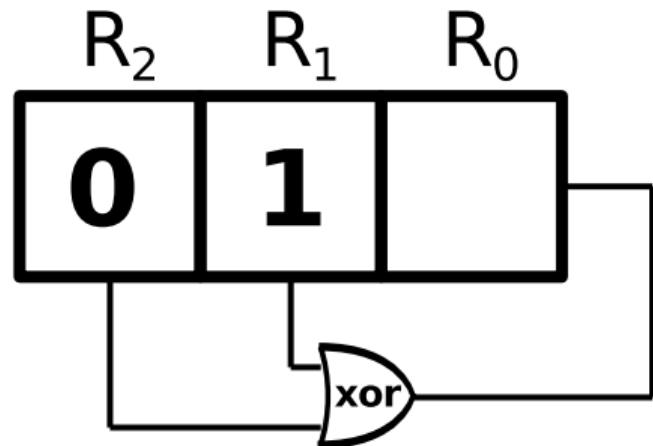
LFSR 3-bit Demo

$$R = '001' = 1$$

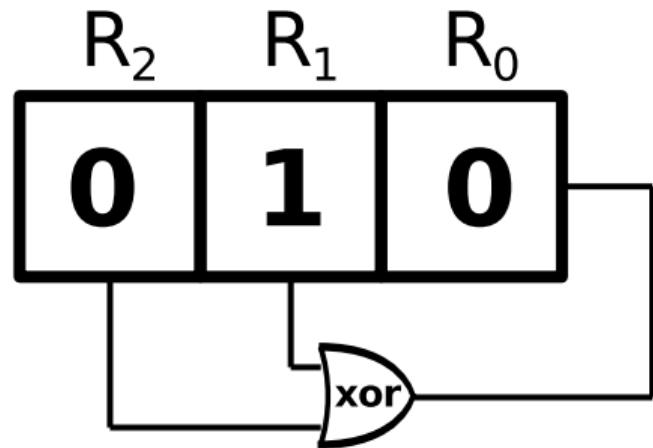


LFSR 3-bit Demo

$$R = '001' = 1$$



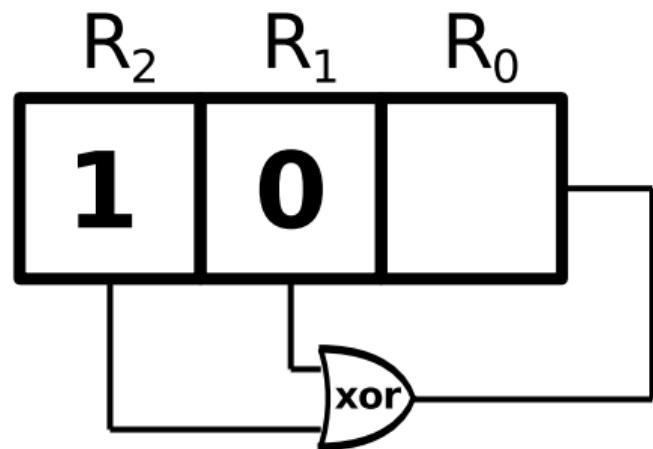
LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

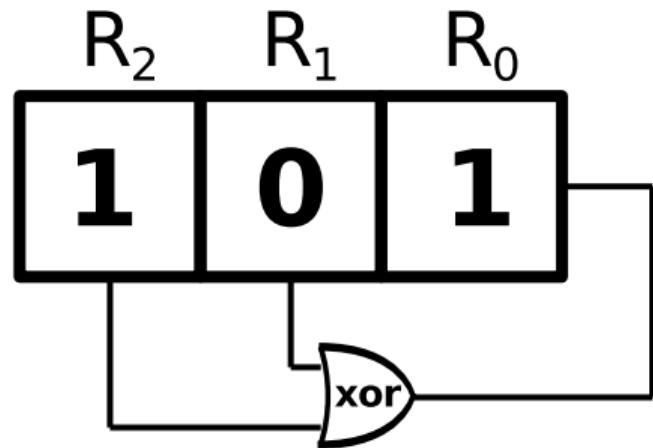
LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

LFSR 3-bit Demo

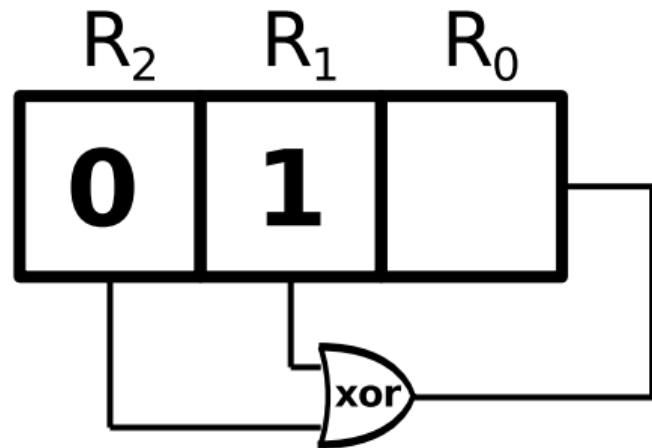


$$R = '001' = 1$$

$$R = '010' = 2$$

$$R = '101' = 5$$

LFSR 3-bit Demo

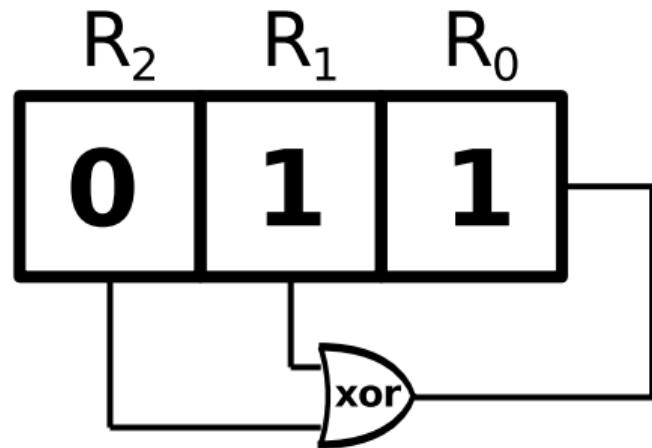


$$R = '001' = 1$$

$$R = '010' = 2$$

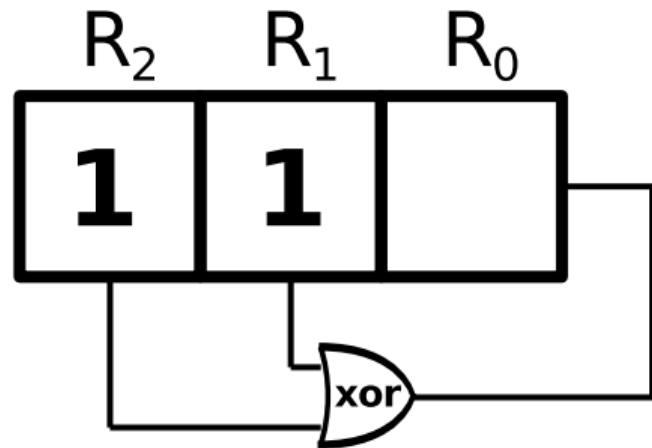
$$R = '101' = 5$$

LFSR 3-bit Demo



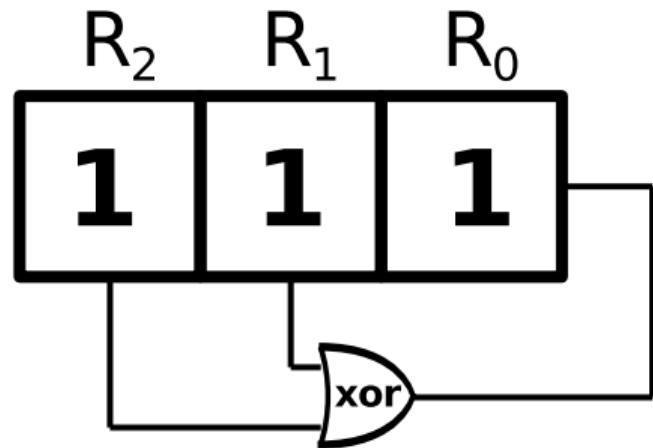
$R = '001' = 1$
 $R = '010' = 2$
 $R = '101' = 5$
 $R = '011' = 3$

LFSR 3-bit Demo



$R = '001' = 1$
 $R = '010' = 2$
 $R = '101' = 5$
 $R = '011' = 3$

LFSR 3-bit Demo



$$R = '001' = 1$$

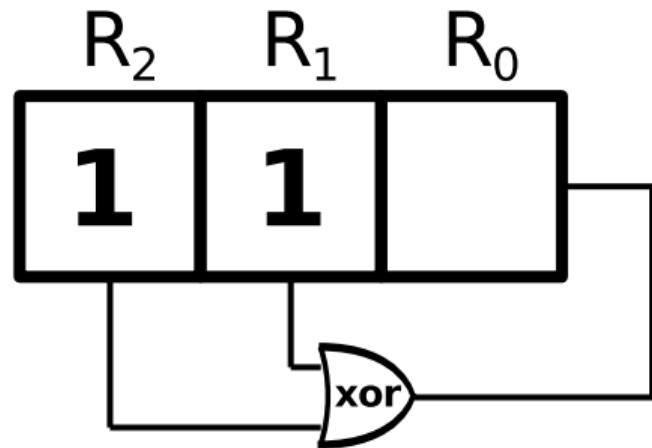
$$R = '010' = 2$$

$$R = '101' = 5$$

$$R = '011' = 3$$

$$R = '111' = 7$$

LFSR 3-bit Demo



$$R = '001' = 1$$

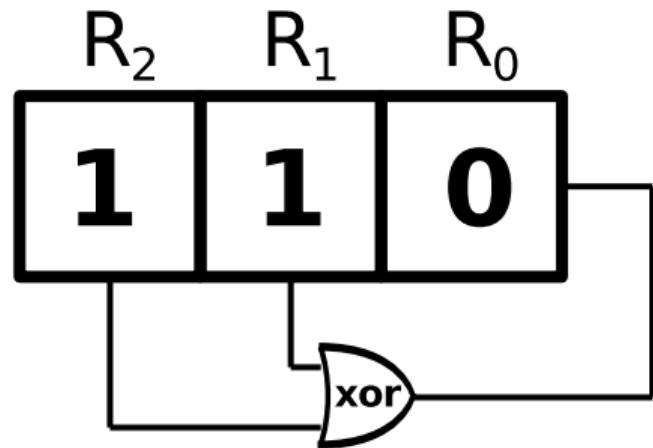
$$R = '010' = 2$$

$$R = '101' = 5$$

$$R = '011' = 3$$

$$R = '111' = 7$$

LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

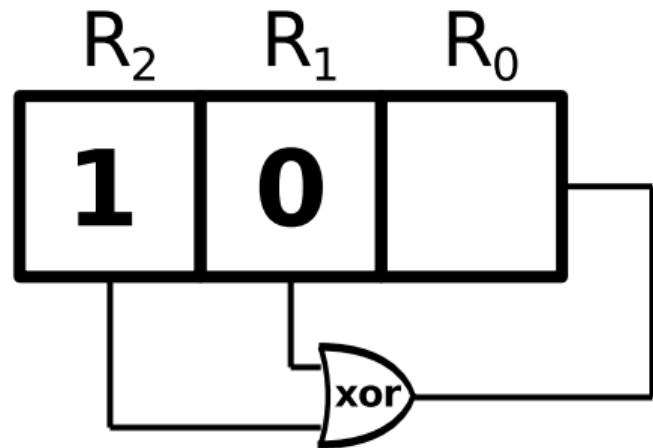
$$R = '101' = 5$$

$$R = '011' = 3$$

$$R = '111' = 7$$

$$R = '110' = 6$$

LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

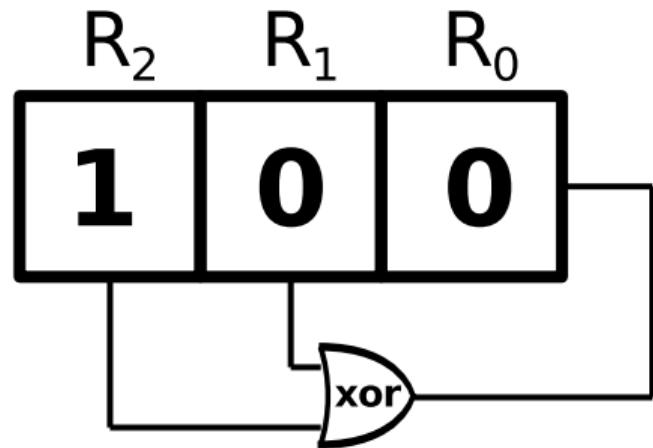
$$R = '101' = 5$$

$$R = '011' = 3$$

$$R = '111' = 7$$

$$R = '110' = 6$$

LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

$$R = '101' = 5$$

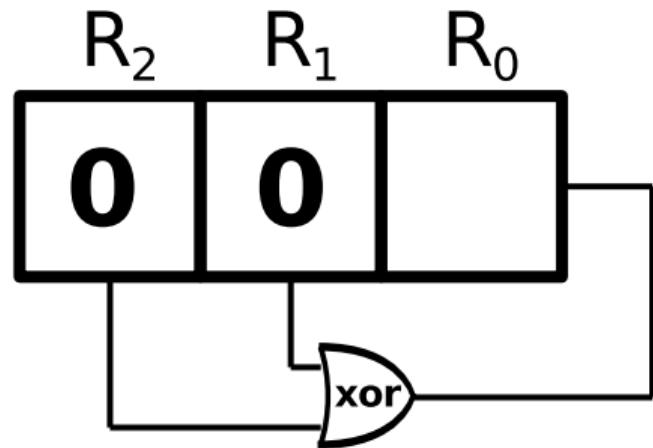
$$R = '011' = 3$$

$$R = '111' = 7$$

$$R = '110' = 6$$

$$R = '100' = 4$$

LFSR 3-bit Demo



$$R = '001' = 1$$

$$R = '010' = 2$$

$$R = '101' = 5$$

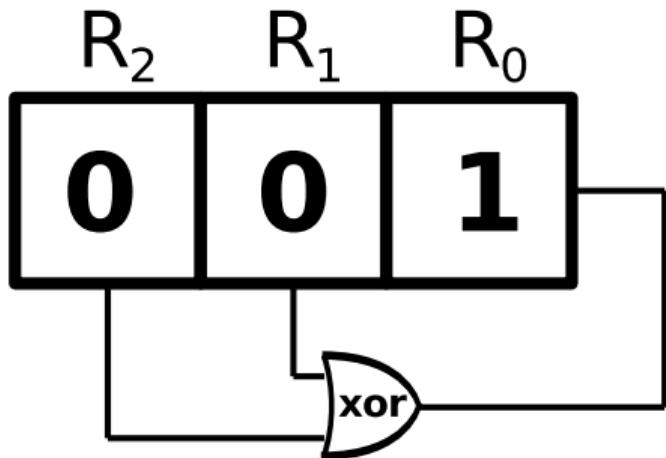
$$R = '011' = 3$$

$$R = '111' = 7$$

$$R = '110' = 6$$

$$R = '100' = 4$$

LFSR 3-bit Demo

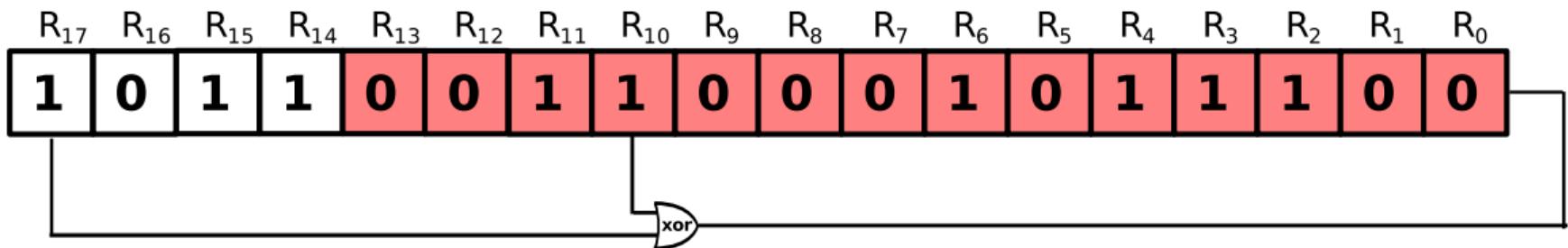


$R = '001' = 1$
 $R = '010' = 2$
 $R = '101' = 5$
 $R = '011' = 3$
 $R = '111' = 7$
 $R = '110' = 6$
 $R = '100' = 4$
 $R = '001' = 1$

13 bits and 18 bits

18-bit LFSR, lowest 13 bits used as pRNG

output range [0,8191], cycle repeats every 262143 cycles (= 6.6 milliseconds)



From Uniform pRNG to Stochastic Interval (Overkill)

What do intervals of stochastic events look like?

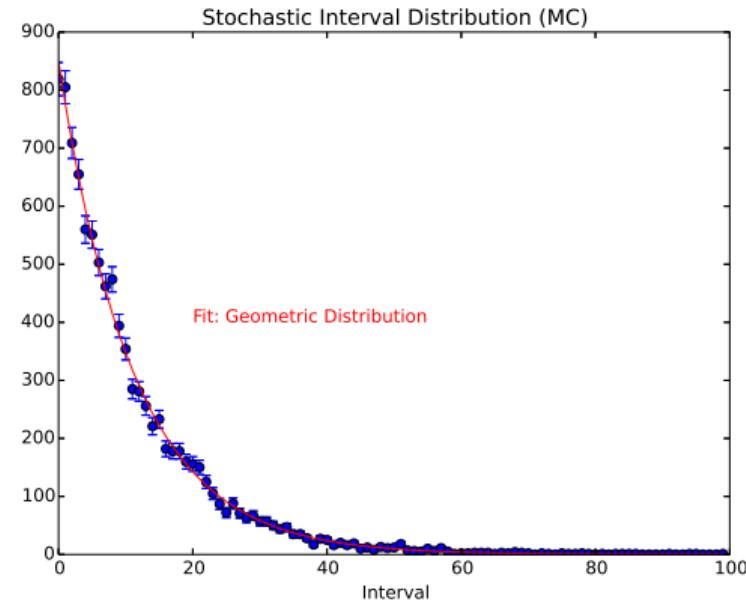
Exponential Distribution (continuous)

$$f_{pdf}(x) = \lambda e^{-\lambda x}$$

Geometric Distribution (discrete)

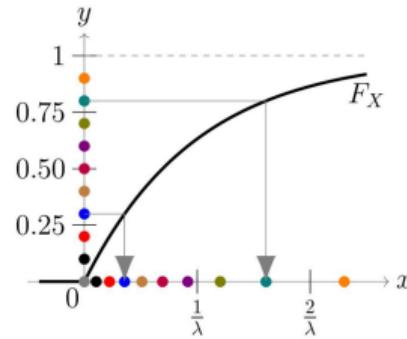
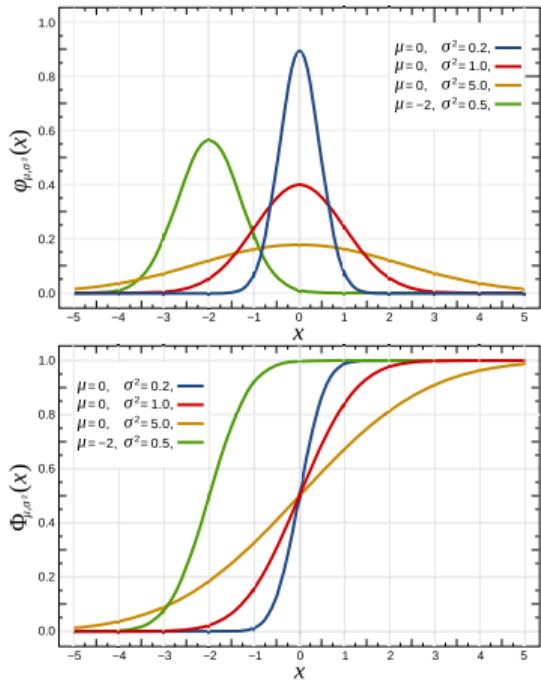
$$g_{pdf}(k) = (1 - p)^k p$$

- p : Probability of success
- k : number of failed trials



From Uniform pRNG to Stochastic Interval (Overkill)

Inverse Transform Sampling



$$f_{cdf}(x) = \int_{-\infty}^x f_{pdf}(t) dt$$

$$y = f_{cdf}(x)$$

$$x = f_{cdf}^{-1}(y)$$

From Uniform pRNG to Stochastic Interval (Overkill)

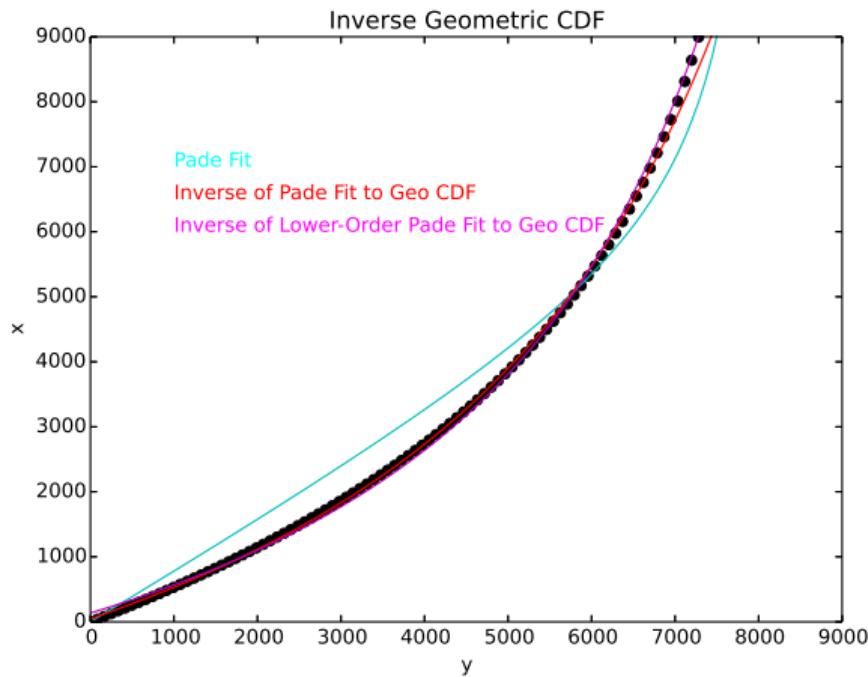
Exponents are Hard; Rational Functions are Easy!

$$g_{pdf}(k) = (1 - p)^k p$$

$$g_{cdf}(k) = 1 - (1 - p)^{k+1}$$

$$p_1(k) = \frac{a + bk}{1 + dk}$$

$$p_2(k) = \frac{a + bk}{8192 + 2k}$$



From Uniform pRNG to Stochastic Interval (Overkill)

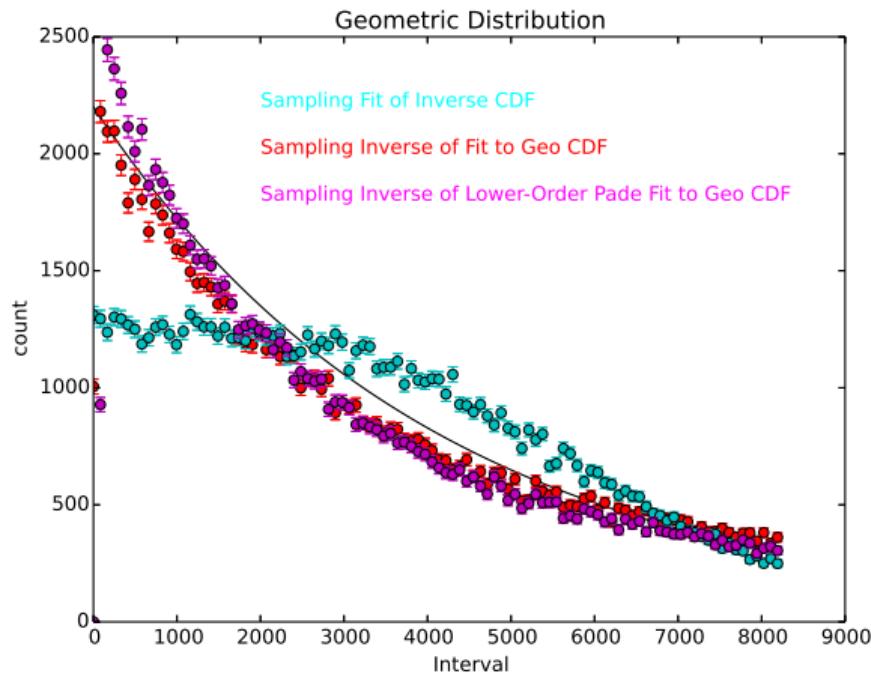
Exponents are Hard; Rational Functions are Easy!

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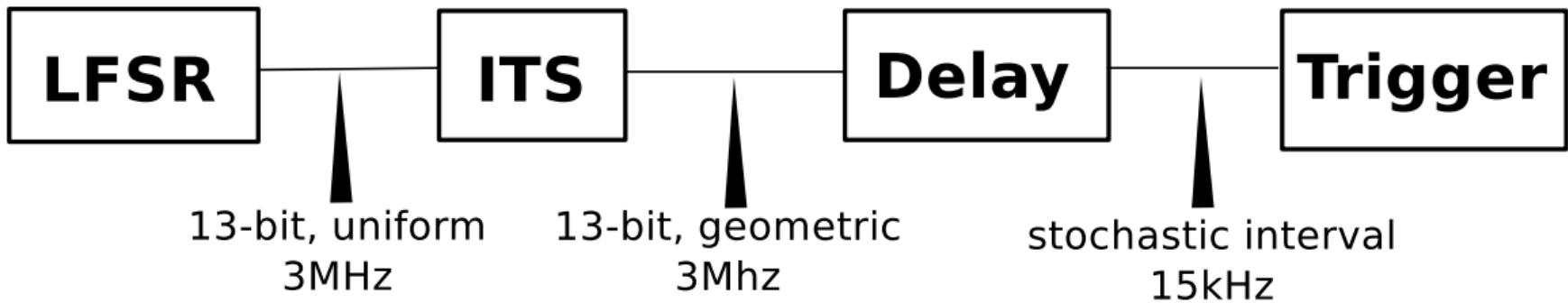
$$p_1(k) = \frac{a + bk}{1 + dk}$$

$$p_2(k) = \frac{a + bk}{8192 + 2k}$$



From Uniform pRNG to Stochastic Interval (Overkill)

Putting It All Together



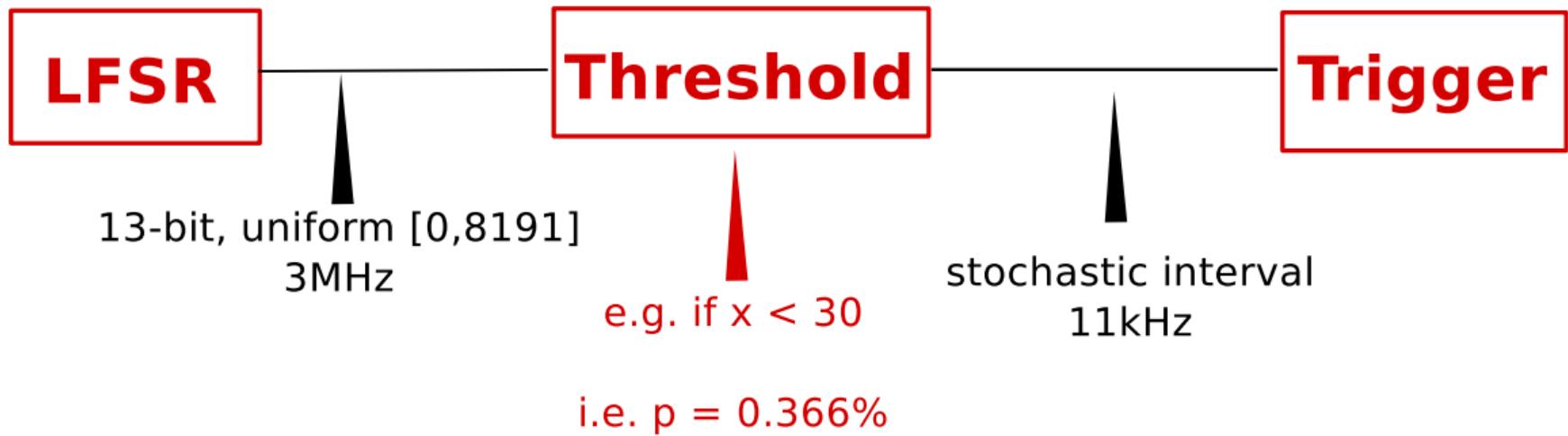
13-bit, uniform
3MHz

13-bit, geometric
3Mhz

stochastic interval
15kHz

From Uniform pRNG to Stochastic Interval (Jedi Solution)

Real-Time Stochastic Trigger Generation



The End

Thanks!