

JLab Hypernuclear Collaboration Meeting 2021

Physics Overview

${}^3_{}{}^4_{\Lambda}$ H measurement (E12-19-002)

Kyoto University, Japan

Toshiyuki Gogami

Dec 7, 2021



GRADUATE
SCHOOL OF
FACULTY OF **SCIENCE**
KYOTO UNIVERSITY



@Czech Republic (Feb 2020)

科研費
KAKENHI

SPIRITS
SUPPORTING PROGRAM FOR INTERACTION-BASED
INITIATIVE TEAM STUDIES

PROPOSAL TO JLAB PAC49

C12-19-002

High accuracy measurement of nuclear masses of Λ hyperhydrogens

T. Gogami,^{1,*} S. N. Nakamura,² F. Garibaldi,^{3,4} P. Markowitz,⁵ J. Reinhold,⁵ L. Tang,^{6,7}

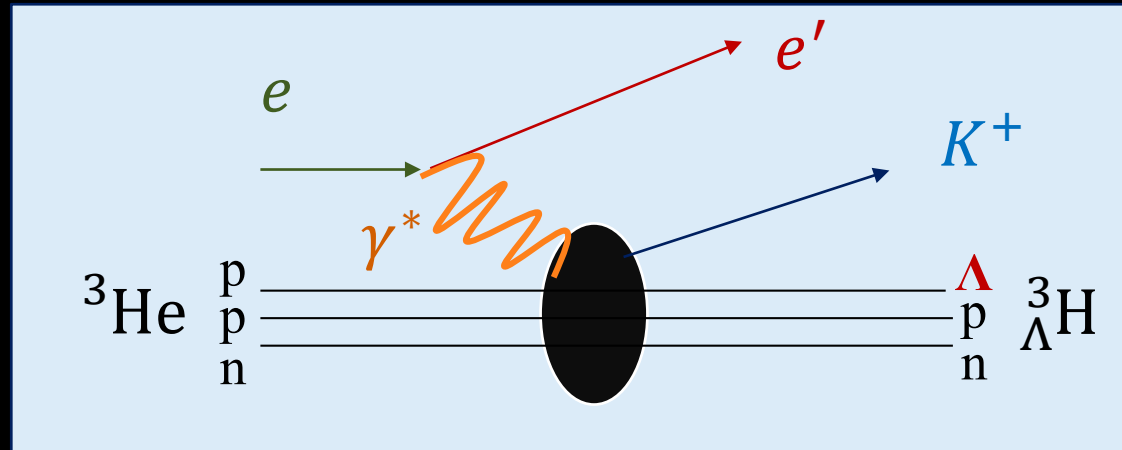
G. M. Urciuoli,³ for the JLab Hypernuclear Collaboration, and the JLab Hall A Collaboration

- 2018 LOI
- 2019 Proposal → Conditional Appr. (C2)
- 2020 Proposal → Conditional Appr. (C2)
- 2021 Proposal → **Approved** (SR = A)
(<https://www.jlab.org/physics/PAC/PAC49>)

https://www-nh.scphys.kyoto-u.ac.jp/~gogami/e12-19-002/opensrc/Proposal-C12-19-002_PAC49_submitted.pdf

Mode	Hypernucleus	Target (mg/cm ²)	Beam current (μA)	Beamtime (day)	Yield
Physics	${}^3_{\Lambda}\text{H}$	${}^3\text{He}$ (165)	50	10	600 (1/2 ⁺ , 3/2 ⁺)
	${}^4_{\Lambda}\text{H}$	${}^4\text{He}$ (228)	50	2	500 (1 ⁺)
	Subtotal			12	-
Calibration	Λ	H_2 (54)	50	1	3500
	Σ^0				1150
	${}^{12}_{\Lambda}\text{B}^{\text{g.s.}}$	Multi foil (100 × 5)	50	1	300 × 5
	-	Multi foil + Sieve slit	50	0.2	-
	-	Empty cell	50	0.1	-
	-	Empty cell + Sieve slit	50	0.2	-
Subtotal				2.5	-
Total				14.5	-

$(e, e' K^+)$ reaction



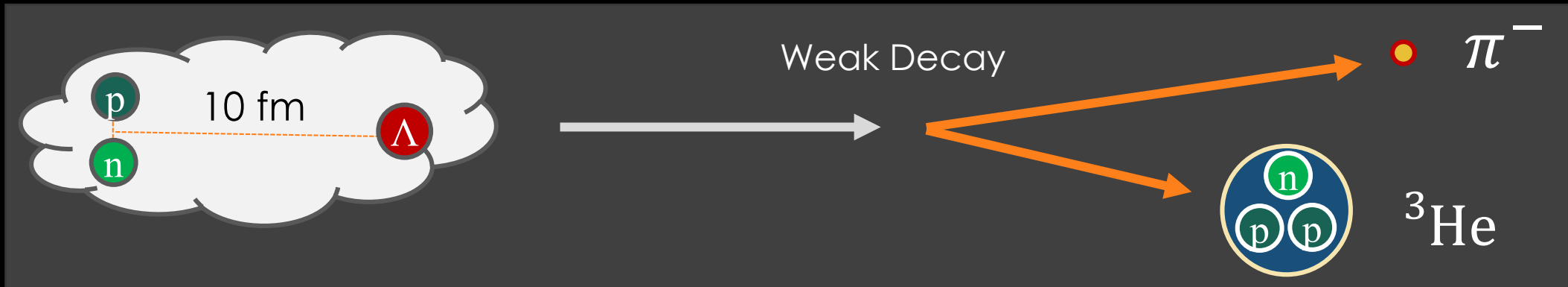
→ Missing mass spectroscopy

HYPERTRITON (${}^3_{\Lambda}\text{H}$) PUZZLE

Small B_{Λ}

vs.

Short Lifetime



$$\left\{ \begin{array}{l} B_{\Lambda} = 0.13 \pm 0.05 \text{ MeV (emulsion}^1) \\ B_{\Lambda} = 0.41 \pm 0.12 \pm 0.11 \text{ MeV (STAR}^2) \end{array} \right.$$

➔ RMS radius, $\sqrt{\langle r^2 \rangle} \cong \frac{\hbar}{\sqrt{4\mu B_{\Lambda}}}$

$$\tau = (0.5 \sim 0.92) \tau_{\Lambda}$$

(HypHI, STAR, ALICE)

Fadееv calculation with realistic NN/YN interactions

➔ $\tau = 0.97 \tau_{\Lambda}$

(H. Kamada *et al.*, *Phys. Rev. C* **57**, 4 (1998))

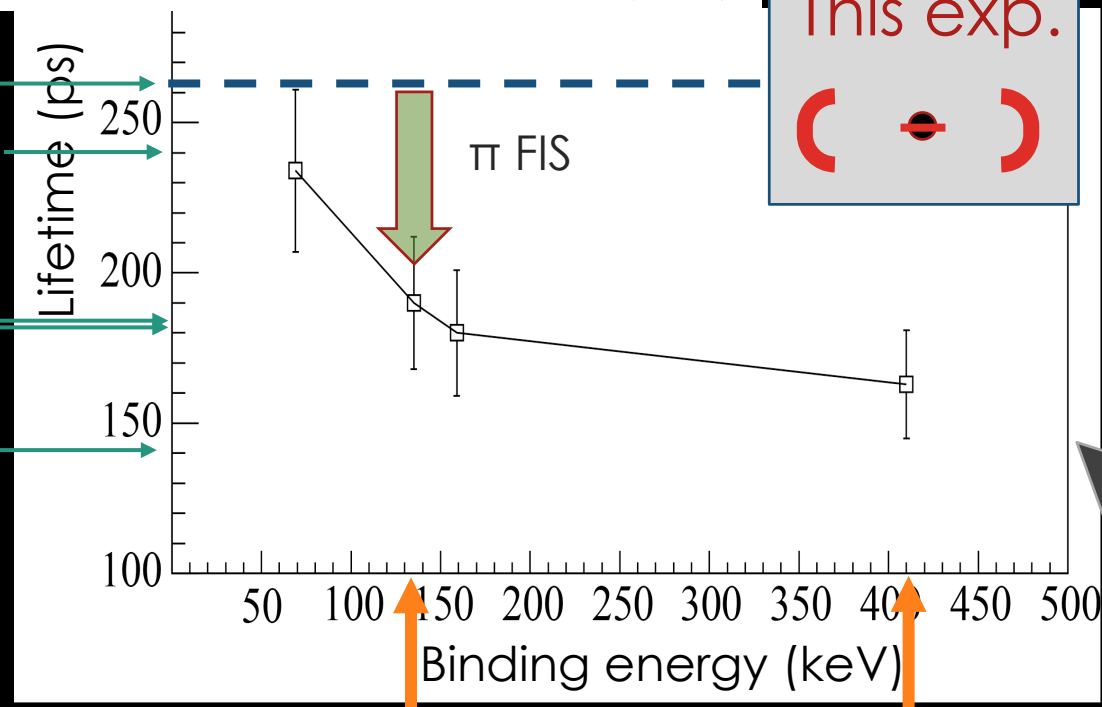
¹ M. Juric *et al.*, *Nucl. Phys. B* **52**, 1-30 (1973).

² The STAR Collaboration, *Nature Physics* (2020); <https://doi.org/10.1038/s41567-020-0799-7>

LIFETIME VS. BINDING ENERGY OF ${}^3_{\Lambda}\text{H}$

A. Pérez-Obiol et al., *PLB* 811 135916 (2020)

Free Λ
ALICE 2
HypHI
ALICE 1
STAR



Experiment	2BD (keV)	3BD (keV)
Emulsion (NPB52 (1973)1-30)	60 ± 110	230 ± 110
STAR (PRA982 (2019)811-814)	176 ± 150	586 ± 160

ex.) Decay width of 2BD channel:

$$\frac{\Gamma_{\Lambda^3\text{H} \rightarrow {}^3\text{He} + \pi^-}}{(G_F m_\pi^2)^2} \approx \frac{q}{\pi} \frac{M_{^3\text{He}}}{M_{^3\text{He}} + \omega_{\pi^-}(q)} \times \left[\mathcal{A}_\Lambda^2 + \frac{1}{9} \mathcal{B}_\Lambda^2 \left(\frac{k_{\pi^-}}{2M} \right)^2 \right] 3|F^{\text{PV}}(q)|^2$$

Spin indep. amp. Spin dep. amp. Form factor (π FSI is included)

$\propto \sqrt{B_\Lambda}$

JLab E12-19-002 Experiment:
 $|\Delta B^{\text{stat.}}| = 20 \text{ keV}, |\Delta B^{\text{sys.}}| = 55 \text{ keV}$


Great Accuracy on $B_\Lambda({}^3_{\Lambda}\text{H})$
 → Pin down the hyperon puzzle

CHARGE SYMMETRY BREAKING (CSB)


*1) T. O. Yamamoto *et al.*
(J-PARC E13 Collaboration),
Phys. Rev. Lett. 115, 222501 (2015)

*2) A. Esser *et al.* (A1 Collaboration),
Phys. Rev. Lett. 114, 232501 (2015).

${}^3\text{He}$



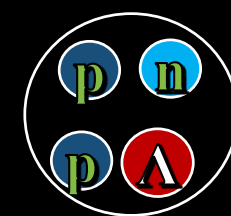
${}^3\text{H}$



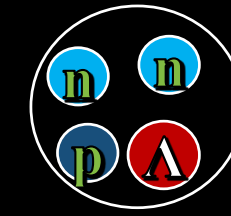
$\Delta B = 0.76384 (26)^{*1}) \text{ MeV}$
 $\Delta B_{\text{Coulomb}} = 0.683^{*2}) \text{ MeV}$
 $\Rightarrow \underline{0.081 \text{ MeV}}$

*1) J.H.E.Mattauch *et al.*, *Nucl. Phys.* 67, 1 (1965).

*2) R.A.Brandenburg, S.A.Coon *et al.*,
NPA294, 305 (1978).



${}^4\text{He}$

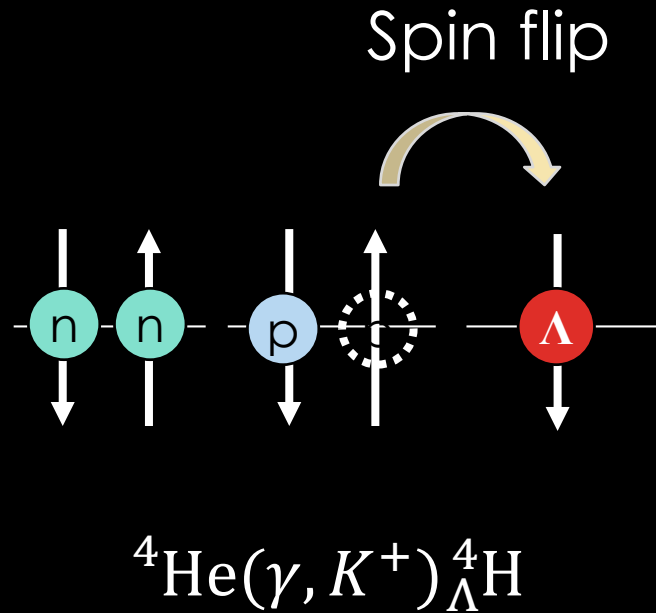


${}^4\text{H}$

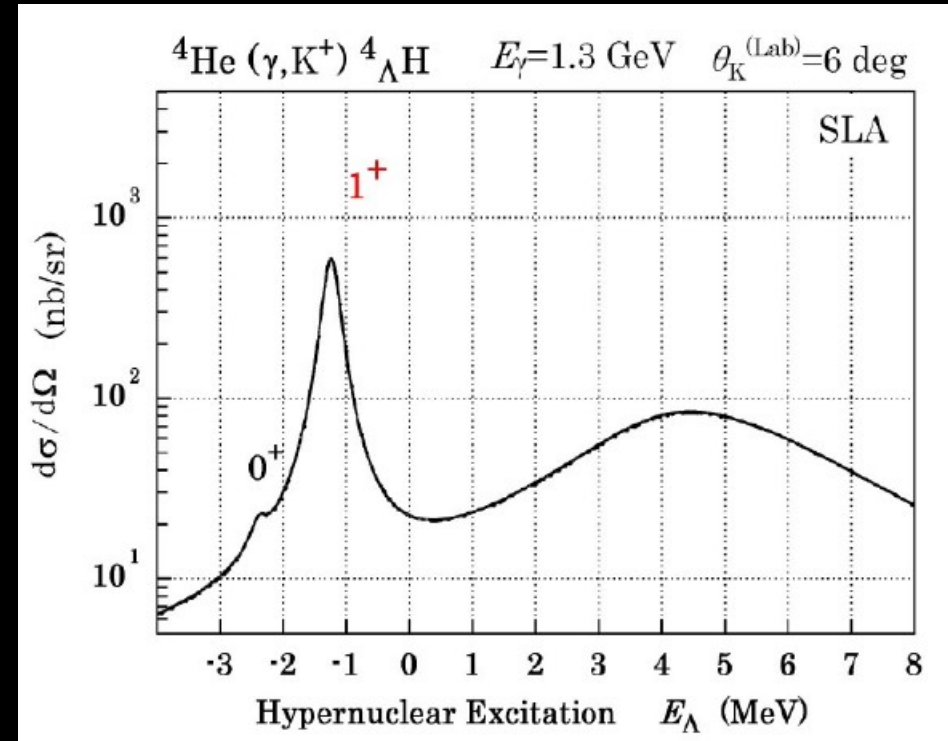
${}^3\text{He} + \Lambda$		${}^3\text{H} + \Lambda$	
$-0.98^{*1})$	1^+	-0.95	1^+
$0.03 \pm 0.05 \text{ MeV}$			
-2.39	0^+	$-2.12^{*2})$	0^+
$0.27 \pm 0.06 \text{ MeV}$			
$\Rightarrow \underline{\approx 0.4 \text{ MeV w/ correction}}$			

- Five times larger effect
- Spin dependent

Direct production of ${}^4_{\Lambda}H(1^+)$

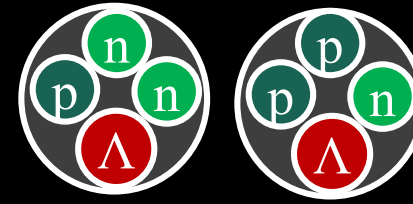


1^+ is preferably produced



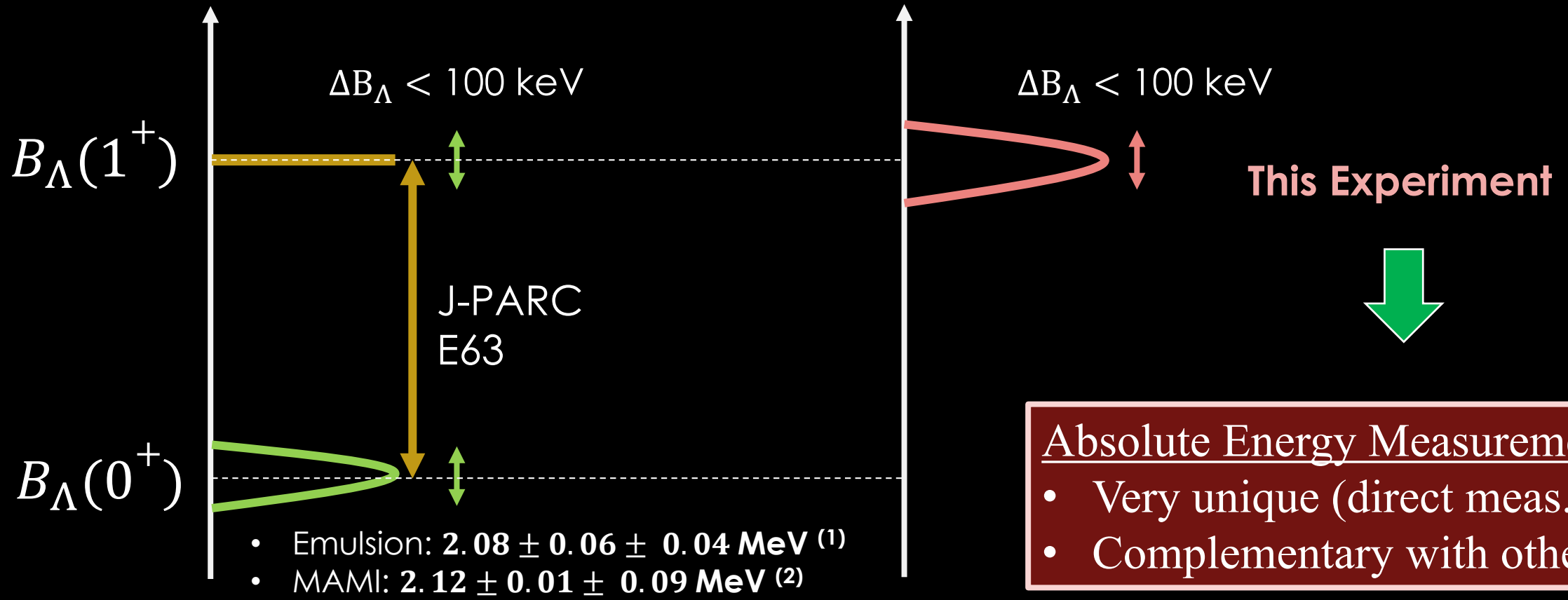
T. Motoba, JPS Conf. Proc. , 011003 (2017)

HOW WE CONFIRM THE $B_{\Lambda}({}^4\text{H}; 1^+)$



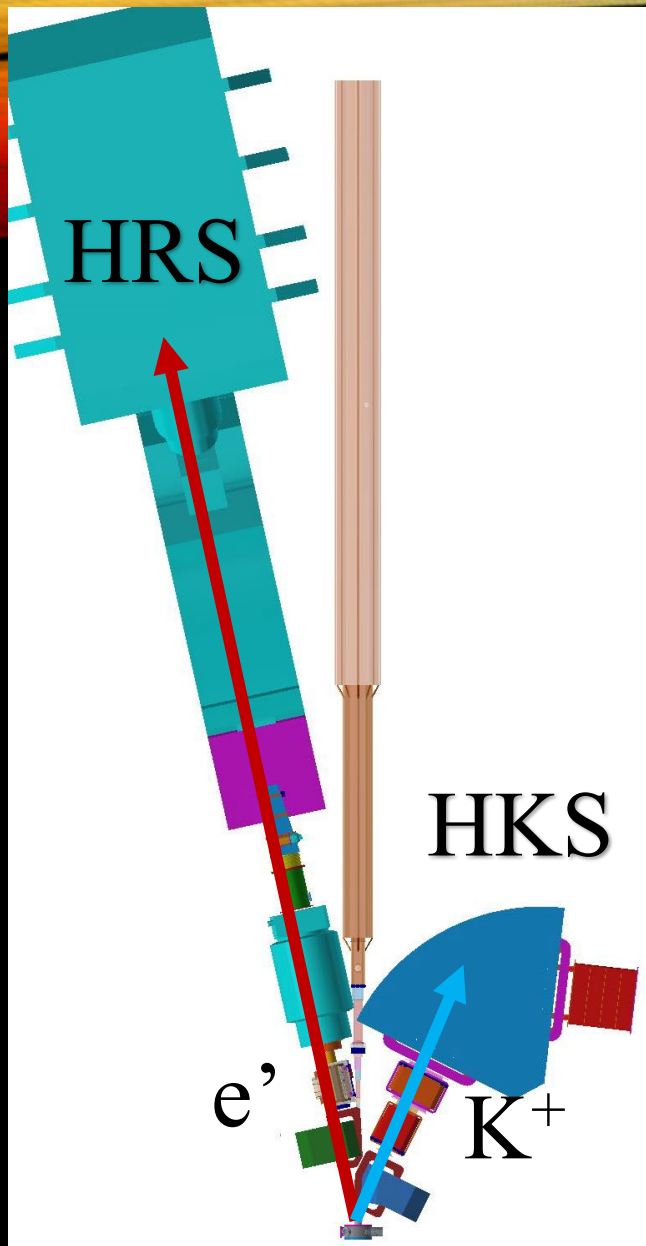
Conventional way

JLab E12-19-002

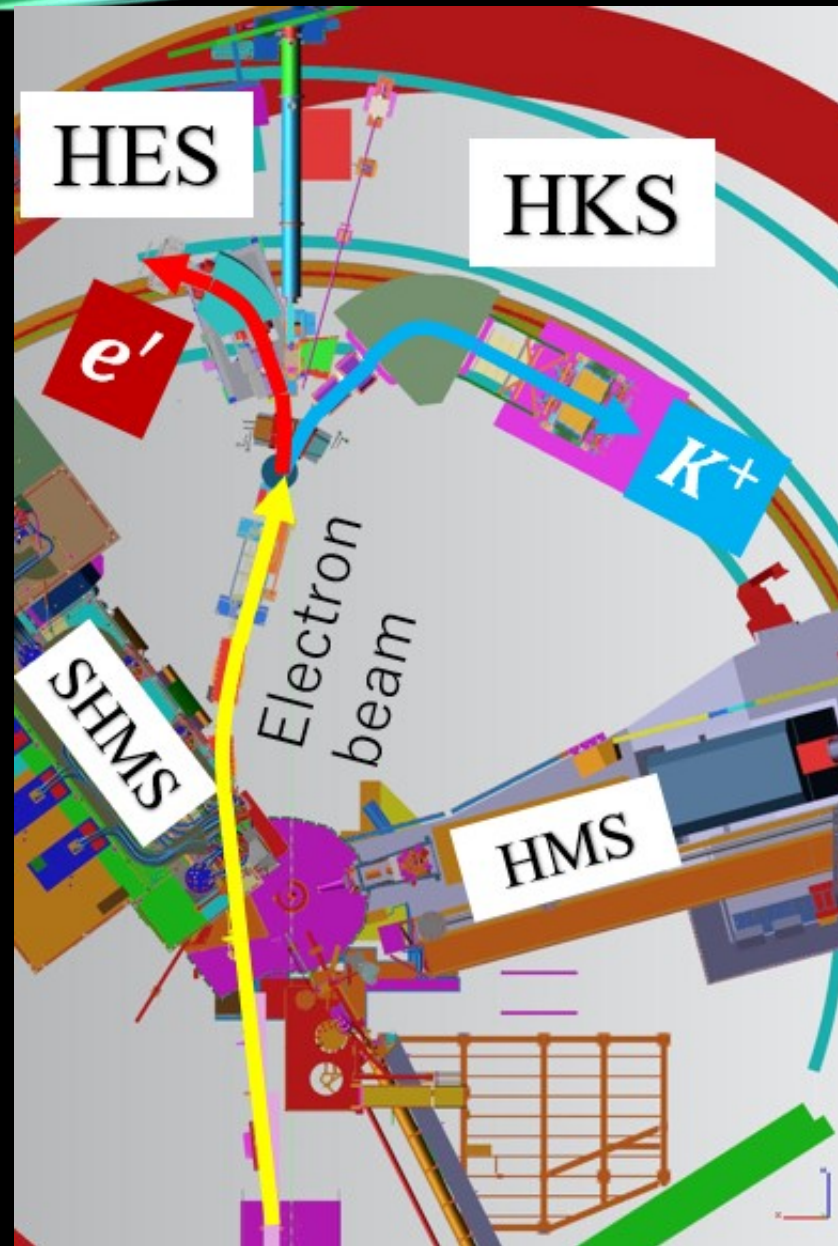


(1) NPB 52, 1-30 (1973)

(2) PRL 114, 232501 (2015)

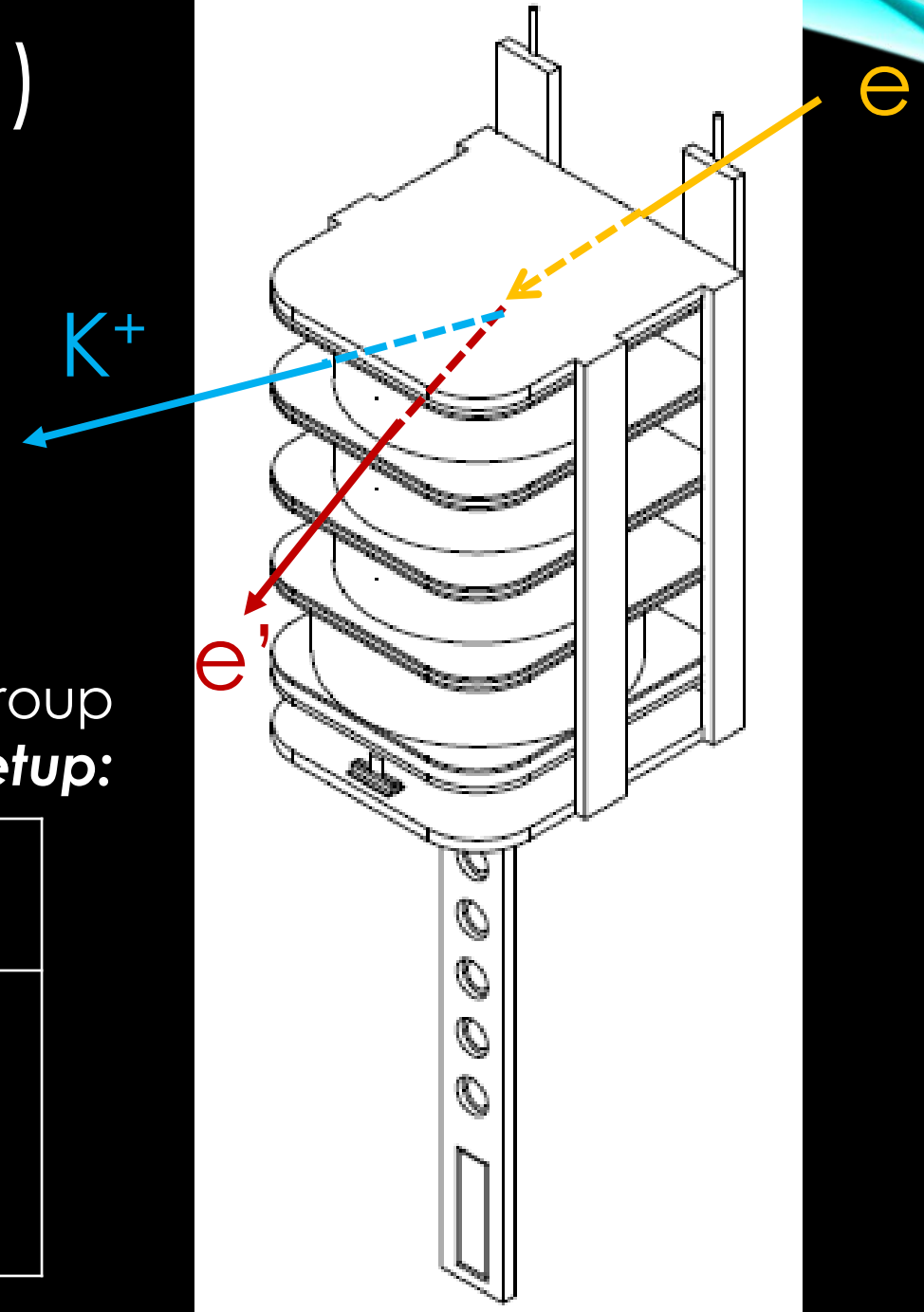
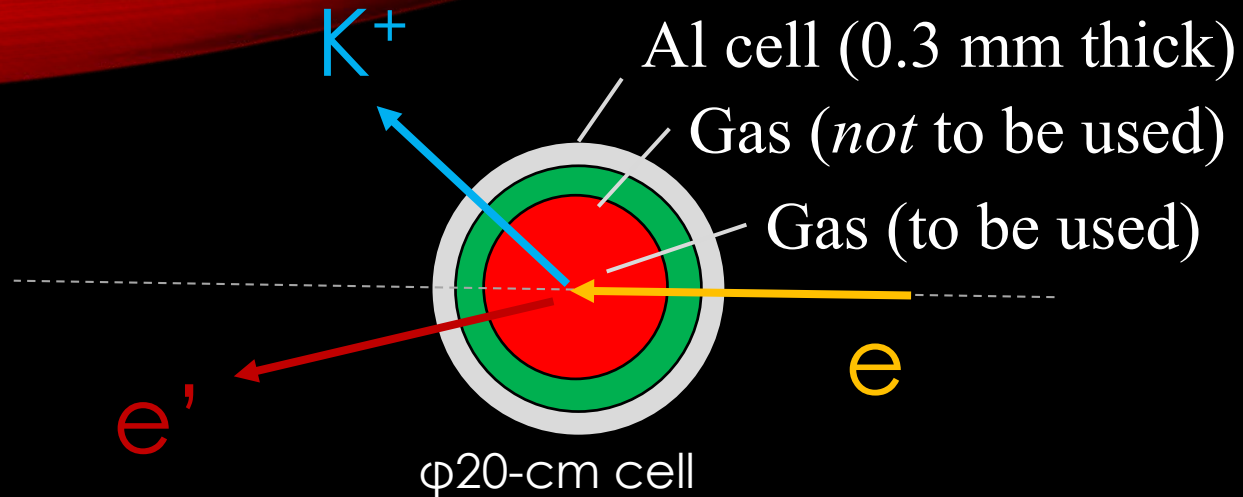


Hall A



Hall C

TARGET CELLS (TUNA CAN)



Available densities calculated by the JLab Target Group
maintaining a compatibility with our experimental setup:

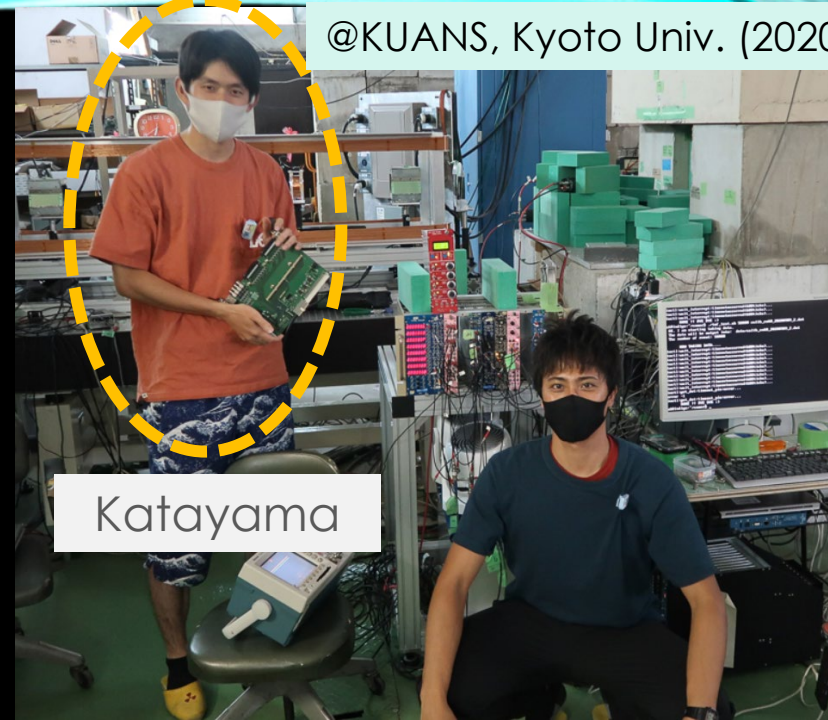
Target	Density [/(g/cm ³)]	Temperature [K]	Pressure [atm]
³ He	9.5	12	3
⁴ He	13.1		
¹ H ₂	2.8	30	

TRIGGER RATE ESTIMATION

(K. Katayama, "Development of HRS-HKS coincidence trigger with FPGA - Precise Hypernuclear Spectroscopy at JLab -", Master's Thesis, Kyoto Univ. JFY2020)

SIMULATION

Geant4 (PCS+HRS+HKS) + Physics Event Generators



Target	Thickness (mg/cm ²)	Beam Current (μA)	e' (kHz)	ρ (kHz)	π (kHz)	Acc. rate (kHz)	Acc. rate w/ Chernkovs (kHz)
¹² C	100	100	21.5	56	71	0.4	0.023
⁴⁰ Ca	100	50	64.5	48	71	1.2	0.060
²⁰⁸ Pb	100	25	97.0	22	33	0.8	0.041
³ He+ ²⁷ Al	190+162	50	90.8	163.2	252.5	3.2	0.15
⁴ He+ ²⁷ Al	262+162	50	91.2	201.6	355.9	4.9	0.23

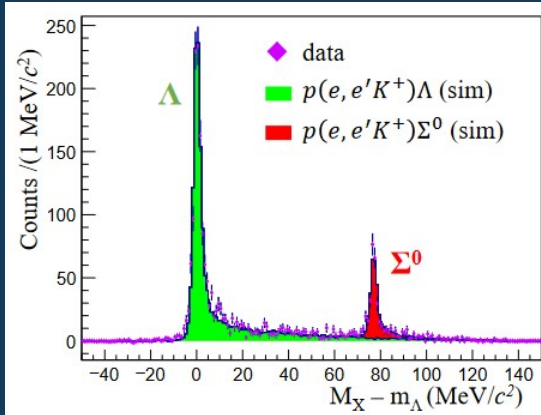
Particle identification by HKS: **TG et al., NIMA 729, 816—824 (2013).**

EXPECTED MISSING MASS RESOLUTION

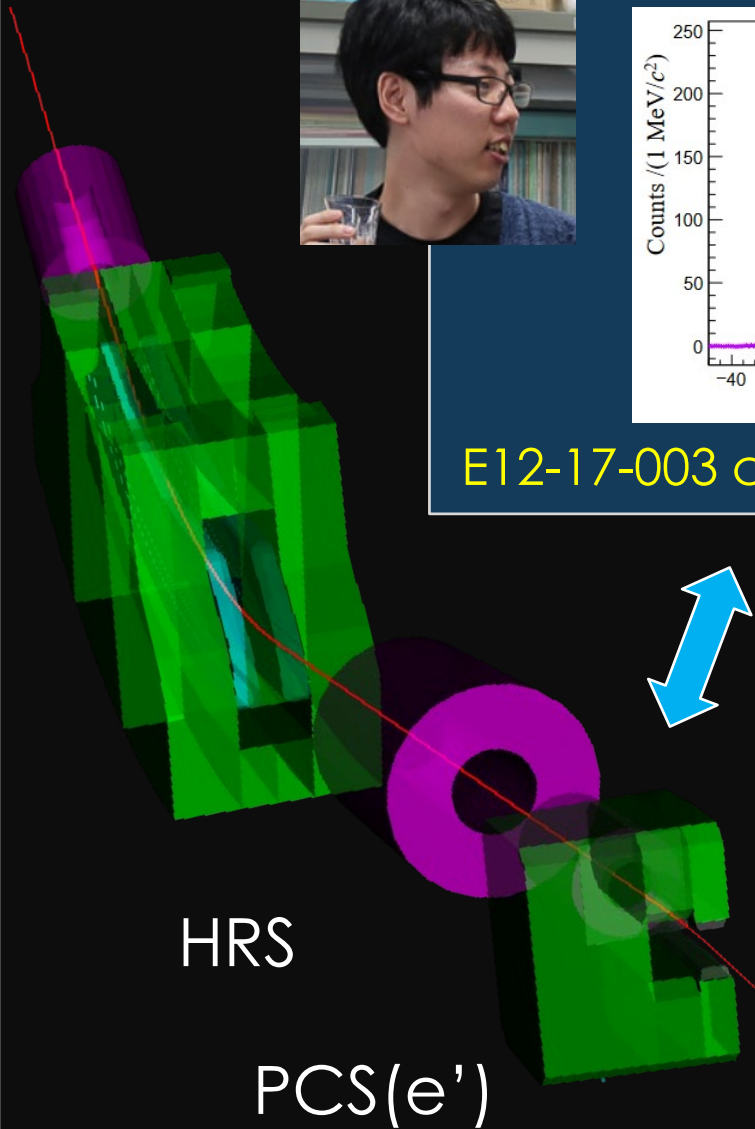


K.N. Suzuki et al., PTEP in Press (2021)

<https://academic.oup.com/ptep/advance-article/doi/10.1093/ptep/ptab158/6454035>



E12-17-003 could be reproduced



Same framework

Geant4 simulation for C12-19-002

$$Z_{T,HRS} = \sum_{i+j+k+l=0}^{n_1} a_{ijklm} x_{FP}^i x'_{FP}{}^j y_{FP}^k y'_{FP}{}^l$$

$$\overrightarrow{p}^{HRS,HKS} = \sum_{i+j+k+l+m=0}^{n_2} a_{ijklm} x_{FP}^i x'_{FP}{}^j y_{FP}^k y'_{FP}{}^l (Z_{T,HRS}^m)$$

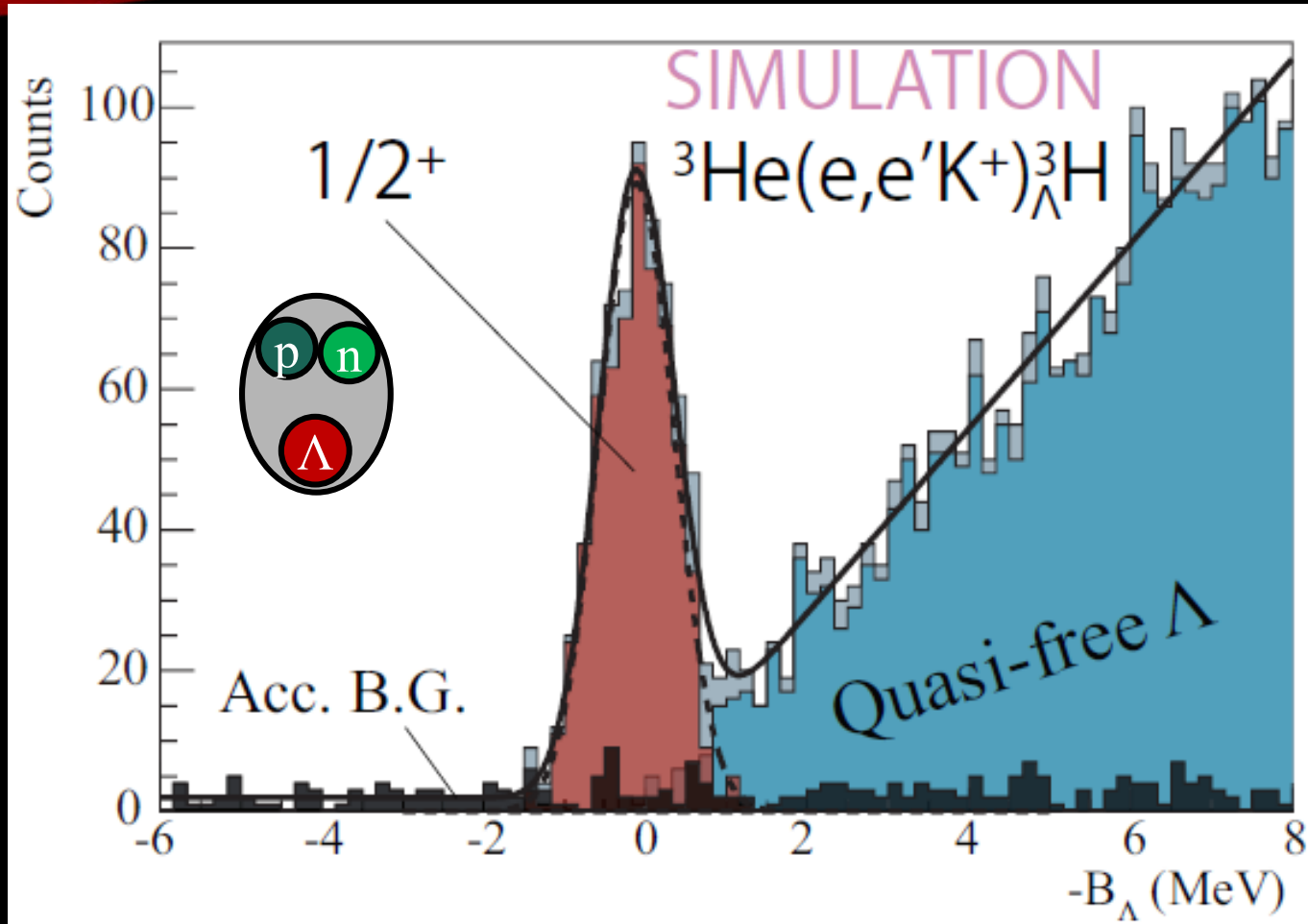
w/ materials (e.g. target cell):

Spectrometer	$\Delta p/p$ (FWHM)
HRS (e')	3.2×10^{-4}
HKS (K')	5.7×10^{-4}



$$\Delta M_{HYP} = 1.1 \text{ MeV}/c^2 \text{ (FWHM)}$$

EXPECTED SPECTRA AND STATISTICAL ERRORS



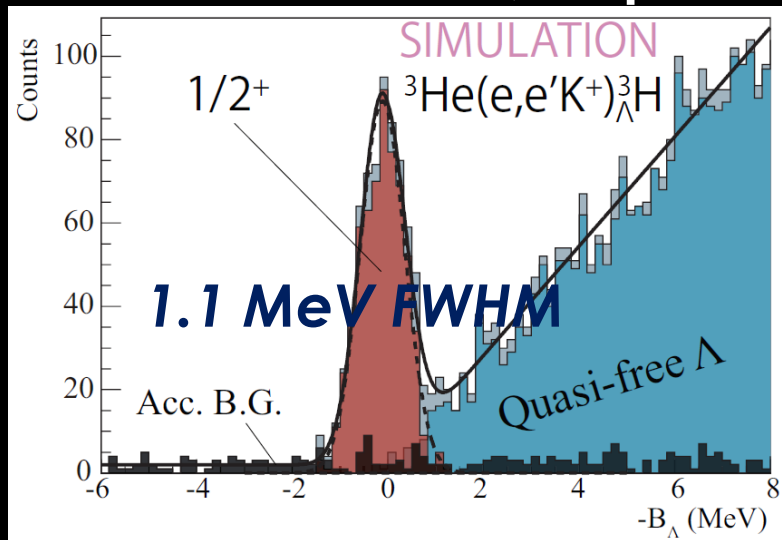
Hall A case

$$|\Delta B_\Lambda^{\text{stat.}}| = 20 \text{ keV}$$

systematic error $< \pm 60 \text{ keV}$

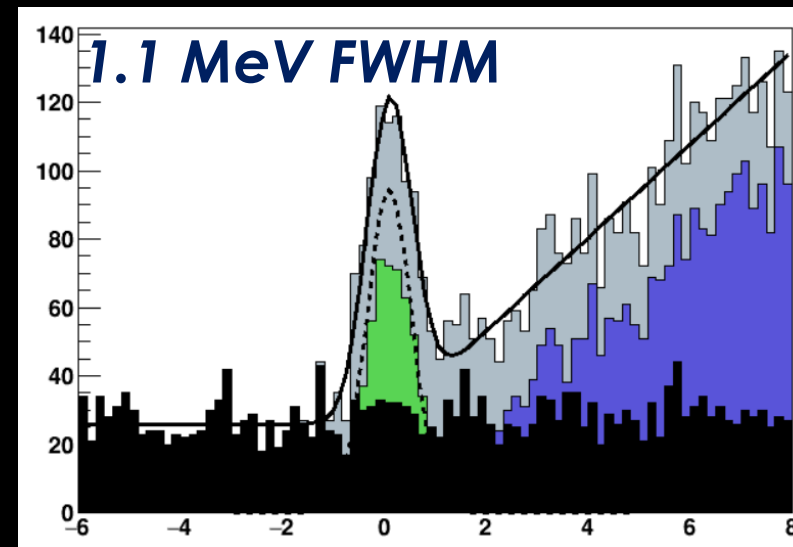
Comparison between Hall A and C

HRS-HKS @Hall A, 50 μ A



Stat. err. = 20 keV

HES-HKS @Hall C, 20 μ A

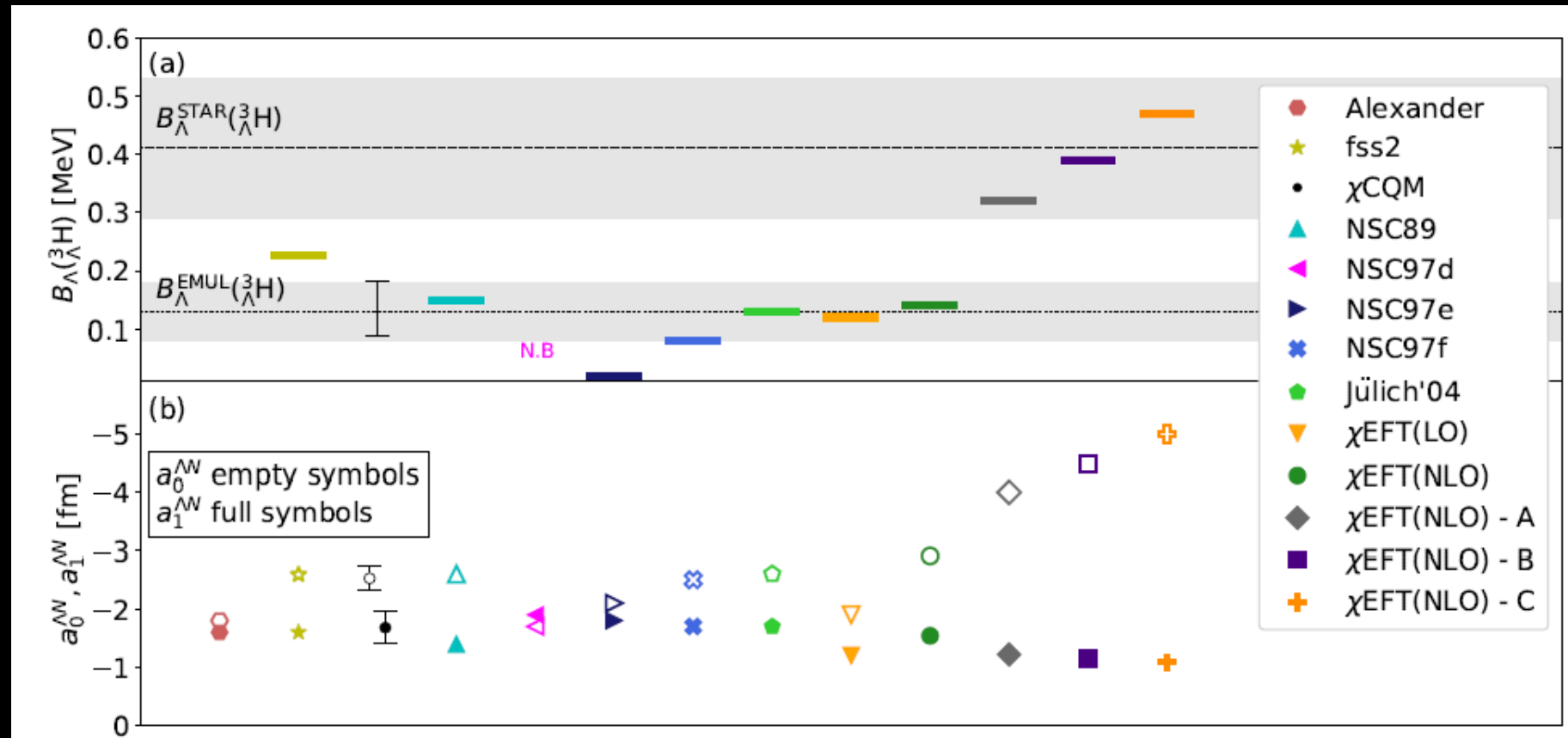


Stat. err. < 30 keV

Feasibility at Hall C is carefully being studied
(Resolution, S/N, Yield)

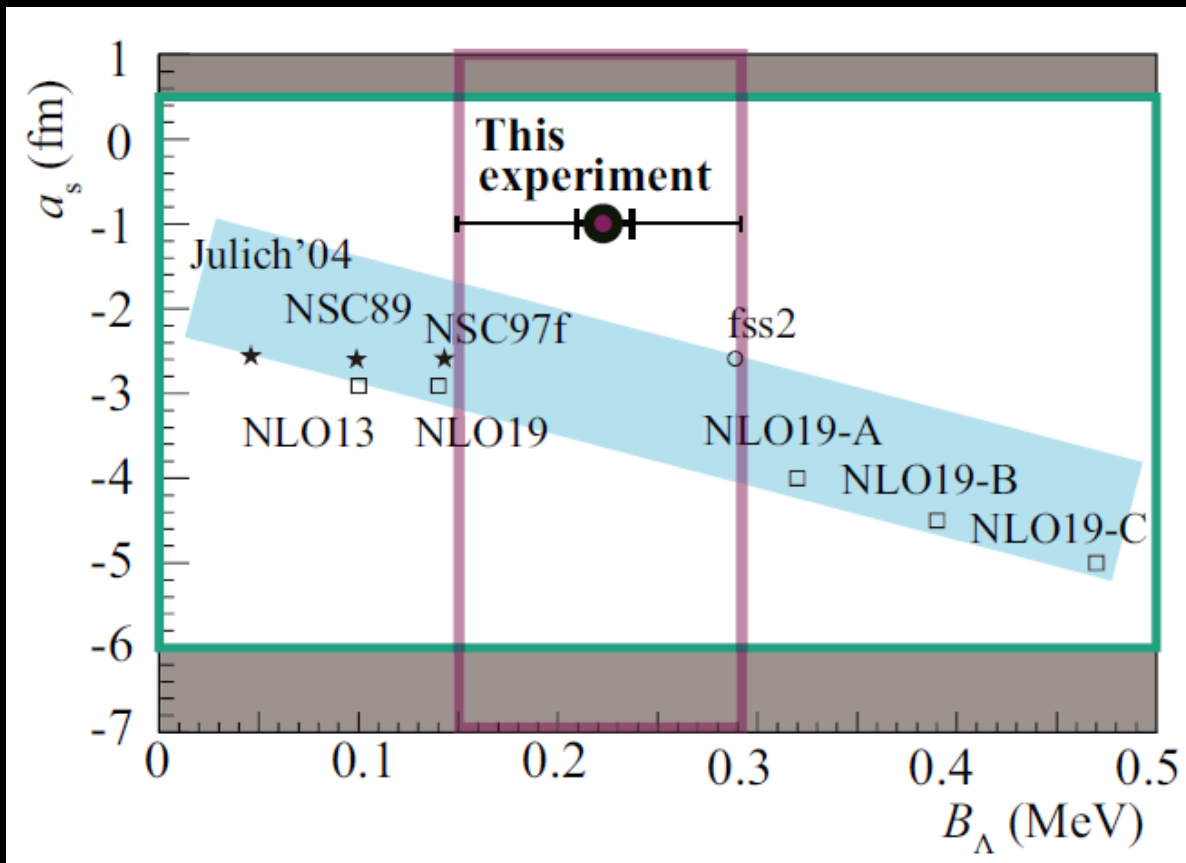
ΛN scattering length vs. B_Λ

M. Schafer et al., arXiv:2108.13900v1 [nucl-th] 31 Aug 2021





GROUND STATE OF ${}^3_{\Lambda}\text{H}$ ($T = 0, J^{\pi} = 1/2^{+}$)



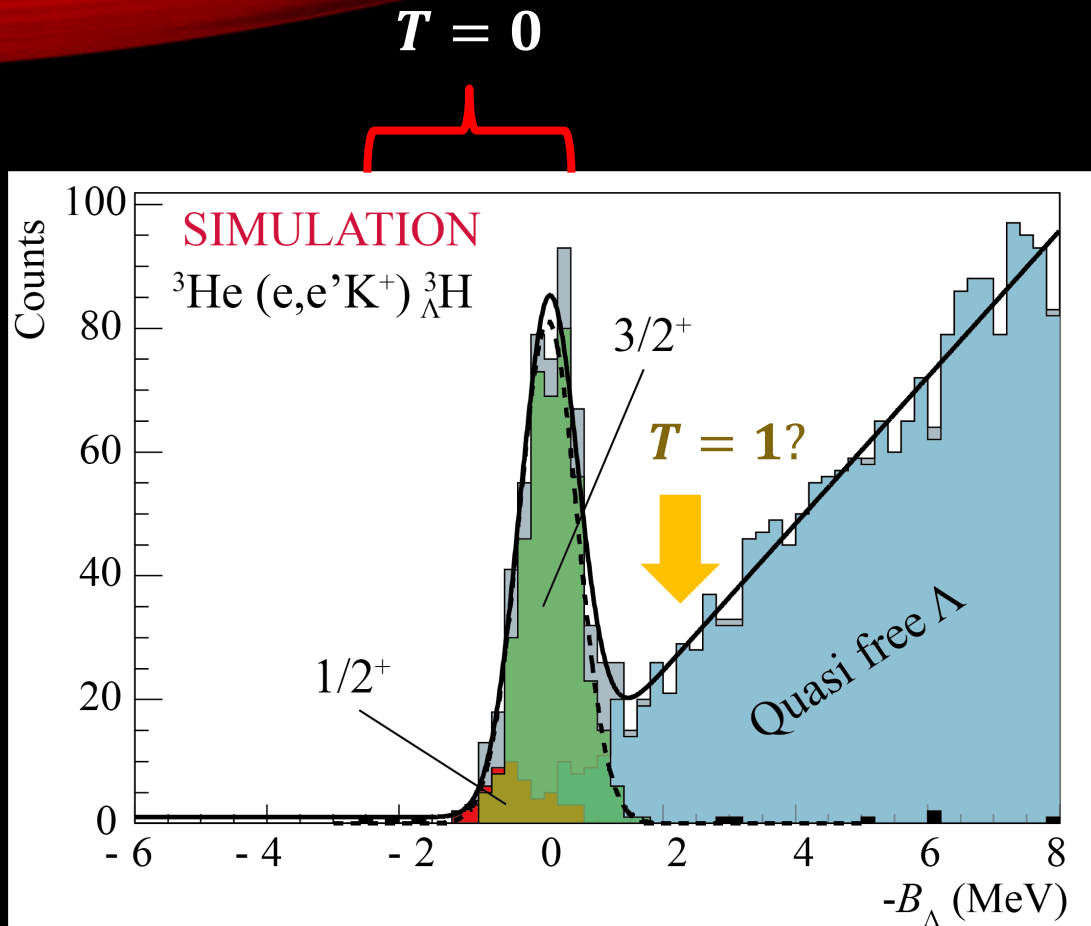
Hypertriton Puzzle

- Λ d m radius ($|\Delta r| \leq 1$ fm)
- ➔ Better estimation for the lifetime

ΛN interaction

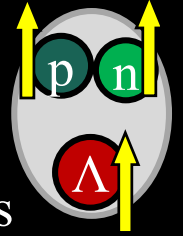
- Constraint for
 - Interaction models
 - The ΛN spin singlet scattering length ($|\Delta a_s| \sim 1$ fm; cf. $a_s = 1.8_{-4.2}^{+2.3}$ fm)

EXCITED STATES OF ${}^3_{\Lambda}\text{H}$



${}^3_{\Lambda}\text{H} (T = 0, J^{\pi} = 3/2^{+})$

- Has NOT been measured
- Hard to measure by emulsion / HI experiments
- Does it exist?
 - If yes, the CS is larger than $1/2$ by a factor of 8 ⁽¹⁾
 - If no, only the $1/2^{+}$ state will be observed
- \leftarrow $\bar{\pi}$ EFT predicts $3/2^{+}$ as a virtual state ⁽²⁾
- Strong constraint for the ΛN spin triplet interaction



${}^3_{\Lambda}\text{H} (T = 1, J^{\pi} = 1/2^{+})$

- Isospin partner of $nn\Lambda$ (and $pp\Lambda$)
 - \rightarrow significant information on the existence of $nn\Lambda$
- CSB study in the $A = 3$ hypernuclear system
- If the CS is 0.5 nb/sr $\rightarrow |\Delta B_{\Lambda}^{\text{stat.}}| \sim 90$ keV



(1) T. Mart *et al*, *Nucl. Phys. A* **640**, 235-258 (1998)

(2) M. Schäfer *et al.*, *Phys. Lett. B* **808**, 135614 (2020)

SUMMARY

HKS experiment @ Hall A/C (JLab E12-19-002)

$B_{\Lambda}({}^3, {}^4_{\Lambda}\text{H})$ measurement with the accuracy of

$$\Delta B_{\Lambda}^{\text{tot.}} = \sqrt{|\Delta B_{\Lambda}^{\text{sys.}}|^2 + |\Delta B_{\Lambda}^{\text{stat.}}|^2} \simeq 60 \text{ keV}$$

→ Hypertriton puzzle / CSB

(complementary with MAMI and J-PARC measurements)



2019



2017



2018



No chance in 2020, 2021...

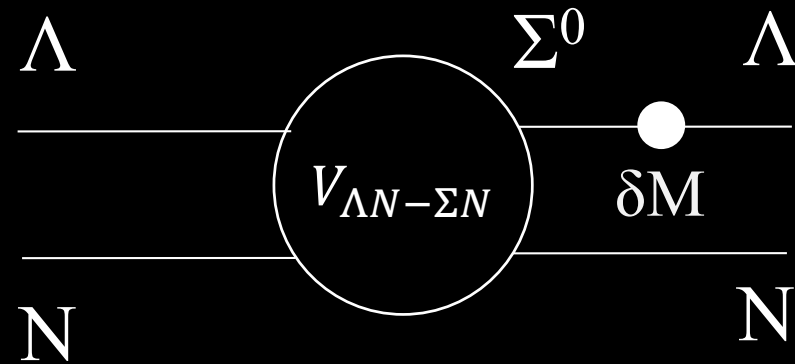
We want to resume preparation in 2022!



BACKUP

ΛN - ΣN COUPLING

A. Gal, Phys. Lett. B 744, 352 (2015)



$$\langle N\Lambda | V_{CSB} | N\Lambda \rangle = -0.0297 \tau_{Nz} \frac{1}{\sqrt{3}} \langle N\Sigma | V_{CS} | N\Lambda \rangle$$

Λ - Σ COUPLING

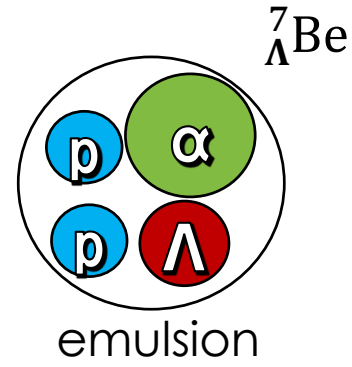
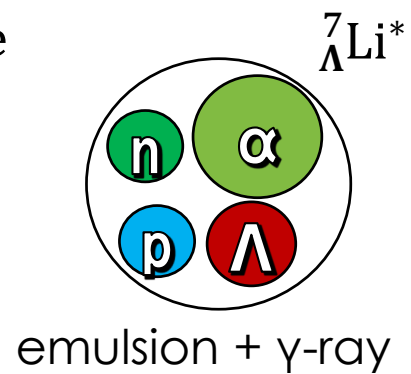
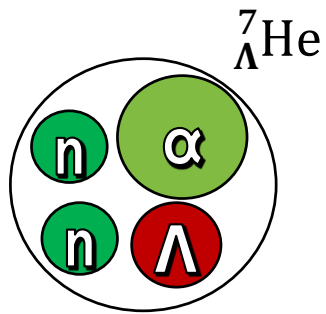
A. Gal, Phys. Lett. B 744, 352 (2015)



What about other systems
such as the **p-shell region**?
(theories predict small effect)

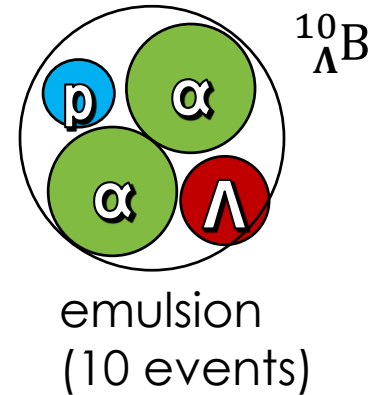
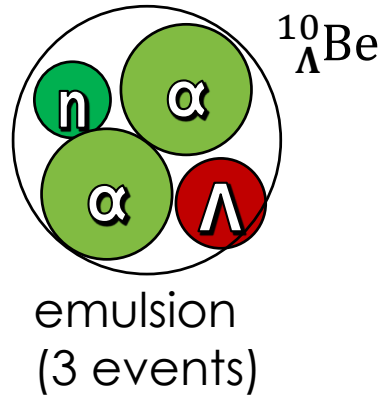
$$0.0297 \tau_{Nz} \frac{1}{\sqrt{3}} \langle N\Sigma | V_{CS} | N\Lambda \rangle$$

Charge symmetry breaking (CSB) in the p-Shell hypernuclei

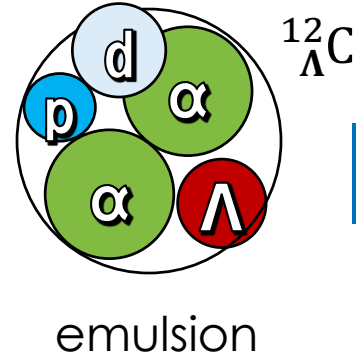
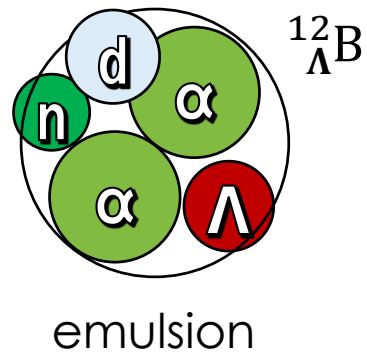


$$A = 7, T = 1$$

9.30 ± 0.26	MeV
8.91 ± 0.60	MeV
8.31 ± 0.61	MeV

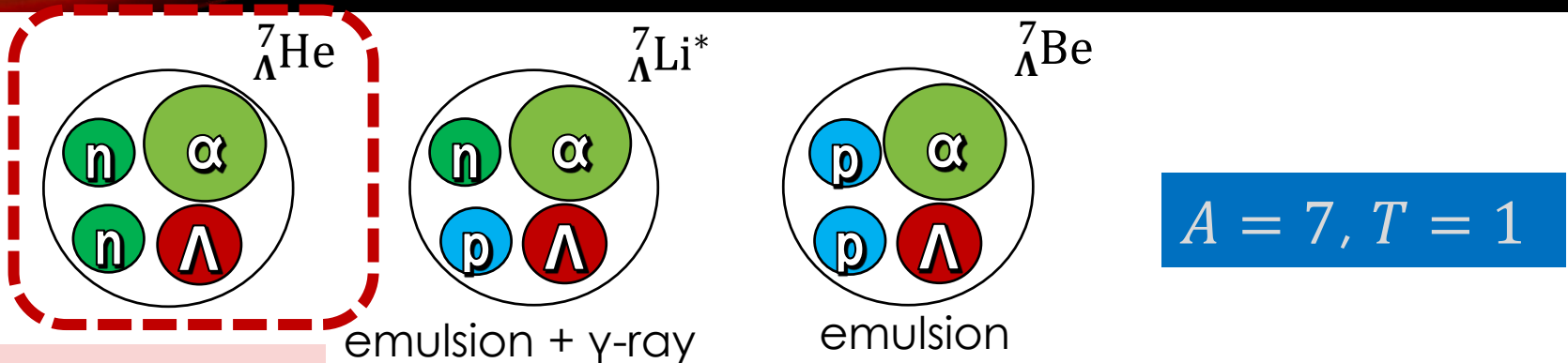


$$A = 10, T = 1/2$$



$$A = 12, T = 1/2$$

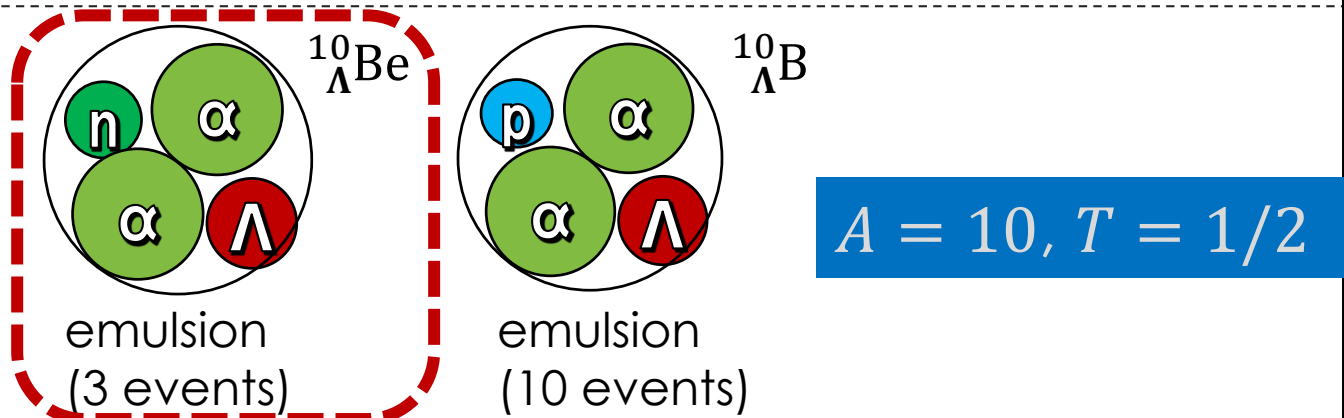
Charge symmetry breaking (CSB) in the p-Shell hypernuclei



$$A = 7, T = 1$$

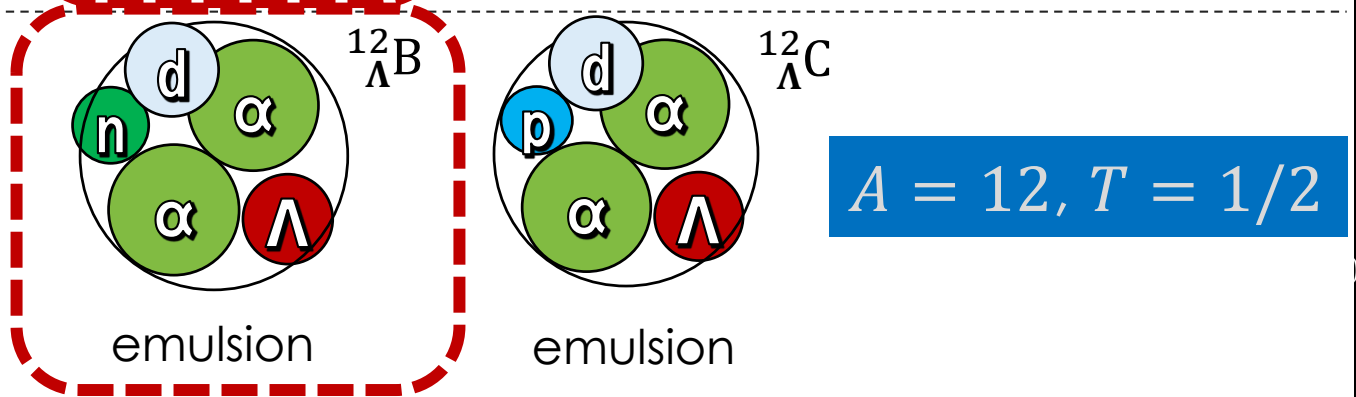
S.N.Nakamura, PRL 110, 012502 (2013).
 TG et al., PRC 94, 02132(R) (2016).

9.30 ± 0.26	MeV
8.91 ± 0.60	MeV
8.31 ± 0.61	MeV



$$A = 10, T = 1/2$$

TG et al., PRC 93, 034314 (2016).



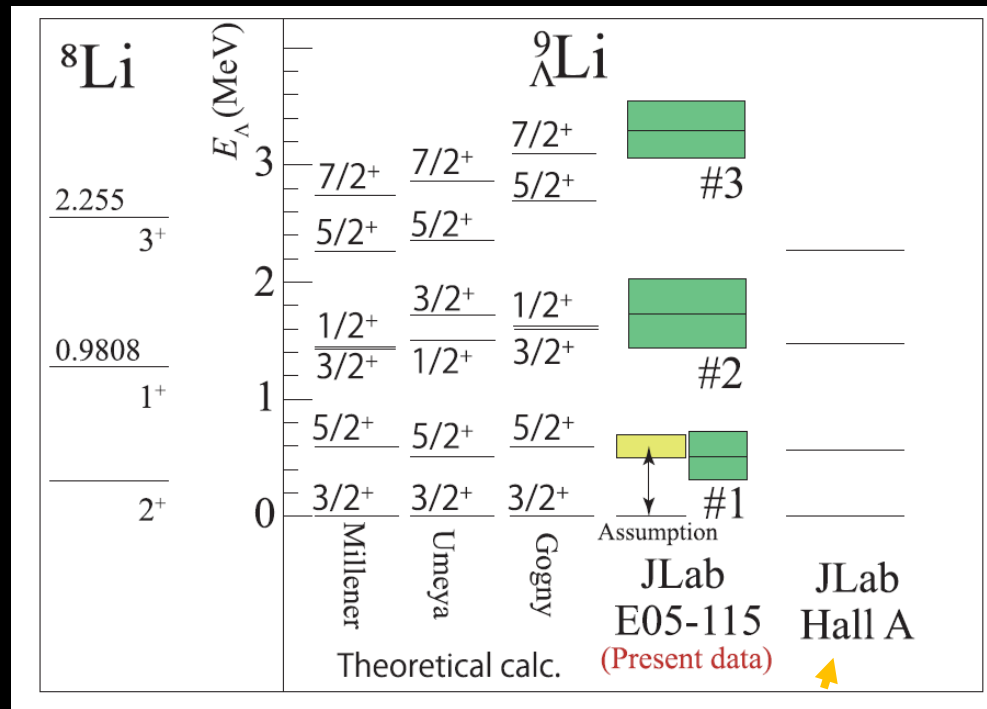
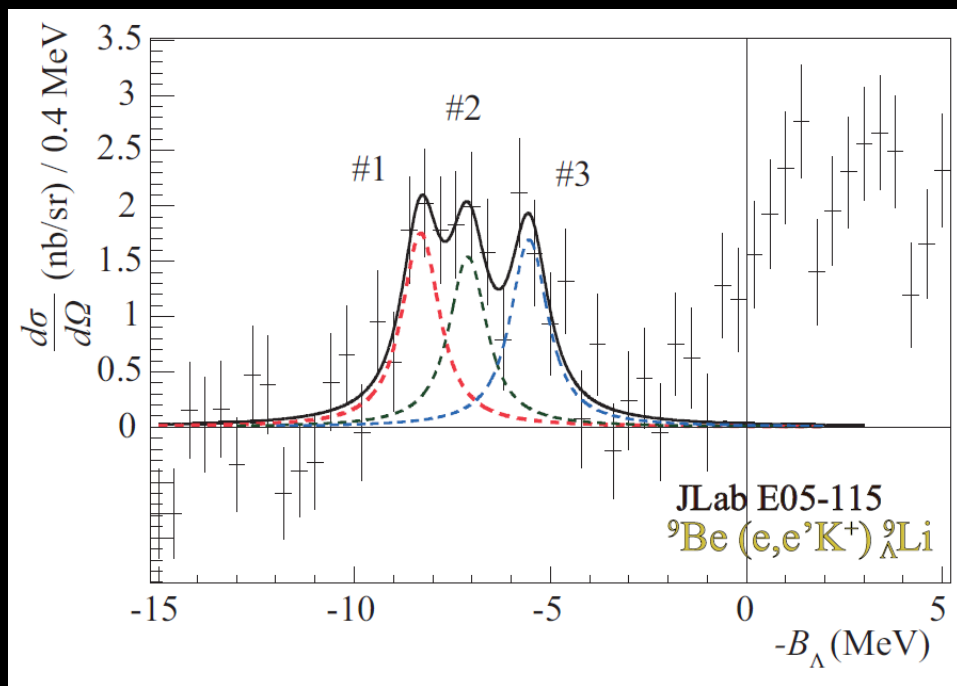
$$A = 12, T = 1/2$$

L. Tang et al., PRC 90, 034320 (2014).

CSB in the p-Shell hypernuclei

→ A = 9 iso-doublet hypernuclei (${}^9_{\Lambda}\text{Li}$ vs. ${}^9_{\Lambda}\text{B}$)

TG et al., Phys. Rev. C 103, L041301 (2021)



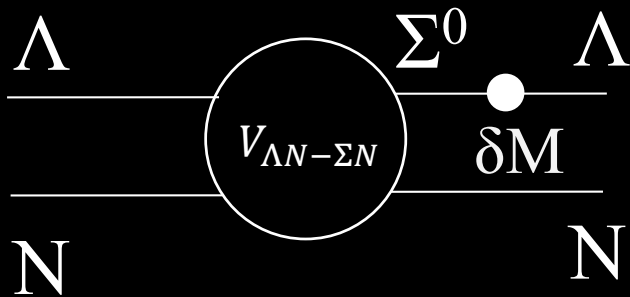
F. Garibaldi et al., Phys. Rev. C 99, 054309 (2019).

BASIC INFORMATION FOR THE ΛN CSB STUDY: ${}^4_{\Lambda}\text{He} - {}^4_{\Lambda}\text{H}$

Explicit inclusion of Σ

A. Gal, Phys. Lett. B 744, 352 (2015)

A. Gal et al., IOP Conf. Series: Jour. Phys.: Conf. Ser. 966 (2018) 012006



$$\langle N\Lambda | V_{CSB} | N\Lambda \rangle = -0.0297 \tau_{Nz} \frac{1}{\sqrt{3}} \langle N\Sigma | V_{CS} | N\Lambda \rangle$$

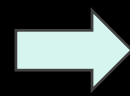
Phenomenological potential

E. Hiyama et al., Phys. Rev. C 80, 054321 (2009).

M. Isaka et al., Phys. Rev. C 101, 024301 (2020).

$$V_{\Lambda N}^{CSB}(r) = -\frac{\tau_z}{2} \left[\frac{1 + P_r}{2} \left(v_0^{\text{even,CSB}} + \sigma_{\Lambda} \cdot \sigma_N v_{\sigma_{\Lambda} \cdot \sigma_N}^{\text{even,CSB}} \right) e^{-\beta_{\text{even}} r^2} + \frac{1 - P_r}{2} \left(v_0^{\text{odd,CSB}} + \sigma_{\Lambda} \cdot \sigma_N v_{\sigma_{\Lambda} \cdot \sigma_N}^{\text{odd,CSB}} \right) e^{-\beta_{\text{odd}} r^2} \right]$$

**Basic Input
(This Experiment)**



**CSB
interaction**

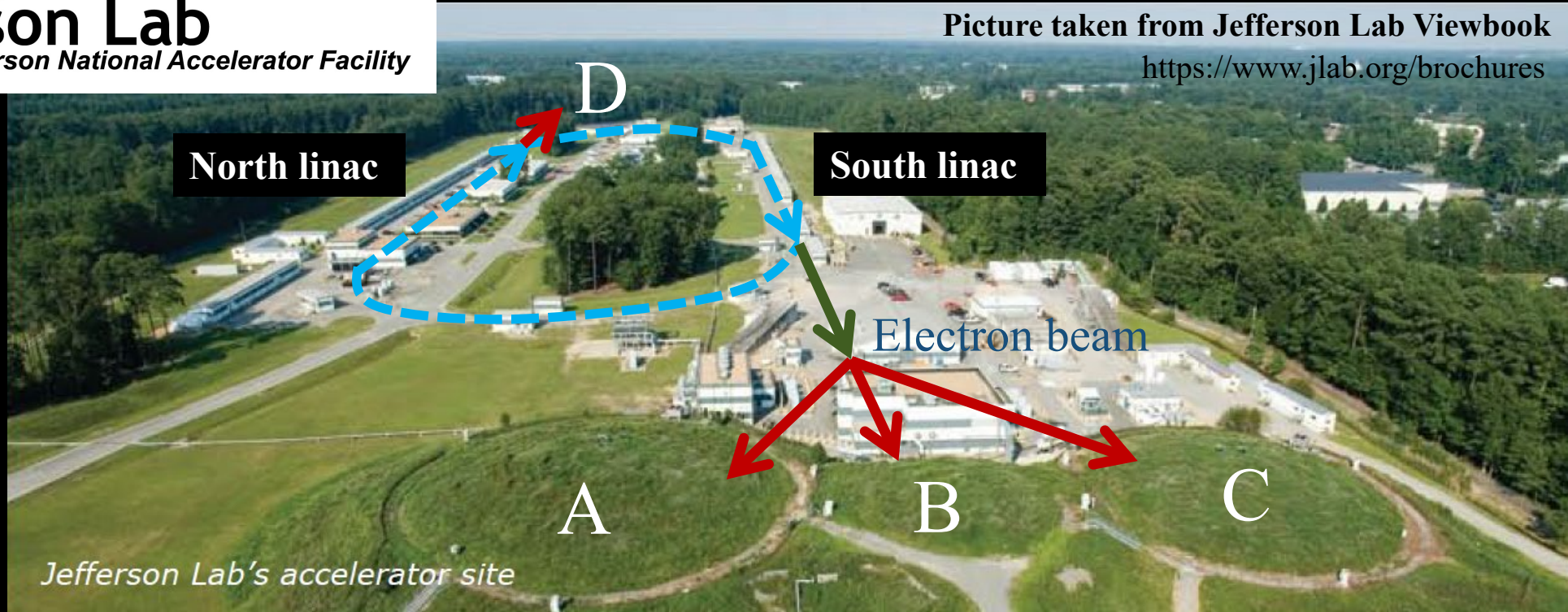
- $A=5$ HKS, PRL 110, 012502 (2013)
- $A=7$ HKS, PRC 94, 021302(R) (2016)
- $A=9$ Hall A, PRC 91, 034308 (2015)
- $A=10$ HKS, PRC103, L041301 (2021)
- \dots HKS, PRC 93, 034314 (2016)
- \dots HKS, PRC 90, 034320 (2014) ...

CEBAF AT JEFFERSON LAB

Jefferson Lab
Thomas Jefferson National Accelerator Facility

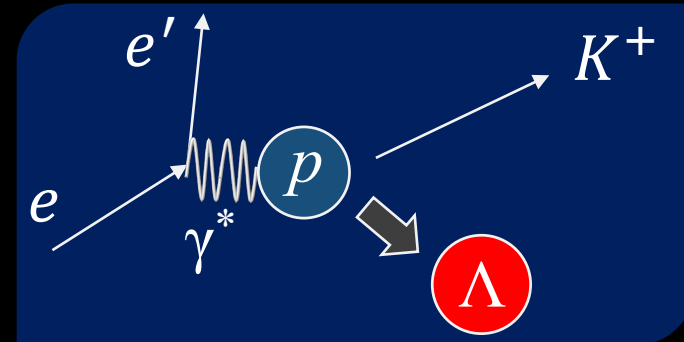
Picture taken from Jefferson Lab Viewbook

<https://www.jlab.org/brochures>

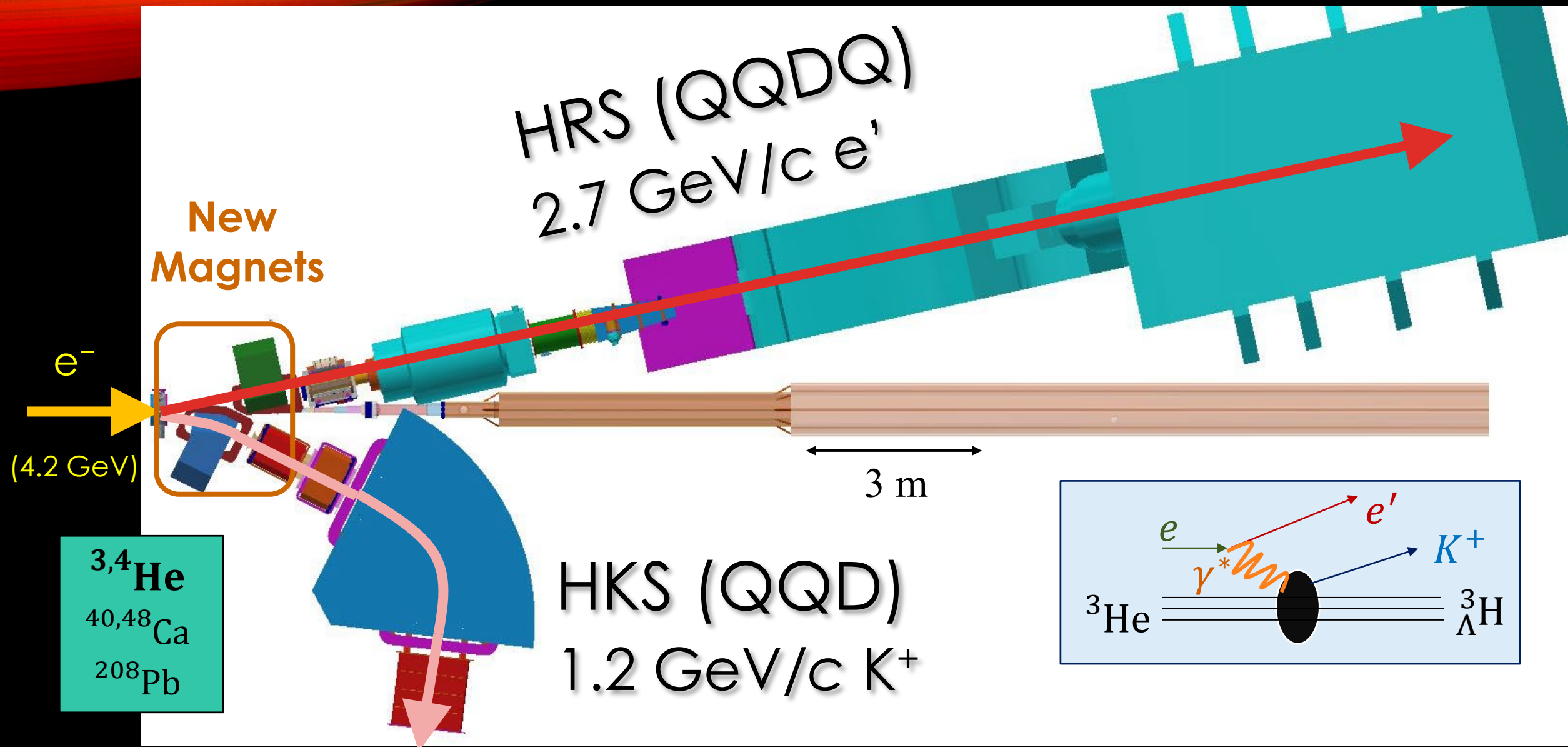


Continuous electron beam facility (CEBAF)

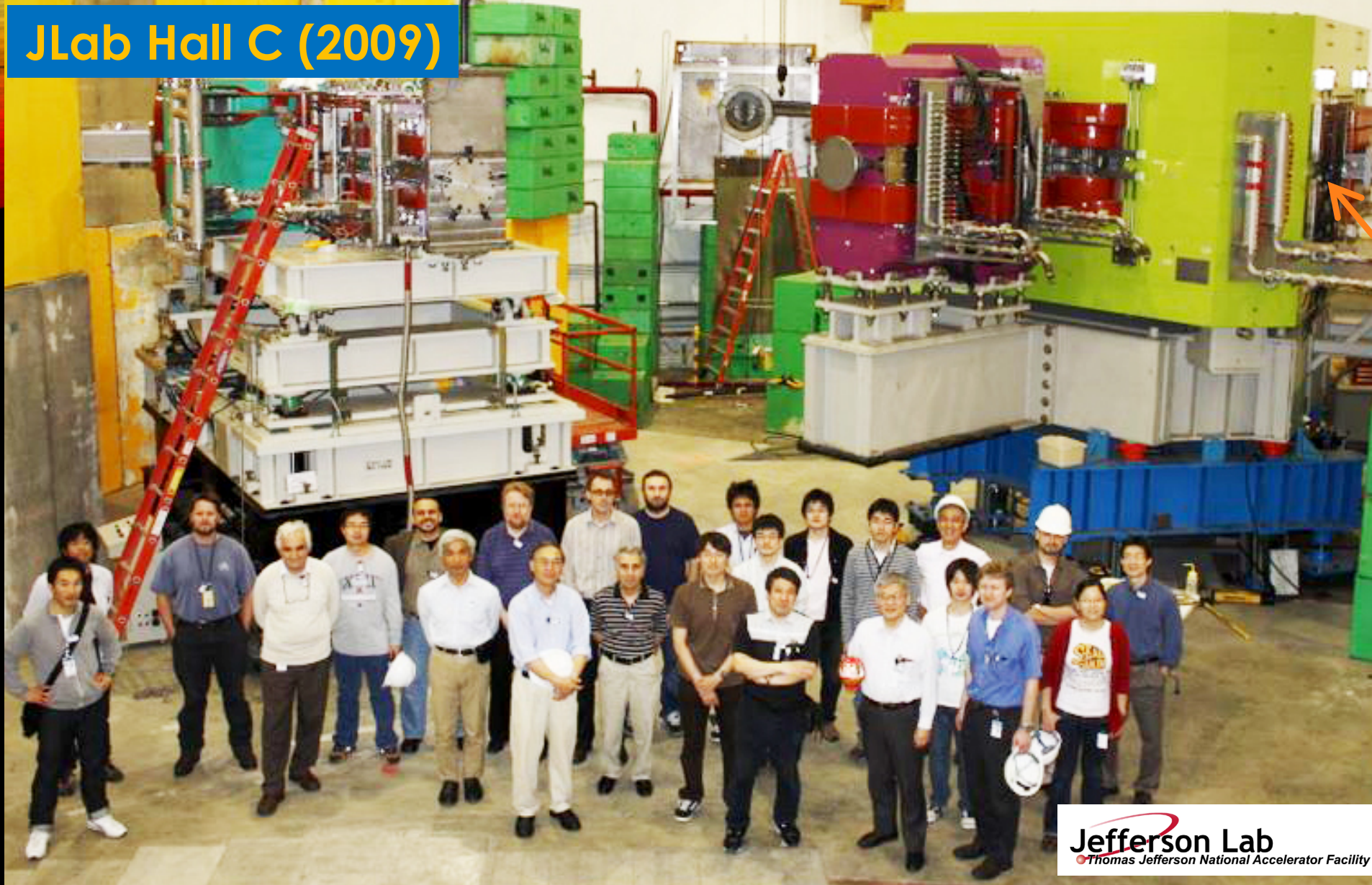
- ✓ 12 GeV at maximum
- ✓ 100 μA (> 600 THz)
- ✓ 2 or 4-ns interval bunches
- ✓ Emittance of 2 $\mu\text{m}\cdot\text{mrad}$
- ✓ Energy spread ($\Delta E/E < 5 \times 10^{-5}$ rms)



Experimental Setup at JLab Hall A



JLab Hall C (2009)



HKS

- TG et al., Nucl. Instrum Methods. Phys. A 729, 816—824 (2013)
- Y. Fujii et al., Nucl. Instrum Methods. Phys. A 795, 351—363 (2015)
- TG et al., Nucl. Instrum Methods. Phys. A 900, 69—83 (2018)

LHRS

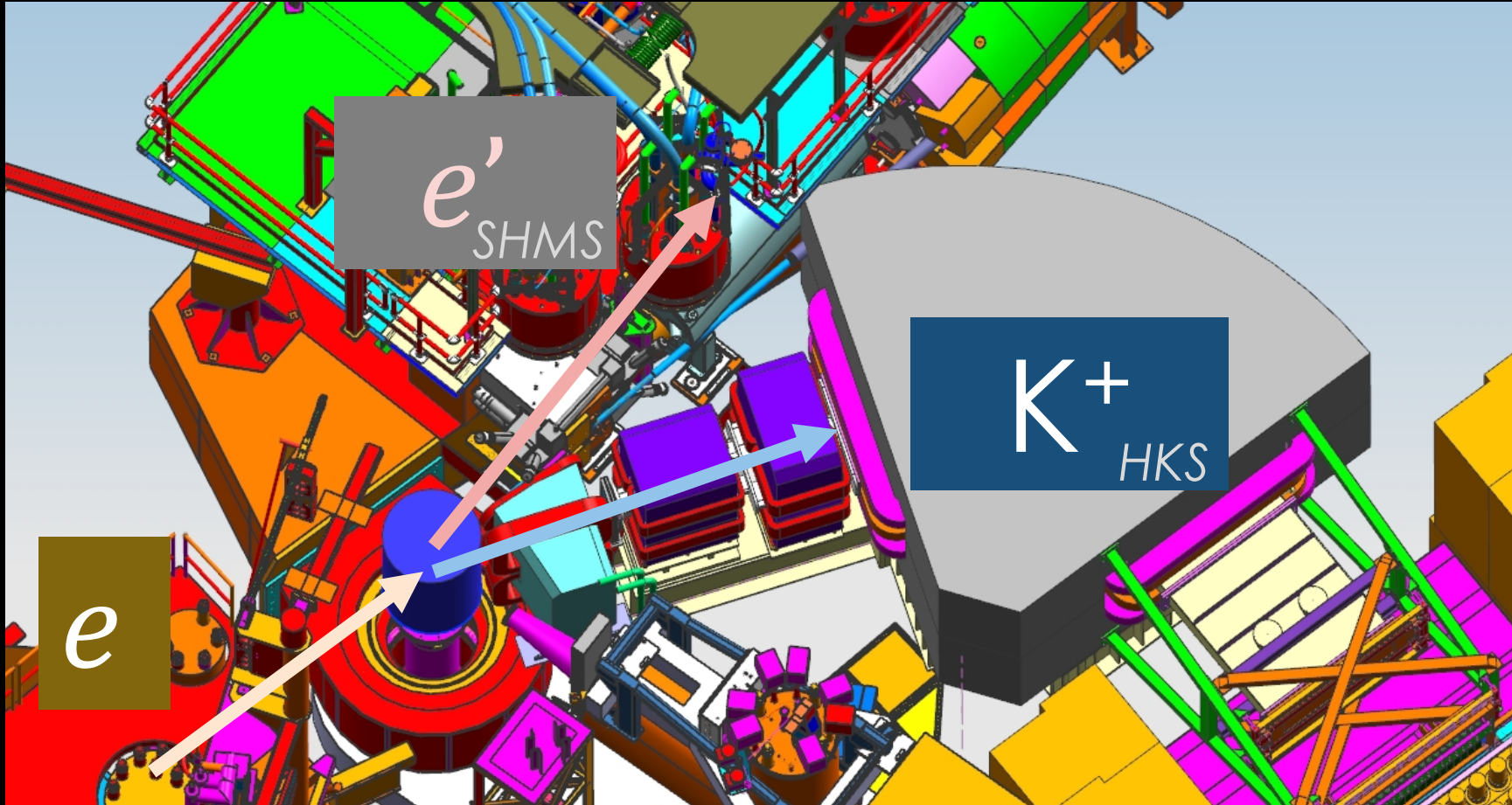
RHRS



JLab Hall A (Apr 2019)



Possibility in Hall C

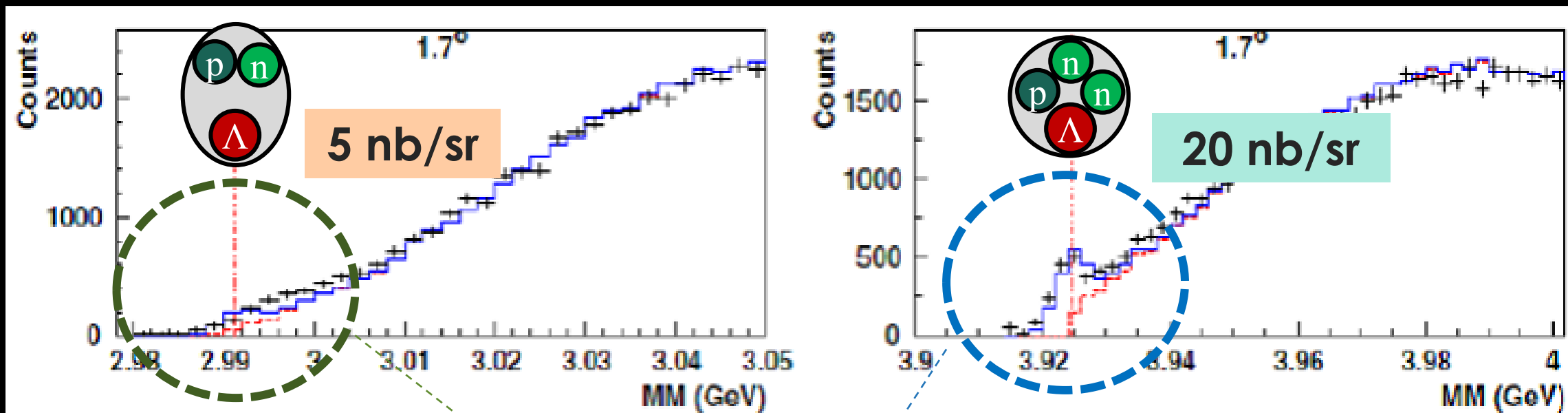


Evaluations are in progress

- SHMS + HKS
- Vertical HES + vertical HKS
- ...

YIELD ESTIMATION

F. Dohrmann et al., *Phys. Rev. Lett.* **93**, 242501 (2004).



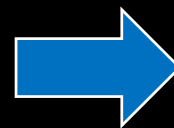
Product	Target [/(mg/cm ²)]	I_{beam} (/ μA)	CS [/(nb/sr)]	Yield / day	Beamtime (/day)	Total yield
$^3_{\Lambda}\text{H}$	^3He (165)	50	5	60	10	600
$^4_{\Lambda}\text{H}$	^4He (228)		20	250	2	500

CALIBRATION AND SYSTEMATIC ERROR ON B_Λ

Calibration	Target + Sieve Slit	Reaction	z_t range (mm)	Beamtime (day)	Remarks
Mom. + z_t	H	$p(e, e' K^+) \Lambda, \Sigma^0$	$-110 < z_t < 110$	1	$\Lambda: 3500, \Sigma^0: 1150$
Mom. + z_t	^{12}C (multi foils)	$^{12}\text{C}(e, e' K^+) ^{12}_\Lambda\text{B}$		1	$^{12}_\Lambda\text{B}^{\text{g.s.}}: 300 \times 5$
Angle + z_t	^{12}C (multi foils) + SS	-		0.2	
z_t	Empty	-	$-100 < z_t < 100$	0.1	+ Background study
	Empty (or gas) + SS	-		0.2	+ Angle resolution check
Physics	$^{3,4}\text{He}$	$^{3,4}_\Lambda\text{H}$	$-100 < z_t < 100$	12	

Major contributions to a systematic error on B_Λ

- Energy scale calibration^(*): ± 50 keV
- Energy loss correction: ± 23 keV
 - target density: $\pm 3\%$
 - cell thickness uniformity: $\pm 25 \mu\text{m}$



$$|\Delta B_\Lambda^{\text{sys.}}| = 55 \text{ keV}$$

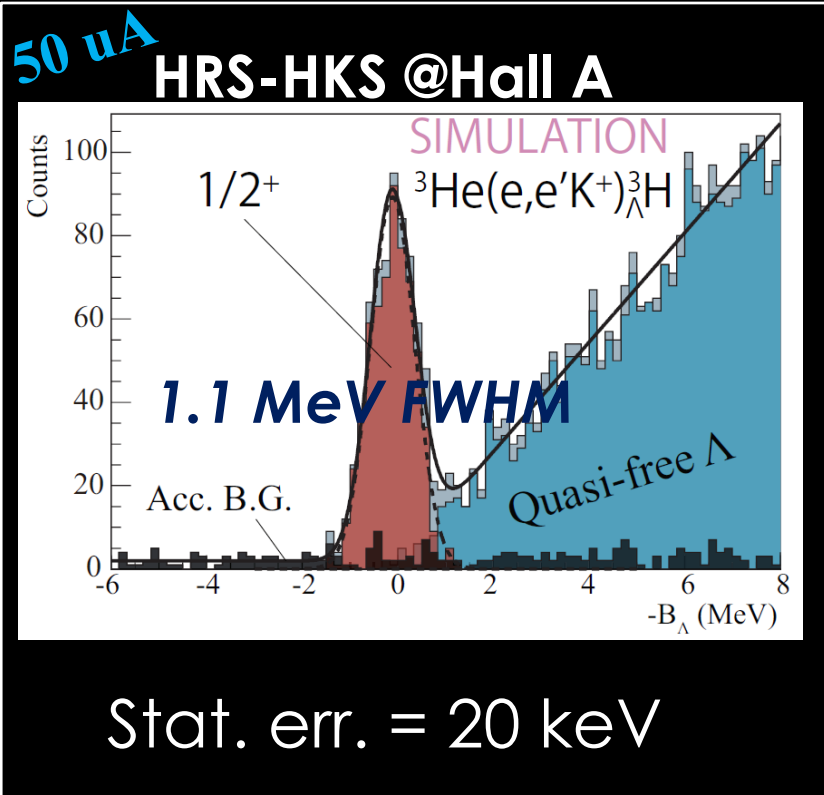


(T. Toyoda, "Basic design of gas targets for precise hypertriton mass measurement at JLab", Master's Thesis, Kyoto Univ. JFY2020)

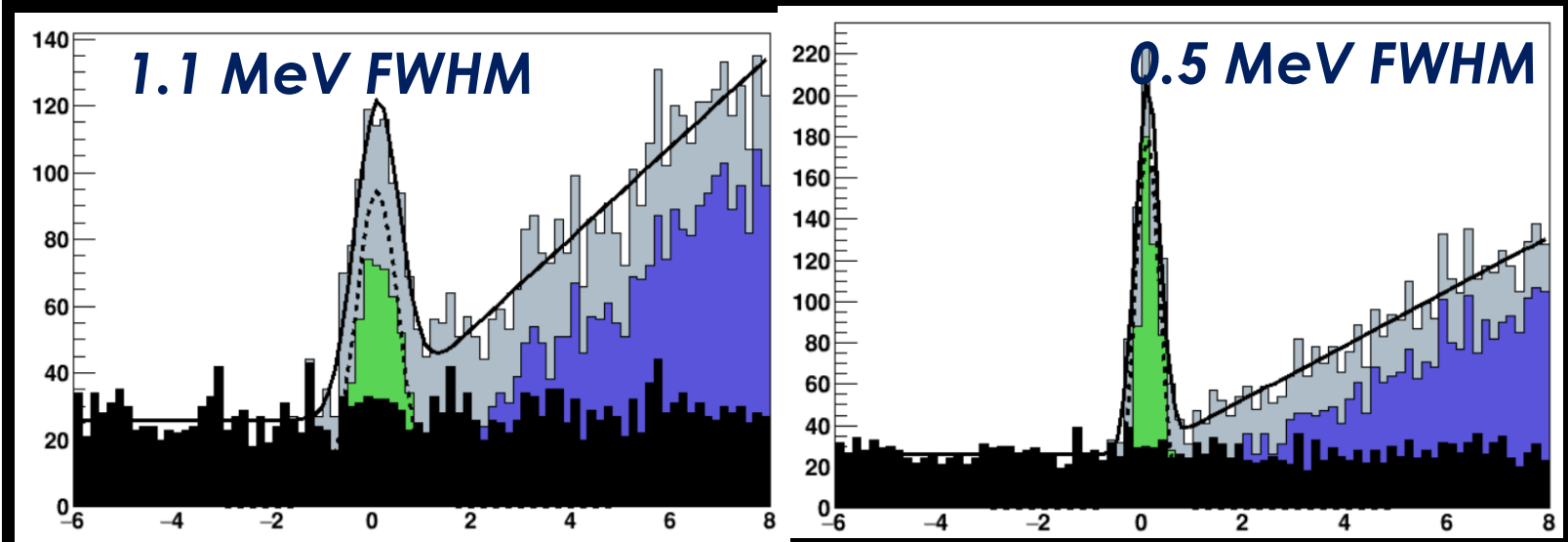
^(*) TG et al., NIMA 900 (2018) 69—83

S/N comparison between Hall A and C

- Assumed that the e^+e^- backgrounds are perfectly rejected
- Expected rate (HES-HKS) @20uA (2.5 MHz @8uA, 52Cr in E05-115):
 - 2.2 MHz (^3He , 190+162 mg/cm²) \rightarrow coin = 1.5 kHz
 - 3.6 MHz (^{40}Ca , 100 mg/cm²) \rightarrow coin = 1.3 kHz
 - 55.7 MHz (^{208}Pb , 100 mg/cm²) \rightarrow **coin = 18.4 kHz**



S/N: HES-HKS @Hall C, 20 uA



Stat. err. < 30 keV

Stat. err. < 20 keV